

# Degenerate Roots of Three Transcendental Equations Involving Spherical Bessel Functions

By Robert L. Pexton and Arno D. Steiger

**Abstract.** Roots of the three transcendental equations

$$j_l(\alpha\lambda)y_l(\lambda) = j_l(\lambda)y_l(\alpha\lambda),$$

$$[xj_l(x)]'_{x=\alpha\eta}[xy_l(x)]'_{x=\eta} = [xj_l(x)]'_{x=\eta}[xy_l(x)]'_{x=\alpha\eta},$$

and

$$[j_l(x)]'_{x=\alpha\mu}[y_l(x)]'_{x=\mu} = [j_l(x)]'_{x=\mu}[y_l(x)]'_{x=\alpha\mu}$$

that are degenerate for certain values of the parameter  $\alpha \in (0, 1)$  are presented. The symbols  $j_l$  and  $y_l$  denote the spherical Bessel functions of the first and second kind. Root degeneracies are discussed for each equation individually as well as for pairs of equations. Only positive roots are considered, since the equations are invariant under the transformations  $\lambda \rightarrow -\lambda$ ,  $\eta \rightarrow -\eta$ , and  $\mu \rightarrow -\mu$ . When  $l = 0$ , only the third equation has nontrivial roots. These roots are identical with the roots of the first equation for  $l = 1$ , i.e.  $\mu_{0n} = \lambda_{1n}$  ( $n = 1, 2, \dots$ ). Various graphs of  $\lambda_{ln}$ ,  $\eta_{ln}$ , and  $\mu_{ln}$  display root-degeneracies as intersections of curves. Accurate values of degenerate roots with the corresponding values of  $\alpha$  are exhibited in tables.

Roots of the third equation for  $l = 1(1)15$ ,  $n = 1(1)30$ ,  $\alpha = 0.1(0.1)0.7$ , together with their minima and associated values of the parameter  $\alpha$ , are given in the microfiche supplement accompanying this issue. Roots of the first and the second equation and minima of roots of the second equation are published in v. 31 and v. 32 of this journal.

The roots of the first two equations determine the eigenfrequencies of the transverse electric and the transverse magnetic normal modes of an ideal cavity resonator bounded by two concentric spheres ( $r = \alpha R$  and  $r = R$ ). The roots of the third equation determine the frequencies of the irrotational magnetic eigenfields.

In [1] roots of the transcendental equations

$$(1) \quad j_l(\alpha\lambda)y_l(\lambda) = j_l(\lambda)y_l(\alpha\lambda)$$

and

$$(2) \quad [xj_l(x)]'_{x=\alpha\eta}[xy_l(x)]'_{x=\eta} = [xj_l(x)]'_{x=\eta}[xy_l(x)]'_{x=\alpha\eta},$$

where  $j_l$  and  $y_l$  denote spherical Bessel functions of the first and second kind, are presented. In [2] these roots are analyzed as functions of the continuous real param-

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eter  $\alpha$ , where  $0 < \alpha < 1$ . The roots of (1) and (2) determine the eigenfrequencies of the transverse electric and the transverse magnetic normal modes of an ideal cavity resonator bounded by two concentric spheres ( $r = \alpha R$  and  $r = R$ ). While the normal modes constitute a complete set of eigenvectors for the expansion of an electromagnetic field in the isolated cavity, they no longer are a complete set of basis vectors if the cavity is coupled to a source of electromagnetic energy. In order to obtain such a complete set, it is necessary to add irrotational electric and magnetic multipole fields to the solenoidal fields of the normal modes. The characteristic frequencies of the irrotational electric multipole fields are also determined by Eq. (1). The characteristic frequencies of the irrotational magnetic multipole fields, however, are determined by the roots of the transcendental equation

$$(3) \quad [j_l(x)]'_{x=\alpha\mu} [y_l(x)]'_{x=\mu} = [j_l(x)]'_{x=\mu} [y_l(x)]'_{x=\alpha\mu}.$$

Roots of Eq. (3) were calculated by the procedure described in [1] and are presented in the microfiche supplement. The ranges of the parameter  $\alpha$ , of the order  $l$  of the spherical Bessel functions, and of the root index  $n$  are  $\alpha = 0.1(0.1)0.7$ ,  $l = 1(1)15$ ,  $n = 1(1)30$ . The minima of the roots of Eq. (3) are also presented in the microfiche supplement and were computed in the same way as the minima of Eq. (2) were calculated in [2].

Since

$$\begin{aligned} j_l(ze^{m\pi i}) &= e^{ml\pi i} j_l(z), \\ y_l(ze^{m\pi i}) &= (-1)^m e^{ml\pi i} y_l(z), \end{aligned} \quad (l, m = 0, 1, 2, \dots)$$

[3, p. 439, 10.1.34, 10.1.35], the equations (1), (2), and (3) are invariant under the transformations  $\lambda \rightarrow -\lambda$ ,  $\eta \rightarrow -\eta$ , and  $\mu \rightarrow -\mu$ , respectively. Therefore, only positive roots need be considered. The roots of Eqs. (1), (2), and (3), namely  $\lambda_{ln}$ ,  $\eta_{ln}$ , and  $\mu_{ln}$ , are labelled by the index  $n = 1, 2, \dots$  such that  $\lambda_{ln+1} > \lambda_{ln}$ ,  $\eta_{ln+1} > \eta_{ln}$ , and  $\mu_{ln+1} > \mu_{ln}$ . For  $l = 0$ , Eqs. (1) and (2) have no nontrivial solutions when  $0 < \alpha < 1$ . This is obvious, since for  $l = 0$  they can both be reduced to the form

$$\tan(\alpha\lambda) = \tan \lambda.$$

Furthermore, Eq. (3) for  $l = 0$  is identical with Eq. (1) for  $l = 1$ ,

$$\mu_{0n} = \lambda_{1n}, \quad n = 1, 2, \dots$$

For particular values of the parameter  $\alpha$  certain roots of the equations (1), (2), and (3) coincide. The following types of root degeneracies are considered

$$\begin{aligned} \lambda_{ln}(\alpha) &= \lambda_{l'n'}(\alpha), & (l, n) &\neq (l', n'), \\ \eta_{ln}(\alpha) &= \eta_{l'n'}(\alpha), & (l, n) &\neq (l', n'), \\ \mu_{ln}(\alpha) &= \mu_{l'n'}(\alpha), & (l, n) &\neq (l', n'), \end{aligned} \quad (4)$$

and

$$(5) \quad \begin{aligned} \lambda_{ln}(\alpha) &= \eta_{l'n'}(\alpha), \\ \lambda_{ln}(\alpha) &= \mu_{l'n'}(\alpha), \\ \eta_{ln}(\alpha) &= \mu_{l'n'}(\alpha). \end{aligned}$$

The graphs, Figures 1 through 4, which show the dependence of various roots  $\lambda_{ln}$ ,  $\eta_{ln}$ , and  $\mu_{ln}$  on the parameter  $\alpha$ , exhibit as intersections of curves some of the root degeneracies (4) and (5).

Write Eqs. (1), (2), and (3) as

$$\begin{aligned} (1') \quad F_l(\alpha, \lambda) &= 0, \quad \text{where } F_l(\alpha, \lambda) = j_l(\alpha\lambda)y_l(\lambda) - j_l(\lambda)y_l(\alpha\lambda), \\ (2') \quad G_l(\alpha, \eta) &= 0, \quad \text{where } G_l(\alpha, \eta) = s_l(\alpha\eta)t_l(\eta) - s_l(\eta)t_l(\alpha\eta), \\ &s_l(x) = xj_{l-1}(x) - ly_l(x), \quad t_l(x) = xy_{l-1}(x) - ly_l(x), \end{aligned}$$

and

$$(3') \quad \begin{aligned} K_l(\alpha, \mu) &= 0, \quad \text{where } K_l(\alpha, \mu) = v_l(\alpha\mu)w_l(\mu) - v_l(\mu)w_l(\alpha\mu), \\ v_l(x) &= j_{l-1}(x) - \frac{l+1}{x}j_l(x), \quad w_l(x) = y_{l-1}(x) - \frac{l+1}{x}y_l(x). \end{aligned}$$

If  $p_{ln}$  or  $q_{ln}$  represent any one of the roots  $\lambda_{ln}$ ,  $\eta_{ln}$ , and  $\mu_{ln}$ , and if  $P_l$  or  $Q_l$  represent any one of the functions  $F_l$ ,  $G_l$ , and  $K_l$ , then the algorithm used to compute degenerate roots can be stated as follows:

*Step 1.* Input values for  $l$ ,  $n$ ,  $l'$ ,  $n'$ ,  $\alpha$ ,  $\Delta\alpha$ ,  $p_{ln}$ ,  $q_{l'n'}$ ,  $\Delta p_{ln}$ ,  $\Delta q_{l'n'}$ ,  $\epsilon$ ,  $dd$ ,  $t$ , where  $p_{ln}$ ,  $q_{l'n'}$  and  $\alpha$  are approximations for the desired degenerate root and the associated value of the parameter. The approximations can readily be obtained from the graphs or the root tables.

- $\epsilon$  error tolerance for  $|p_{ln} - q_{l'n'}|$
- $dd$  coefficient used to decrease  $\Delta\alpha$
- $t$  determines the sign of  $\Delta\alpha$ . Initially  $t = 1$ .

*Step 2.* With the current value of  $\alpha$  compute new values of  $p_{ln}$  and  $q_{l'n'}$  such that

$$P_l(\alpha, p_{ln}) = 0 \quad \text{and} \quad Q_l(\alpha, q_{l'n'}) = 0.$$

*Step 3.* Test the new roots. If  $|p_{ln} - q_{l'n'}| < \epsilon$ , we have our desired degenerate root and associated value  $\alpha$ .

*Step 4.* Otherwise, if  $(p_{ln} - q_{l'n'})t < 0$ , then  $-t \rightarrow t$  and  $dd\Delta\alpha \rightarrow \Delta\alpha$ .

*Step 5.*  $\alpha + t\Delta\alpha \rightarrow \alpha$ . Return to Step 2.

A FORTRAN program implementing this algorithm computes values of the degenerate roots (4) and (5) together with the associated values of  $\alpha$  to near machine accuracy. Results are presented in Tables 1 through 6.

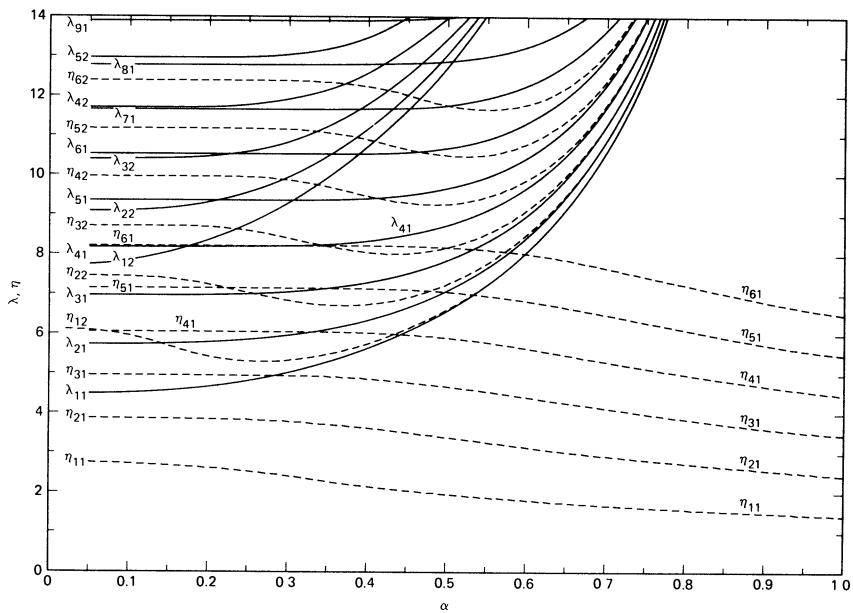


FIGURE 1

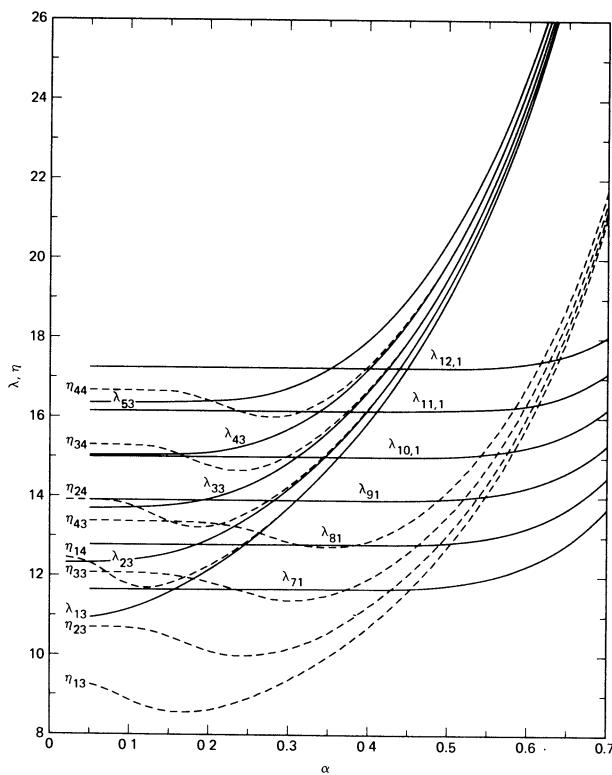


FIGURE 2

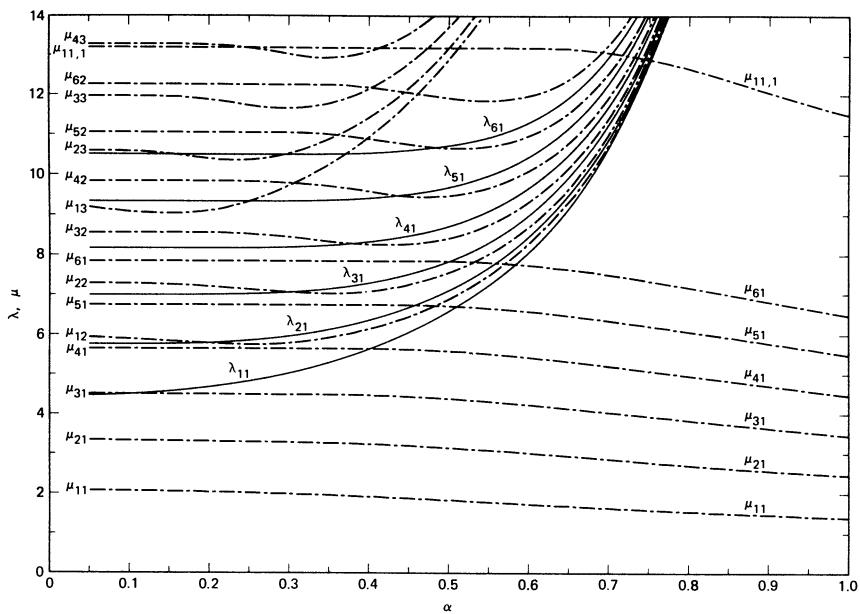


FIGURE 3

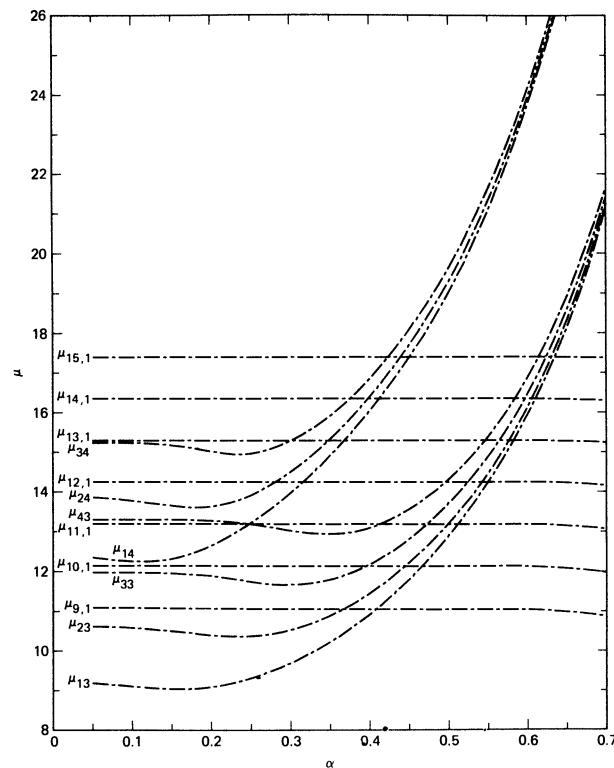


FIGURE 4

TABLE 1

(L N	L'N')	ALPHA	LAMBDA L N	=LAMBDA L'N'
4 1	1 2	1.7126280679338E-01	8.1827583831863E+00	
5 1	1 2	3.0409732823857E-01	9.3613355361517E+00	
6 1	1 2	3.8976135002034E-01	1.0532706055389E+01	
6 1	2 2	3.5386004528366E-01	1.0520195451432E+01	
6 1	3 2	2.2097368533374E-01	1.0512868726504E+01	
7 1	1 2	4.5437133153515E-01	1.1700001008926E+01	
7 1	1 3	1.5561575902538E-01	1.1657032221077E+01	
7 1	2 2	4.3360736305650E-01	1.1682964958136E+01	
7 1	3 2	3.9132959670722E-01	1.1650087032676E+01	
8 1	1 2	5.0576934362594E-01	1.2864655267768E+01	
8 1	1 3	2.4512007807570E-01	1.2790784560892E+01	
8 1	2 2	4.9311925714532E-01	1.2845000200407E+01	
8 1	3 2	4.6761080775992E-01	1.2820563923668E+01	
8 1	4 2	4.2082322482786E-01	1.2798735665857E+01	
9 1	1 2	5.4792997100230E-01	1.4027463366049E+01	
9 1	1 3	3.1159812200931E-01	1.3915849824674E+01	
9 1	2 2	5.3830422197287E-01	1.4006383094531E+01	
9 1	2 3	2.8402501739023E-01	1.3915828212438E+01	
9 1	3 2	5.2197951870556E-01	1.3978168461079E+01	
9 1	3 3	1.9978525072569E-01	1.3915822621344E+01	
9 1	4 2	4.9509609241442E-01	1.3947734440023E+01	
9 1	5 2	4.4467217849102E-01	1.3923184183159E+01	
10 1	1 2	5.8325888352305E-01	1.5188915448963E+01	
10 1	1 3	3.6552966752839E-01	1.5033586473287E+01	
10 1	2 2	5.7614980031642E-01	1.5167149736328E+01	
10 1	2 3	3.4833291387055E-01	1.5033518544033E+01	
10 1	3 2	5.6447336371849E-01	1.5136868983422E+01	
10 1	3 3	3.1393437146020E-01	1.5033476537993E+01	
11 1	1 2	6.1334878454385E-01	1.6349335806599E+01	
11 1	1 3	4.1080728016735E-01	1.6145080366711E+01	
11 1	2 2	6.0791916366849E-01	1.6327346699072E+01	
11 1	2 3	3.9892636166092E-01	1.6144937075439E+01	
11 1	3 2	5.9917971203256E-01	1.6296054654392E+01	
11 1	3 3	3.7770573236507E-01	1.6144810875390E+01	
11 1	4 3	3.3748506326985E-01	1.6144750217050E+01	
12 1	1 2	4.4959836288581E-01	1.7251218533827E+01	
12 1	2 3	4.4089502244773E-01	1.7250975357694E+01	
12 1	3 3	4.2616668360948E-01	1.7250719265198E+01	
12 1	4 3	4.0193870378578E-01	1.7250534757090E+01	
12 1	5 3	3.5686684458354E-01	1.7250460870201E+01	

TABLE 2

(L N	L'N')	ALPHA	ETA L N	=ETA L'N'
1 4	3 3	7.1506742584463E-02	1.2063302630523E+01	
1 4	3 3	1.7269587060611E-01	1.1971485186709E+01	
2 4	4 3	1.4739100984938E-01	1.3375996312163E+01	
2 4	4 3	2.1447582237830E-01	1.3301666048358E+01	
4 1	1 2	7.0010866660159E-02	6.0619493542981E+00	
4 1	1 2	4.3458767568285E-01	6.0030517595060E+00	
5 1	2 3	2.2766429824463E-01	7.1401934217484E+00	
5 1	2 2	4.7752997364267E-01	7.0874487501519E+00	
6 1	1 2	5.9706171548852E-01	8.0176551250788E+00	
6 1	2 2	5.7280039842735E-01	8.0738795809855E+00	
6 1	3 2	3.4650343360255E-01	8.2102063139689E+00	
6 1	3 2	5.0211244439851E-01	8.1713407895880E+00	

TABLE 3

(L N	L'N')	ALPHA	MU L N	=MU L'N'
4 2	1 3	3.0560166436990E-01	9.7768178761880E+00	
5 1	1 2	4.8095936180034E-01	6.7286219288186E+00	
5 2	1 3	3.9712594537559E-01	1.0907437280180E+01	
5 2	2 3	3.6017923608757E-01	1.0985809391387E+01	
6 1	1 2	5.6975608228212E-01	7.7799021272269E+00	
6 1	2 2	5.3008031720922E-01	7.8151404673729E+00	
6 2	1 3	4.6086226890926E-01	1.2027472118634E+01	
6 2	2 3	4.4235479078226E-01	1.2082141526461E+01	
6 2	3 3	4.0086360642163E-01	1.2183767505963E+01	
11 1	1 2	7.5245224521590E-01	1.2900218460577E+01	
11 1	1 3	5.1289565648331E-01	1.3201822683999E+01	
11 1	2 2	7.4842642924687E-01	1.2916571602170E+01	
11 1	2 3	4.9970788799001E-01	1.3202131098528E+01	
11 1	3 2	7.4187972123218E-01	1.2942076321558E+01	
11 1	3 3	4.7477568847200E-01	1.3202436363935E+01	
11 1	4 2	7.3197615271535E-01	1.2978024567707E+01	
11 1	4 3	2.4213818395278E-01	1.3202620396698E+01	
11 1	4 3	4.1327087559330E-01	1.3202608622369E+01	
11 1	5 2	7.1694914307867E-01	1.3026357464333E+01	
11 1	6 2	6.9211056986977E-01	1.3089897269223E+01	

TABLE 4

(L N	L'N')	ALPHA	ETA L N	=LAMBDA L'N'
1 2	2 1	1.3689030947367E-01	5.7698729929792E+00	
2 2	3 1	2.5490599344310E-01	7.0125755915093E+00	
3 1	1 1	2.8204263961059E-01	4.9628270089990E+00	
3 2	1 2	2.3275232200162E-01	8.6404980615129E+00	
3 2	4 1	3.4191635465948E-01	8.2299074031068E+00	
4 1	1 1	4.4340090404323E-01	5.9938297878784E+00	
4 1	2 1	3.3126377223292E-01	6.0548990423623E+00	
4 2	1 2	3.3538474533576E-01	9.7467178201989E+00	
4 2	2 2	2.9128555571748E-01	9.8790007045619E+00	
4 2	5 1	4.0829201719491E-01	9.4274365569750E+00	
5 1	1 1	5.3467701345668E-01	7.0073191021999E+00	
5 1	2 1	4.9554033050096E-01	7.0678976923855E+00	
5 1	3 1	3.5099931773671E-01	7.1373138327947E+00	
5 2	1 2	4.0869156889741E-01	1.0845663836043E+01	
5 2	2 2	3.8840362512342E-01	1.0943687737015E+01	
5 2	3 2	3.3614281815884E-01	1.1101578465420E+01	
5 2	6 1	4.6069883942953E-01	1.0609231450974E+01	
6 1	1 1	5.9788204763506E-01	8.0155350185321E+00	
6 1	1 2	1.7571383663424E-01	8.2108418325225E+00	
6 1	2 1	5.7691251645373E-01	8.0652340589106E+00	
6 1	3 1	5.3278531610879E-01	8.1399928443295E+00	
6 1	4 1	3.1781767672858E-01	8.2106145469471E+00	
6 2	1 2	4.6613765809816E-01	1.1945702066588E+01	
6 2	2 2	4.5195326790701E-01	1.2015244502132E+01	
6 2	3 2	4.2624725825721E-01	1.2134521594576E+01	
6 2	4 2	3.7206387075334E-01	1.2308868562633E+01	
6 2	7 1	5.0325034503418E-01	1.1778232641012E+01	

TABLE 5

(L N	L'N')	ALPHA	MU L N	= LAMBDA L'N'
1 2	2 1	1.9772652403568E-01	5.7978760571995E+00	
1 3	5 1	2.5328228275670E-01	9.3567654234745E+00	
1 3	6 1	3.7047960270123E-01	1.0524710853371E+01	
2 2	3 1	3.0582883643917E-01	7.0585791986358E+00	
2 3	6 1	1.5518972152495E-01	1.0512835028998E+01	
2 3	6 1	2.9717742615205E-01	1.0513921759296E+01	
3 1	1 1	8.8968075131997E-02	4.5140980452001E+00	
3 2	4 1	3.8473298267519E-01	8.2885288005756E+00	
4 1	1 1	3.9915602451889E-01	5.6327241415465E+00	
4 2	5 1	4.4493361027329E-01	9.4955108800748E+00	
5 1	1 1	5.1154937581843E-01	6.7092762876190E+00	
5 1	2 1	4.5771229756763E-01	6.7385473904137E+00	
5 2	6 1	4.9257661295007E-01	1.0684757078089E+01	
6 1	1 1	5.8381749833796E-01	7.7625837496334E+00	
6 1	2 1	5.5807931870672E-01	7.7922454482169E+00	
6 1	3 1	4.9833756415319E-01	7.8317911293936E+00	
11 1	2 1	7.5063221509005E-01	1.2907673777424E+01	
11 1	1 1	7.5437582202699E-01	1.2892228576026E+01	
11 1	3 1	7.4461769841400E-01	1.2931575676039E+01	
11 1	4 1	7.3571932123530E-01	1.2964815574344E+01	
11 1	5 1	7.2278727362398E-01	1.3008476135871E+01	
11 1	6 1	7.0343701937221E-01	1.3063400003542E+01	

TABLE 6

(L N	L'N')	ALPHA	MU LN	= ETA L'N'
1 3	1 3	6.3289226469119E-02	9.1761179764685E+00	
2 3	2 3	1.3291182914516E-01	1.0557617071159E+01	
3 3	1 4	7.8698037003981E-02	1.1972438464397E+01	
3 3	1 4	1.6847453074461E-01	1.1935272056718E+01	
4 3	1 4	2.6549491005295E-01	1.3139594547296E+01	
9 1	1 3	4.2113462436406E-01	1.1879274136952E+01	
9 1	2 3	3.9090746881455E-01	1.1879376976673E+01	
10 1	1 3	4.7479710312284E-01	1.2142770261848E+01	
10 1	1 4	6.5333002137485E-02	1.2143204100943E+01	
10 1	1 4	1.9041480082058E-01	1.2143204100935E+01	
10 1	2 3	4.5687185169372E-01	1.2142984799306E+01	
10 1	3 3	4.1866597226675E-01	1.2143159104602E+01	

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 MR 31 #1400.

Robert L. Paxton and Arno D. Steiger, Degenerate Roots of Three Transcendental Equations Involving Spherical Bessel Functions, p. 1041.

PAC

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61      X1=XOO
62      F1=FUN(XOO)
63      OO = T+I*INN/IMAX
64      X=XOO+I*DELK
65      F2=FUN(X)
66      IF(F1+F2.GT.0.0) 196,199
67
68 196      X1=X2
69      X2=X
70      P=DELK*VALUE
71      X2=X
72      CALL HYPOL(FUNX,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)
73      ROOT1=X1,889,ROOT2
74      M=MAX(1,889,ROOT2)
75      3 DIF=(ROOT1-ROOT2)/M
76      77 IF(DIF.GT.EPS) 10,11
77      11 IF(DIFGT1.LT.0.0) 20,21
78      20 DELA=DELA00
79      21 DELA=DELA00
80      22 WRITE (3,885) A
81      885 WRITE (12,886) A,ROOT1,ROOT2,L,M,LPR,NPR
82      19 CALL (3,889) A,ROOT1,ROOT2,L,M,LPR,NPR
83      998 FORMAT (8X,3E20.13,4I10)
84      END
85
86

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87 FUNCTION FUNC(X)
88 COMMON /PEXT/LA,LPR,LHM,LM,LP,LPRP
89 REAL JA(0,5),YALM,YAL(L),YAL(LM)
90 C SPHERICAL BESSEL FUNCTION OF THE 1ST & 2ND KIND
91 C (AL(LM) J SUB L OF X YAL(L) + Y SUB L OF X
92 C AL(LM)) * J SUB L OF X YAL(L) + Y SUB L OF X
93 C AL(LM) = J SUB L OF X YAL(L)
94 C AX = X*JA(LM)
95 CALL SJYNECIA(X,JA,YAL(L))
96 TML = X*JA(LM)
97 TML = TML - LP*YA(L)
98 TML = TML - LP*YA(LM)
99 FUNC = TML*(X*YA(LM)-LP*YA(L))-TML*(X*JA(LM)-LP*JA(L))
99 RETURN
99 END

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100 FUNCTION FUNK(X)
101 COMMON /PEXTL/LA,LPR,X,LPRM,LP,LPRP
102 REAL X(10,50),Y(10,50)
103 C SPHERICAL BESSEL FUNCTION OF THE 1ST & 2ND KIND
104 C J(L,X) = J SUB L OF X   Y(L,X) = Y SUB L OF X
105 C X*X*X
106 C LA(L,X)=X*L*JA(L,X)/IN(LPR)
107 C LP(L,X)=X*L*JA(L,X)/IN(LPR)
108 C LPR=L*IN(LPR)
109 C LPRM=L*IN(LPRM)
110 C TEMR=AX*Y(LPRM)-LPR*YA(LPR)
111 C TEL=AX*J(LPRM)-LPR*JA(LPR)
112 C FUNK=TEML+(X*YA(LPRM)-LPR*YA(LPR))-TEMR*(X*JA(LPRM)-LPR*JA(LPR))
113 RETURN
114 END

```

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113 C
114 C SUBROUTINE INVOL(FUN,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)
115 C
116 C
117 C A STABLE METHOD OF INVERSE INTERPOLATION
118 C J M BLATT
119 C
120 C
121 C THE AUSTRALIAN COMPUTER JOURNAL
122 C VOL. 7 #2 JULY, 1975 PP. 51-57
123 C
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172 C
      A METHOD
      AT EVERY STAGE OF THE ITERATION AT LEAST ONE ROOT
      IS GUARANTEED TO LIE WITHIN THE INTERVAL (X1,X2).
      IF CERTAIN CONDITIONS HOLD THE ROUTINE CALCULATES THE
      NEXT APPROXIMATION USING MULLER'S QUADRATIC POLYNOMIAL
      APPROXIMATION. OTHERWISE A LINEAR APPROXIMATION IS USED.
      REDUCED VARIABLES ARE USED FOR THE MULLER APPROXIMATION.

      INVERSE INTERPOLATION BY MODIFIED MULLER METHOD

      INPUT REQUIREMENTS
      FUN=FUNCTION NAME WE WANT TO FIND X SUCH THAT F(X)=0.
      NOTE THE ACTUAL NAME MUST BE DECLARED EXTERNAL IN THE
      CALLING PROGRAM
      X1=X-VALUE AT ONE END OF INTERVAL
      X2=X-VALUE AT OTHER END OF INTERVAL
      BY ASSUMPTION, Y1 AND Y2 HAVE OPPOSITE SIGNS. ROUTINE
      CHECKS THIS, RETURNS WITH ITOL=-1 IF UNTRUE
      XTOL=TOLERANCE ON ROOT, I.E. ON ABS(X1-X2) AT THE END
      YTOL=OPTIONAL TOLERANCE ON ABS(Y), IGNORED IF >0.
      ITOL=MAX NO OF ITERATIONS (IF ITOL LE 0, ITOL=60)

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173 C
174 C
175 C
176 C
177 C
178 C      AFTER RETURN FROM ROUTINE
179 C
180 C      (X1,Y1) AND (X2,Y2) ARE THE BEST POINTS FOUND
181 C      ABS(Y1) LE ABS(Y2)
182 C      IF(Y1.NE.0) THEN Y1 AND Y2 HAVE OPPOSITE SIGNS.
183 C      ITOL IS THE ACTUAL NO. OF ITERATIONS USED.  IF THE
184 C      INITIAL POINTS WERE CHOSEN SO BADLY THAT Y1 AND Y2
185 C      HAD THE SAME SIGN, THEN ITOL IS SET TO -1, AND WE
186 C      EXIT IMMEDIATELY.
187 C
188 C      USER MUST SUPPLY
189 C
190 C      1. AN ACTUAL FUNCTION NAME TO REPLACE THE NOMINAL "FUN"
191 C      2. VALUES OF X1,X2,XTOL.
192 C      3. OPTIONALY: VALUES OF YTOL,ITOL.
193 C      4. FUNCTION SUBPROGRAM, OF DECLARED NAME, TO EVALUATE
194 C         F(X)
195 C
196 C      5. WITHIN THE CALLING PROGRAM, AN "EXTERNAL" DECLARATION
197 C         FOR THAT FUNCTION NAME.
198 C
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200 C
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208 C
209 C
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211 C
212 C
213 C
214 C      DIMENSION X(3),Y(3)
215 C      I1=1      X1=X(1)      SITER=0      $MULLER=0
216 C      ITCM=1      SNOTCH=1      XTOL=ABS(X(TOL))
217 C      YTOL=ABS(Y(TOL))      ITOL=ABS(I(TOL))      ITOL=60
218 C      X(1)=X1      Y(1)=Y1      FUN(X1)=F(X1)
219 C      Y(2)=Y1      FUN(X2)=F(X2)      X(2)=X1+X2
220 C      Y(3)=Y1      FUN(X3)=F(X3)      X(3)=X1+X2
221 C      ITOL=-1      IF(YTOL.LT.0) ITOL=9100      1100,9000,1050
222 C      ITOL=9100      IF(X1.EQ.X2) ITOL=9000
223 C      IF(X1.EQ.X2) LE YTOL.OR.ABS(X(1))-X(2)) LE XTOL.OR.ITER.GE.ITOL
224 C      C 00 TO 9000
225 C
226 C
227 C      TO DISPLAY INTERMEDIATE VALUES REMOVE THE "C" IN
228 C      COLUMN 1 OF THE FOLLOWING CARDS
229 C
230 C
231 C
232 C
233 C

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233 C
234      DEBUB PRINTING
235 C
236 C      WRITE (3,223) I,X,ITER,MULLER,ITCH,NOTCH,Miller,JJ
237 C      2323 FORMAT (B15)
238 C      2323 FORMAT (B15) X(1),X(2),X(3),YNEW
239 C      WRITE (3,242) Y(1),Y(2),Y(3),YNEW
240 C      WRITE (3,242) Y(1),Y(2),Y(3),YNEW
241 C      2424 FORMAT (B5.4E25.13)
242 C
243 C      ITEM=ITER+1   SPH(10,5,SMILLER+1,SIF((ITCH.LE.0).GO TO 1150
244 C      1150 MILLER=2    SIF(MULLER.GE.5).GO TO 2000
245 C      1150 MILLER=1    SIF(MULLER.GE.5).GO TO 2000
246 C      1150 MILLER=0    SIF(MULLER.GE.5).GO TO 2000
247 C      IF(ALPHA.LE.1.0D1) GO TO 1550   SIF(ALPHA.GE.1000.0) GO TO 2000
248 C      BETA=1.0D0
249 C      B=(ALPHA+1.0)*GAMMA/ALPHA+(ALPHA-BETA/ALPHA)/(ALPHA-1.0)
250 C      T1=B*(1.0D0-GAMMA)/B+SQR((B*1.0D0-GAMMA)*(B*2.4D0-GAMMA))
251 C      PH=(B*2.0D0-GAMMA)/B+SQR((B*1.0D0-GAMMA)*(B*2.4D0-GAMMA))
252 C      MILLER=3    SMULLERMULLER=1.0D0 GO TO 2000
253 C      1550 PH=MILLER*1.0D0
254 C      1550 MILLER=MILLER+1.0D0
255 C      1550 MILLER=MILLER+1.0D0,0.5
256 C
257 C      PATHS REJOIN
258 C
259 C      2000 XNEW=X(1)+PH*((X(2)-X(1))
260 C      IF(XNEW.EQ.X(1) OR XNEW.EQ.X(2)) GO TO 9000
261 C      IF(XNEW.FUN(XNEW).LT.0.3*MIN(ABS(Y(1)),ABS(Y(2)))) GO TO 10
262 C      C GO TO 10
263 C
264 C      A MULLER-TYPE ITERATION HAS PROVED UNSUCCESSFUL.
265 C      INITIATE A NEWTON-TYPE ITERATION FOR A FEW TIMES.
266 C      AND UP THE NUMBER OF INHIBITIONS FOR THE NEXT
267 C      SUCH OCCURRENCE
268 C
269 C      ITCH=NOTCH  NOTCH=NOTCH+1
270 C      2010 JJ=1
271 C      IF(MILLER.EQ.0.0D0 OR ABS(Y(1)).GT.ABS(Y(1))) GO TO 2000
272 C
273 C      DISCARD POINT I
274 C      X(1)=XNEW
275 C      Y(1)=YNEW
276 C      900 TO 2060
277 C      PREPARE FOR SWITCHING LABELS I AND K
278 C
279 C      2020 JJ+2
280 C
281 C      DISCARD POINT K
282 C
283 C      2040 X(1)+X(2)  Y(1)+Y(2)  X(2)+XNEW  Y(2)+YNEW
284 C
285 C      TEST FOR PRECISE ROOT.
286 C      2060 IF(Y(2).EQ.0.0D0 GO TO 8000  900 TO (1100,2100),JJ
287 C
288 C      INTERCHANGE LABELS I AND K
289 C
290 C      2100 JJ+1  S1+K  SK+JJ  900 TO 1100

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312 C SUBROUTINE SJYMEC(X,Y,MN,OUT)      SPHERICAL
313 C JSUBN(X),JSUBN(X)      SPHERICAL BESSEL FUNCTIONS
314 C DO 100 I=1,10          JSUB N (D) , FOR ALL N GE 0
315 C JSUB0,0=1,1,JSUB N (D),0, FOR ALL N GE 0
316 C Y=JSUB N (X),1,J SUB (-(N+1)),X, FOR ALL N GE 0
317 C Y SUB N (X),1,J SUB ((N+1)),X, FOR ALL N GE 0
318 C MN=MN+1,UPWARD RECURSION FOR DESIRED BESSEL FUNCTIONS COMPUTED
319 C OUT=MN,MAXIMUM SUBROUTINE OF DESIRED BESSEL FUNCTIONS
320 C RECURRENCE TECHNIQUE FOR BESSEL FUNCTIONS
321 C FOR MORE INFORMATION ON BESSEL FUNCTIONS SEE VOL 22 NO 101 JAN 1968
322 C REAL J,JK
323 C DIMENSION X(10,200),Y(10,200)
324 C THE DIMENSION OF X AND Y MAY BE VARIED TO SUIT THE USERS NEEDS
325 C DATA NMAX,NADD,ALPHA,NADD0/10,10,10,10/
326 C BOUND1,NADD,ALPHA,NADD0 MAY BE VARIED
327 C NADD0=20,IS NUMBER OF TERMS IN THE CONTINUED FRACTION
328 C MN=MN-20,IS INT(X)-10,AND Y0=CONTFR(X/X)
329 C X1=X-10,X2=X-10,X3=X-10,X4=X-10
330 C UPWARD RECURSION VALID FOR N>X FOR BOTH BESSEL FUNCTIONS
331 C JSUBN(X)=JSUBN(X)*JSUBN(X-1)/JSUBN(X-1)*JSUBN(X-1)
332 C JSUBN(X)=JSUBN(X)*JSUBN(X-1)/JSUBN(X-1)*JSUBN(X-1)
333 C JSUBN(X)=JSUBN(X)*JSUBN(X-1)/JSUBN(X-1)*JSUBN(X-1)
334 C JSUBN(X)=JSUBN(X)*JSUBN(X-1)/JSUBN(X-1)*JSUBN(X-1)
335 C UPWARD RECURSION FOR JSUBN(X) TO OBTAIN GOOD GUESS FOR JSUBN(X)
336 C DO 200 I=MN,1,-1,X=JN-1,I,JSUBN(X-1),JSUBN(X-1)
337 C 1 MN=INT(X)+1,X=JN-1,I,JSUBN(X-1),JSUBN(X-1)
338 C 2 MN=MN-MAX(X-1),SIMAX=MN-MAX(X-1),NADD=100,I=JN-1
339 C 3 MN=MN-MAX(X-1),SIMAX=MN-MAX(X-1),NADD=100,I=JN-1
340 C DEVELOP CONTINUED FRACTION TO OBTAIN GOOD GUESS FOR JSUBN+1(X)
341 C P1=1.0,P2=1.0,Q1=1.0,Q2=1.0,B1=1.0,B2=1.0
342 C P1=P1*B1,P2=P2*B2,Q1=Q1*B1,Q2=Q2*B2
343 C P1=P1*B1,P2=P2*B2,Q1=Q1*B1,Q2=Q2*B2
344 C CONTINUE
345 C DO 2 MN=MN,0,MN=1,-1,X=MN-1,MN,JSUBN(X)
346 C 1 MN=MN-1,X=MN-1,MN,JSUBN(X)
347 C 2 MN=MN-1,X=MN-1,MN,JSUBN(X)
348 C 3 MN=MN-1,X=MN-1,MN,JSUBN(X)
349 C IF (X.LT.-E3) RETURN
350 C JSUBN(X)=JSUBN(X)*JSUBN(X)
351 C JSUBN(X)=JSUBN(X)*JSUBN(X)
352 C END

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61     C13 BX 7HROOT < ,E20 131
62     F1+F2
63     X1
64     1(FIN GE 3D) 4,1
65     1 CONTINUE
66     R=PAGENO-1
67     WRITE-(5,35) PAGENO
68     35 FORM(1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1)
69     3 CONTINUE
70     3 CONTINUE
71     END EXIT
72     END
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73  FUNCTION FUNC(X)
74  C          REAL JA(0,500), YA(0,500)
75  C          Spherical Bessel Functions of the 1st & 2nd kind
76  C
77  C          JA(L) = J SUB L OF X, YA(L) = Y SUB L OF X
78  C
79  C          AX=XA(L)
80  C          OME=SUYNEC(X, YA, MN, L)
81  C          TEML=AX*JA(LM)-LP*JA(L)
82  C          TERR=(X*YA(LM)-LP*YA(L))
83  C          CALL SUYNEC(X, YA, MN, L)
84  C          FUNC=TEML+(X*YA(LM)-LP*YA(L))-TERR*(X*JA(LM)-LP*JA(L))
85  C
86  RETURN
87  END

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145 C

SUBROUTINE NVPOL(FUN,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)

      A STABLE METHOD OF INVERSE INTERPOLATION
      J. M. BLATT

      THE AUSTRALIAN COMPUTER JOURNAL
      VOL. 7 #2 JULY, 1975    PP 51-57

METHOD
AT EVERY STAGE OF THE ITERATION AT LEAST ONE ROOT
IS GUARANTEED TO LIE WITHIN THE INTERVAL (X1,X2).

IF CERTAIN CONDITIONS HOLD THE ROUTINE CALCULATES THE
NEXT APPROXIMATION USING MULLER'S QUADRATIC POLYNOMIAL
APPROXIMATION. OTHERWISE A LINEAR APPROXIMATION IS USED.

"REDUCED VARIABLES" ARE USED FOR THE MULLER APPROXIMATION.

INVERSE INTERPOLATION BY MODIFIED MULLER METHOD

INPUT REQUIREMENTS
FUNCTION NAME. WE WANT TO FIND X SUCH THAT F(X)=0.
NOTE THE ACTUAL NAME MUST BE DECLARED EXTERNAL IN THE
CALLING PROGRAM.
X1=X-VALUE AT ONE END OF INTERVAL.
X2=X-VALUE AT OTHER END OF INTERVAL.
BY ASSUMPTION, Y1 AND Y2 HAVE OPPOSITE SIGNS. ROUTINE
CHECKS THIS, RETURNS WITH ITOL=1 IF UNTRUE.
XTOL=TOLERANCE ON ROOT, I.E. ON ABS(X1-X2) AT THE END
YTOL=OPTIONAL TOLERANCE ON ABS(Y1), IGNORED IF =0.
ITOL=MAX.NO. OF ITERATIONS. IF ITOL.LE. 0, ITOL=60.

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AFTER RETURN FROM ROUTINE
(X1,Y1) AND (X2,Y2) ARE THE BEST POINTS FOUND
ABS(Y1).LE.ABS(Y2)
IF(Y1.NE.0) THEN Y1 AND Y2 HAVE OPPOSITE SIGNS
ITOL IS THE ACTUAL NO. OF ITERATIONS USED. IF THE
INITIAL POINTS WERE CHOSEN SO BADLY THAT Y1 AND Y2
HAD THE SAME SIGN, THEN ITOL IS SET TO -1, AND WE
EXIT IMMEDIATELY.
USER MUST SUPPLY
1. AN ACTUAL FUNCTION NAME TO REPLACE THE NOMINAL "FUN"
2. VALUES OF X1,X2,XTOL
3. OPTIONALY, VALUES OF YTOL,ITOL
4. FUNCTION SUBPROGRAM, OF DECLARED NAME, TO EVALUATE
F(X)
5. WITHIN THE CALLING PROGRAM, AN "EXTERNAL" DECLARATION
FOR THAT FUNCTION NAME.

DIMENSION X(3),Y(3)
ITER=0  SHULLER=0
ITCH=1  SNOTCH=1  XTOL=ABS(XTOL)
YTOL=ABS(YTOL)  IF((XTOL.EQ.0).OR.(YTOL.EQ.0)) ITOL=-60
X(1)=X1  Y(1)=Y1  FUN=X1*Y1
X(2)=X2  Y(2)=Y2  SIF(Y(1)).NE.Y(2))
IF((Y(1)-Y(2)).LT.0) SIF(Y(1)).Y(2)) 1100,9000,1050
1050  C 900 TO 9000
1000  IF(ABS(Y(2)).LE.YTOL.OR.ABS(X(1)-X(2)).LE.XTOL .OR. ITER.GE.ITOL)
C 900 TO 9000
TO DISPLAY INTERMEDIATE VALUES REMOVE THE "C" IN
COLUMN 1 OF THE FOLLOWING CARDS

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206 C          DEBUG PRINTING
207 C
208 C      2323  WRITE( 9,2323 ) I,K,ITER,MULLER,ITCH,NOTCH,MILLER,JJ
209 C      2324  WRITE( 9,2324 ) X(1),X(2),X(3),XNEW
210 C      2325  WRITE( 9,2324 ) Y(1),Y(2),Y(3),YNEW
211 C      2326  WRITE( 9,2324 ) PH
212 C      2327  FORMAT( 2X,4E25.13)
213 C
214 C      2424  FORMAT( 2X,4E25.13)
215 C
216 C      ITER,ITER+1,SPN(1,0,5,SMILLER)+1,SIF(ITCH LE 0) GO TO 1150
217 C      ITCH,ITCH+1, 500 TO 2000
218 C      1150  IF(X(1)-XNEW LE 5.E-5) GO TO 2000
219 C      IF(X(2)-EQ(X(1)) GO TO 9000  SALPHA*(X(1)-X(2))/(X(2)-X(1))
220 C      IF(X(3)-EQ(X(1)) GO TO 9000  SALPHA*(X(1)-X(2))/(X(2)-X(1))
221 C      BEALPHA(Y(2),0.001) GO TO 1000  SALPHA GE 1000.0 GO TO 2000
222 C      BEALPHA(Y(2),0.001) GO TO 1000  SALPHA LE 1000.0 GO TO 2000
223 C      B+ALPHA/Y(2)=SALPHA+ALPHA*BETA/ALPHA+(ALPHA-BETA)/2000
224 C      IF(B+ALPHA/Y(2) LE 0.001) GO TO 1000
225 C      PH=(2*0.5*GAMMA)/(B+SORT((B+12*0.5*GAMMA)**2+24*0.5*GAMMA))
226 C      MUL=1.0/(PH*(B+12*0.5*GAMMA)) GO TO 2000
227 C      PHI=AMAX1(1,0.2*DIALPHA-1,0.0,0.5)
228 C
229 C      PATHS REJOIN
230 C
231 C      2000 XNEW=X(1)+PH*(X(2)-X(1))
232 C      IF(XNEW EQ X(1) OR XNEW EQ X(2)) GO TO 9000
233 C      IF(MULLER NE 3 OR ABS(YNEW)-LT 0.3*MIN(ABS(Y(1)),ABS(Y(2)))) GO TO 2010
234 C
235 C      A MULLER-TYPE ITERATION HAS PROVED UNSUCCESSFUL
236 C      INHIBIT MULLER-TYPE ITERATIONS FOR A FEW TIMES
237 C      AND UP THE NUMBER OF INHIBITIONS FOR THE NEXT
238 C      SUCH OCCURRENCE
239 C
240 C      1010  ITCH=NOTCH
241 C      1020  X(1)=XNEW
242 C      1030  Y(1)=YNEW
243 C      1040  ITCH=NOTCH
244 C      1050  IF(MULLER EQ 1 OR ABS(Y(1)) GT ABS(Y(1))) GO TO 2040
245 C      1060  IF(Y(2) EQ 0.0) GO TO 8000
246 C      1070  TEST FOR PRECISE ROOT
247 C      1080  DISCARD POINT I
248 C
249 C      X(1)=XNEW
250 C      Y(1)=YNEW
251 C      2060  PREPARE FOR SWITCHING LABELS I AND K
252 C
253 C      2030  JJ=2
254 C
255 C      DISCARD POINT K
256 C      2040  X(1)=X(2)
257 C      2050  SY(1)=Y(2)
258 C      2060  SY(2)=XNEW
259 C      2070  SY(1)=Y(2)
260 C      2080  IF(Y(2) EQ 0.0) GO TO 8000
261 C      2090  GO TO (1100,2100),JJ
262 C      2100  INTERCHANGE LABELS I AND K
263 C      2100  JJ=I
264 C      2100  SY=K
265 C      2100  SY=JJ
266 C      2100  GO TO 1100

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286 C      FINISHED
288 C
289 C      Y(2) WAS EXACTLY ZERO. SELECT THE BEST OTHER ONE.
290 C
291 C      9000 IF(ABS(Y(K)) LT ABS(Y(1))) !K
292 C
293 C      REPORT NO. OF ITERATIONS USED.
294 C
295 C      9000 ITOL+ITER
296 C
297 C      REPORT THE TWO BEST POINTS FOUND
298 C
299 C      9100 IF(ABS(Y(12)) LE ABS(Y(1))) GO TO 9200
300 C      1112      $12=2      900 TO 9300
301 C      9200 K1=X(12)      $Y1=Y(1)
302 C      9300 K1=X(11)      $Y1=Y(11)      $X2=X(12)      $Y2=Y(12)
303 C      RETURN
304 C      END
```

PAGE

**INPUT PARAMETERS**

LMIN	=1
LYMX	=15
DELX	=1.0
XB	=1.0
ATOL	=1.0E-12
YTOL	=0.0
IMIN	=1
ITMX	=1000
ITOLB	=50
END	

```

1 ROOTS OF EQUATION 3
R = 0.10 L = 1 N = 1      ROOT = 3.0782433453798E+00
R = 0.10 L = 1 N = 2      ROOT = 5.9888384413978E+00
R = 0.10 L = 1 N = 3      ROOT = 9.1145918690435E+00
R = 0.10 L = 1 N = 4      ROOT = 1.2508311588014E+01
R = 0.10 L = 1 N = 5      ROOT = 1.5427349947224E+01
R = 0.10 L = 1 N = 6      ROOT = 1.8659358444722E+01
R = 0.10 L = 1 N = 7      ROOT = 2.1801111111111E+01
R = 0.10 L = 1 N = 8      ROOT = 2.5296752929981E+01
R = 0.10 L = 1 N = 9      ROOT = 2.8675891163345E+01
R = 0.10 L = 1 N = 10     ROOT = 3.1980000000000E+01
R = 0.10 L = 1 N = 11     ROOT = 3.5495352092359E+01
R = 0.10 L = 1 N = 12     ROOT = 3.8933853904223E+01
R = 0.10 L = 1 N = 13     ROOT = 4.2280000000000E+01
R = 0.10 L = 1 N = 14     ROOT = 4.5829492713989E+01
R = 0.10 L = 1 N = 15     ROOT = 4.9286724599653E+01
R = 0.10 L = 1 N = 16     ROOT = 5.2748500000000E+01
R = 0.10 L = 1 N = 17     ROOT = 5.6243116489325E+01
R = 0.10 L = 1 N = 18     ROOT = 5.9683016138011E+01
R = 0.10 L = 1 N = 19     ROOT = 6.3154238196344E+01
R = 0.10 L = 1 N = 20     ROOT = 6.6626000000000E+01
R = 0.10 L = 1 N = 21     ROOT = 7.012653965072E+01
R = 0.10 L = 1 N = 22     ROOT = 7.357527503655E+01
R = 0.10 L = 1 N = 23     ROOT = 7.7026500000000E+01
R = 0.10 L = 1 N = 24     ROOT = 8.0536260603993E+01
R = 0.10 L = 1 N = 25     ROOT = 8.4016305339523E+01
R = 0.10 L = 1 N = 26     ROOT = 8.7470000000000E+01
R = 0.10 L = 1 N = 27     ROOT = 9.097888668222E+01
R = 0.10 L = 1 N = 28     ROOT = 9.4461238559810E+01
R = 0.10 L = 1 N = 29     ROOT = 9.7944300000000E+01
R = 0.10 L = 1 N = 30     ROOT = 1.014276303247E+02

```

```

1
1 ROOTS OF EQUATION 3
R = 0.10 L = 2 N = 1      ROOT = 3.34196594670427E+00
R = 0.10 L = 2 N = 2      ROOT = 7.2065427232245E+00
R = 0.10 L = 2 N = 3      ROOT = 1.05973351517864E+01
R = 0.10 L = 2 N = 4      ROOT = 1.3945452559563E+01
R = 0.10 L = 2 N = 5      ROOT = 1.7294291523010E+01
R = 0.10 L = 2 N = 6      ROOT = 2.0837689139275E+01
R = 0.10 L = 2 N = 7      ROOT = 2.3157639354095E+01
R = 0.10 L = 2 N = 8      ROOT = 2.5487444444444E+01
R = 0.10 L = 2 N = 9      ROOT = 2.9553613337851E+01
R = 0.10 L = 2 N = 10     ROOT = 3.26369957255556E+01
R = 0.10 L = 2 N = 11     ROOT = 3.5738000000000E+01
R = 0.10 L = 2 N = 12     ROOT = 3.95231954629818E+01
R = 0.10 L = 2 N = 13     ROOT = 4.2989142565984E+01
R = 0.10 L = 2 N = 14     ROOT = 4.6457000000000E+01
R = 0.10 L = 2 N = 15     ROOT = 4.9729615735317E+01
R = 0.10 L = 2 N = 16     ROOT = 5.3157834495228E+01
R = 0.10 L = 2 N = 17     ROOT = 5.6536000000000E+01
R = 0.10 L = 2 N = 18     ROOT = 6.0039532625171E+01
R = 0.10 L = 2 N = 19     ROOT = 6.3488031575398E+01
R = 0.10 L = 2 N = 20     ROOT = 6.6927000000000E+01
R = 0.10 L = 2 N = 21     ROOT = 7.0460324169932E+01
R = 0.10 L = 2 N = 22     ROOT = 7.3961741515426E+01
R = 0.10 L = 2 N = 23     ROOT = 7.7425981518328E+01
R = 0.10 L = 2 N = 24     ROOT = 8.0923238000000E+01
R = 0.10 L = 2 N = 25     ROOT = 8.4261425955207E+01
R = 0.10 L = 2 N = 26     ROOT = 8.7732323232610E+01
R = 0.10 L = 2 N = 27     ROOT = 9.1225232323232E+01
R = 0.10 L = 2 N = 28     ROOT = 9.4677898940368E+01
R = 0.10 L = 2 N = 29     ROOT = 9.8152884327634E+01
R = 0.10 L = 2 N = 30     ROOT = 1.0162600319443E+02

```

## ROOTS OF EQUATION 3

```

R * 0.10 L * 3 N * 1      ROOT = 4.5148968383698E+00
R * 0.10 L * 3 N * 2      ROOT = 0.5835985034545E+00
R * 0.10 L * 3 N * 3      ROOT = -1.1971287276635E+01
R * 0.10 L * 3 N * 4      ROOT = -2.0000000000000E+01
R * 0.10 L * 3 N * 5      ROOT = 1.8446342023918E+01
R * 0.10 L * 3 N * 6      ROOT = 2.1612789063213E+01
R * 0.10 L * 3 N * 7      ROOT = 2.4772488062632E+01
R * 0.10 L * 3 N * 8      ROOT = 2.7942818546597E+01
R * 0.10 L * 3 N * 9      ROOT = 3.0941276826329E+01
R * 0.10 L * 3 N * 10     ROOT = 3.3940466272752E+01
R * 0.10 L * 3 N * 11     ROOT = 3.7246731147078E+01
R * 0.10 L * 3 N * 12     ROOT = 4.0487246592725E+01
R * 0.10 L * 3 N * 13     ROOT = 4.3728085000000E+01
R * 0.10 L * 3 N * 14     ROOT = 4.7075294168089E+01
R * 0.10 L * 3 N * 15     ROOT = 5.0422522382044E+01
R * 0.10 L * 3 N * 16     ROOT = 5.3670000000000E+01
R * 0.10 L * 3 N * 17     ROOT = 5.7182378027755E+01
R * 0.10 L * 3 N * 18     ROOT = 6.0595115550427E+01
R * 0.10 L * 3 N * 19     ROOT = 6.4030000000000E+01
R * 0.10 L * 3 N * 20     ROOT = 6.7422748959987E+01
R * 0.10 L * 3 N * 21     ROOT = 7.0853792751395E+01
R * 0.10 L * 3 N * 22     ROOT = 7.4265000000000E+01
R * 0.10 L * 3 N * 23     ROOT = 7.7334595123100E+01
R * 0.10 L * 3 N * 24     ROOT = 8.1181294136835E+01
R * 0.10 L * 3 N * 25     ROOT = 8.4660000000000E+01
R * 0.10 L * 3 N * 26     ROOT = 8.8087226521100E+01
R * 0.10 L * 3 N * 27     ROOT = 9.1544867470099E+01
R * 0.10 L * 3 N * 28     ROOT = 9.5085113002951E+01
R * 0.10 L * 3 N * 29     ROOT = 9.8484386500000E+01
R * 0.10 L * 3 N * 30     ROOT = 1.0193228453639E+02

```

3

## ROOTS OF EQUATION 3

```

R * 0.10 L * 4 N * 1      ROOT = 5.6467035263953E+00
R * 0.10 L * 4 N * 2      ROOT = 9.8484386776593E+00
R * 0.10 L * 4 N * 3      ROOT = 1.1971287276635E+01
R * 0.10 L * 4 N * 4      ROOT = 1.6680751652189E+01
R * 0.10 L * 4 N * 5      ROOT = 1.9859857328892E+01
R * 0.10 L * 4 N * 6      ROOT = 2.387437859424E+01
R * 0.10 L * 4 N * 7      ROOT = 2.7883552000000E+01
R * 0.10 L * 4 N * 8      ROOT = 2.9420027506414E+01
R * 0.10 L * 4 N * 9      ROOT = 3.2556639762384E+01
R * 0.10 L * 4 N * 10     ROOT = 3.5600000000000E+01
R * 0.10 L * 4 N * 11     ROOT = 3.874864057056E+01
R * 0.10 L * 4 N * 12     ROOT = 4.185352464425E+01
R * 0.10 L * 4 N * 13     ROOT = 4.4950000000000E+01
R * 0.10 L * 4 N * 14     ROOT = 4.8181793862712E+01
R * 0.10 L * 4 N * 15     ROOT = 5.141753357229E+01
R * 0.10 L * 4 N * 16     ROOT = 5.4654000000000E+01
R * 0.10 L * 4 N * 17     ROOT = 5.8887143894141E+01
R * 0.10 L * 4 N * 18     ROOT = 6.134582368539E+01
R * 0.10 L * 4 N * 19     ROOT = 6.3980000000000E+01
R * 0.10 L * 4 N * 20     ROOT = 6.6983122095256E+01
R * 0.10 L * 4 N * 21     ROOT = 7.1474179361386E+01
R * 0.10 L * 4 N * 22     ROOT = 7.6080000000000E+01
R * 0.10 L * 4 N * 23     ROOT = 7.8288446145705E+01
R * 0.10 L * 4 N * 24     ROOT = 8.1788227793081E+01
R * 0.10 L * 4 N * 25     ROOT = 8.5380000000000E+01
R * 0.10 L * 4 N * 26     ROOT = 8.8567048277532E+01
R * 0.10 L * 4 N * 27     ROOT = 9.2084359525742E+01
R * 0.10 L * 4 N * 28     ROOT = 9.5480000000000E+01
R * 0.10 L * 4 N * 29     ROOT = 9.889158364592E+01
R * 0.10 L * 4 N * 30     ROOT = 1.023403811259E+02

```

4

```

ROOTS OF EQUATION 3
A + 0.10 L + 5 N + 1      ROOT = 6.756453279629E+00
A + 0.10 L + 5 N + 2      ROOT = 1.459845322695E+01
A + 0.10 L + 5 N + 3      ROOT = 4.59845322695E+01
A + 0.10 L + 5 N + 4      ROOT = 1.7947138112126E+01
A + 0.10 L + 5 N + 5      ROOT = 2.1239818512775E+01
A + 0.10 L + 5 N + 6      ROOT = 2.568787209159E+01
A + 0.10 L + 5 N + 7      ROOT = 2.769854981212E+01
A + 0.10 L + 5 N + 8      ROOT = 3.6897298692366E+01
A + 0.10 L + 5 N + 9      ROOT = 4.038787209159E+01
A + 0.10 L + 5 N + 10     ROOT = 3.72240214987E+01
A + 0.10 L + 5 N + 11     ROOT = 4.035957576846E+01
A + 0.10 L + 5 N + 12     ROOT = 4.038787209159E+01
A + 0.10 L + 5 N + 13     ROOT = 4.656175697188E+01
A + 0.10 L + 5 N + 14     ROOT = 4.966936989526E+01
A + 0.10 L + 5 N + 15     ROOT = 5.00000000000E+01
A + 0.10 L + 5 N + 16     ROOT = 5.39228053996661E+01
A + 0.10 L + 5 N + 17     ROOT = 5.9125598428519E+01
A + 0.10 L + 5 N + 18     ROOT = 6.25000000000E+01
A + 0.10 L + 5 N + 19     ROOT = 5.641153323397E+01
A + 0.10 L + 5 N + 20     ROOT = 6.8558709339787E+01
A + 0.10 L + 5 N + 21     ROOT = 7.00000000000E+01
A + 0.10 L + 5 N + 22     ROOT = 7.5634670232798E+01
A + 0.10 L + 5 N + 23     ROOT = 7.980246481038E+01
A + 0.10 L + 5 N + 24     ROOT = 8.23000000000E+01
A + 0.10 L + 5 N + 25     ROOT = 8.727479568259E+01
A + 0.10 L + 5 N + 26     ROOT = 8.9178717669519E+01
A + 0.10 L + 5 N + 27     ROOT = 8.9428619887186E+01
A + 0.10 L + 5 N + 28     ROOT = 9.428619887186E+01
A + 0.10 L + 5 N + 29     ROOT = 1.0265694328996E+02

```

5

```

ROOTS OF EQUATION 3
A + 0.10 L + 6 N + 1      ROOT = 7.8510776794204E+00
A + 0.10 L + 6 N + 2      ROOT = 1.2279333973215E+01
A + 0.10 L + 6 N + 3      ROOT = 1.9262701490169E+01
A + 0.10 L + 6 N + 4      ROOT = 1.9262701490169E+01
A + 0.10 L + 6 N + 5      ROOT = 2.257804185710E+01
A + 0.10 L + 6 N + 6      ROOT = 2.5984603182339E+01
A + 0.10 L + 6 N + 7      ROOT = 2.9984603182339E+01
A + 0.10 L + 6 N + 8      ROOT = 3.23013427631239E+01
A + 0.10 L + 6 N + 9      ROOT = 3.4691545242676E+01
A + 0.10 L + 6 N + 10     ROOT = 3.8631545242676E+01
A + 0.10 L + 6 N + 11     ROOT = 4.1866173633439E+01
A + 0.10 L + 6 N + 12     ROOT = 4.4665842232397E+01
A + 0.10 L + 6 N + 13     ROOT = 4.8162461861038E+01
A + 0.10 L + 6 N + 14     ROOT = 5.128639962295E+01
A + 0.10 L + 6 N + 15     ROOT = 5.439337793121E+01
A + 0.10 L + 6 N + 16     ROOT = 5.799163204935E+01
A + 0.10 L + 6 N + 17     ROOT = 6.0578738274055E+01
A + 0.10 L + 6 N + 18     ROOT = 6.376469378783625E+01
A + 0.10 L + 6 N + 19     ROOT = 7.0075343863933E+01
A + 0.10 L + 6 N + 20     ROOT = 7.3319784354394E+01
A + 0.10 L + 6 N + 21     ROOT = 7.665173633439E+01
A + 0.10 L + 6 N + 22     ROOT = 7.998163204935E+01
A + 0.10 L + 6 N + 23     ROOT = 8.3228642232397E+01
A + 0.10 L + 6 N + 24     ROOT = 8.6565842232397E+01
A + 0.10 L + 6 N + 25     ROOT = 8.9334723695493E+01
A + 0.10 L + 6 N + 26     ROOT = 8.9334723695493E+01
A + 0.10 L + 6 N + 27     ROOT = 9.3308177192987E+01
A + 0.10 L + 6 N + 28     ROOT = 9.3308177192987E+01
A + 0.10 L + 6 N + 29     ROOT = 1.08862599644945E+02
A + 0.10 L + 6 N + 30     ROOT = 1.0348754541389E+02

```

6

## 1 ROOTS OF EQUATION 3

```

A = 8.10 L = 7 N = 1      ROOT = 8.348388783516E+00
A = 8.10 L = 7 N = 2      ROOT = 1.3472830353837E+01
A = 8.10 L = 7 N = 3      ROOT = 1.455948086423E+01
A = 8.10 L = 7 N = 4      ROOT = 2.055948086423E+01
A = 8.10 L = 7 N = 5      ROOT = 2.398644867918E+01
A = 8.10 L = 7 N = 6      ROOT = 2.49813914629E+01
A = 8.10 L = 7 N = 7      ROOT = 3.04574249521E+01
A = 8.10 L = 7 N = 8      ROOT = 3.3692848358864E+01
A = 8.10 L = 7 N = 9      ROOT = 3.6969528796452E+01
A = 8.10 L = 7 N = 10     ROOT = 4.0248828796452E+01
A = 8.10 L = 7 N = 11     ROOT = 4.3387411245514E+01
A = 8.10 L = 7 N = 12     ROOT = 4.491835226194E+01
A = 8.10 L = 7 N = 13     ROOT = 4.591835226194E+01
A = 8.10 L = 7 N = 14     ROOT = 5.2825198985061E+01
A = 8.10 L = 7 N = 15     ROOT = 5.39785965895627E+01
A = 8.10 L = 7 N = 16     ROOT = 5.402785965895627E+01
A = 8.10 L = 7 N = 17     ROOT = 6.2287644532731E+01
A = 8.10 L = 7 N = 18     ROOT = 6.3382578217755E+01
A = 8.10 L = 7 N = 19     ROOT = 6.5002578217755E+01
A = 8.10 L = 7 N = 20     ROOT = 7.1581398128235E+01
A = 8.10 L = 7 N = 21     ROOT = 7.4641859866243E+01
A = 8.10 L = 7 N = 22     ROOT = 7.5000000000000E+01
A = 8.10 L = 7 N = 23     ROOT = 8.1029489501798E+01
A = 8.10 L = 7 N = 24     ROOT = 8.4277331982951E+01
A = 8.10 L = 7 N = 25     ROOT = 8.455948086423E+01
A = 8.10 L = 7 N = 26     ROOT = 9.0857540561072E+01
A = 8.10 L = 7 N = 27     ROOT = 9.4186579534508E+01
A = 8.10 L = 7 N = 28     ROOT = 9.4186579534508E+01
A = 8.10 L = 7 N = 29     ROOT = 9.8675316345482E+01
A = 8.10 L = 7 N = 30     ROOT = 1.0424207682566E+02

```

7

## 1 ROOTS OF EQUATION 3

```

A = 8.10 L = 8 N = 1      ROOT = 1.6818378746203E+01
A = 8.10 L = 8 N = 2      ROOT = 1.82563628893175E+01
A = 8.10 L = 8 N = 3      ROOT = 1.8356318341665E+01
A = 8.10 L = 8 N = 4      ROOT = 2.1848012871687E+01
A = 8.10 L = 8 N = 5      ROOT = 2.3036488202221E+01
A = 8.10 L = 8 N = 6      ROOT = 2.8536488202221E+01
A = 8.10 L = 8 N = 7      ROOT = 3.18151026395757E+01
A = 8.10 L = 8 N = 8      ROOT = 3.42388672084743E+01
A = 8.10 L = 8 N = 9      ROOT = 4.1516299835125E+01
A = 8.10 L = 8 N = 10     ROOT = 4.4234637625172E+01
A = 8.10 L = 8 N = 11     ROOT = 5.791889807765E+01
A = 8.10 L = 8 N = 12     ROOT = 5.1167415647409E+01
A = 8.10 L = 8 N = 13     ROOT = 5.1167415647409E+01
A = 8.10 L = 8 N = 14     ROOT = 5.7468527881309E+01
A = 8.10 L = 8 N = 15     ROOT = 6.0623168674213E+01
A = 8.10 L = 8 N = 16     ROOT = 6.32765481363E+01
A = 8.10 L = 8 N = 17     ROOT = 6.5981333841363E+01
A = 8.10 L = 8 N = 18     ROOT = 7.0825333842598E+01
A = 8.10 L = 8 N = 19     ROOT = 7.3126781391389E+01
A = 8.10 L = 8 N = 20     ROOT = 7.4000000000000E+01
A = 8.10 L = 8 N = 21     ROOT = 7.3316779458464E+01
A = 8.10 L = 8 N = 22     ROOT = 8.2434637625172E+01
A = 8.10 L = 8 N = 23     ROOT = 8.2434637625172E+01
A = 8.10 L = 8 N = 24     ROOT = 8.6767017133521E+01
A = 8.10 L = 8 N = 25     ROOT = 8.6767017133521E+01
A = 8.10 L = 8 N = 26     ROOT = 9.1966730443087E+01
A = 8.10 L = 8 N = 27     ROOT = 9.1966730443087E+01
A = 8.10 L = 8 N = 28     ROOT = 9.8516145366164E+01
A = 8.10 L = 8 N = 29     ROOT = 1.0181708313396E+02
A = 8.10 L = 8 N = 30     ROOT = 1.051368398769E+02

```

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8

## 1 ROOTS OF EQUATION 3

```

A * 0.10 L * 9 N * 1      ROOT = 1.1879418389950E+01
A * 0.10 L * 9 N * 2      ROOT = 1.5815215488934E+01
A * 0.10 L * 9 N * 3      ROOT = 2.10856842814E+01
A * 0.10 L * 9 N * 4      ROOT = 2.319658642814E+01
A * 0.10 L * 9 N * 5      ROOT = 2.6516682554113E+01
A * 0.10 L * 9 N * 6      ROOT = 2.8516682554113E+01
A * 0.10 L * 9 N * 7      ROOT = 3.158753793303E+01
A * 0.10 L * 9 N * 8      ROOT = 3.6427717184023E+01
A * 0.10 L * 9 N * 9      ROOT = 3.958753793303E+01
A * 0.10 L * 9 N * 10     ROOT = 4.0994912628893E+01
A * 0.10 L * 9 N * 11     ROOT = 4.6122298118903E+01
A * 0.10 L * 9 N * 12     ROOT = 4.9368959599870E+01
A * 0.10 L * 9 N * 13     ROOT = 4.9328918302940E+01
A * 0.10 L * 9 N * 14     ROOT = 5.5719659863439E+01
A * 0.10 L * 9 N * 15     ROOT = 6.8980696142757E+01
A * 0.10 L * 9 N * 16     ROOT = 6.9936269110000E+01
A * 0.10 L * 9 N * 17     ROOT = 6.5255762690154E+01
A * 0.10 L * 9 N * 18     ROOT = 6.8419744313573E+01
A * 0.10 L * 9 N * 19     ROOT = 7.0000000000000E+01
A * 0.10 L * 9 N * 20     ROOT = 7.4714276223772E+01
A * 0.10 L * 9 N * 21     ROOT = 7.853959599870E+01
A * 0.10 L * 9 N * 22     ROOT = 8.0000000000000E+01
A * 0.10 L * 9 N * 23     ROOT = 8.4045516895303E+01
A * 0.10 L * 9 N * 24     ROOT = 8.7138964714529E+01
A * 0.10 L * 9 N * 25     ROOT = 8.8000000000000E+01
A * 0.10 L * 9 N * 26     ROOT = 9.33596353686020E+01
A * 0.10 L * 9 N * 27     ROOT = 9.6528351345401E+01
A * 0.10 L * 9 N * 28     ROOT = 1.0000000000000E+02
A * 0.10 L * 9 N * 29     ROOT = 1.0294659377687E+02
A * 0.10 L * 9 N * 30     ROOT = 1.9620071914651E+02

```

9

## 1 ROOTS OF EQUATION 3

```

A * 0.10 L * 10 N * 1      ROOT = 1.2143204108943E+01
A * 0.10 L * 10 N * 2      ROOT = 1.6977549986165E+01
A * 0.10 L * 10 N * 3      ROOT = 2.1085682554113E+01
A * 0.10 L * 10 N * 4      ROOT = 2.319658642814E+01
A * 0.10 L * 10 N * 5      ROOT = 2.7801885334662E+01
A * 0.10 L * 10 N * 6      ROOT = 2.8516682554113E+01
A * 0.10 L * 10 N * 7      ROOT = 3.448979442374E+01
A * 0.10 L * 10 N * 8      ROOT = 3.7776267283676E+01
A * 0.10 L * 10 N * 9      ROOT = 4.0000000000000E+01
A * 0.10 L * 10 N * 10     ROOT = 4.4291547365987E+01
A * 0.10 L * 10 N * 11     ROOT = 4.7510414572429E+01
A * 0.10 L * 10 N * 12     ROOT = 4.9368959599870E+01
A * 0.10 L * 10 N * 13     ROOT = 4.9357477036000E+01
A * 0.10 L * 10 N * 14     ROOT = 5.7136091395220E+01
A * 0.10 L * 10 N * 15     ROOT = 6.8277711652113E+01
A * 0.10 L * 10 N * 16     ROOT = 6.7800456149360E+01
A * 0.10 L * 10 N * 17     ROOT = 6.3878813362738E+01
A * 0.10 L * 10 N * 18     ROOT = 6.3878813362738E+01
A * 0.10 L * 10 N * 19     ROOT = 7.6215146313537E+01
A * 0.10 L * 10 N * 20     ROOT = 7.9371898786001E+01
A * 0.10 L * 10 N * 21     ROOT = 8.0000000000000E+01
A * 0.10 L * 10 N * 22     ROOT = 8.5658263176401E+01
A * 0.10 L * 10 N * 23     ROOT = 8.8676199716989E+01
A * 0.10 L * 10 N * 24     ROOT = 8.8676199716989E+01
A * 0.10 L * 10 N * 25     ROOT = 9.4986319793486E+01
A * 0.10 L * 10 N * 26     ROOT = 9.8861762634973E+01
A * 0.10 L * 10 N * 27     ROOT = 9.8861762634973E+01
A * 0.10 L * 10 N * 28     ROOT = 1.04305953959586E+02
A * 0.10 L * 10 N * 29     ROOT = 1.0747708465753E+02

```

10

```

1 ROOTS OF EQUATION 3
R * 0.10 L * 11 N * 1      P00T * -1.32026289396828E+01
R * 0.10 L * 11 N * 2      P00T * 1.8127564101891E+01
R * 0.10 L * 11 N * 3      P00T * 2.4592559717429E+01
R * 0.10 L * 11 N * 4      P00T * 2.569487717429E+01
R * 0.10 L * 11 N * 5      P00T * 2.9075816903035E+01
R * 0.10 L * 11 N * 6      P00T * 3.143886134589E+01
R * 0.10 L * 11 N * 7      P00T * 3.5809325936480E+01
R * 0.10 L * 11 N * 8      P00T * 3.911343921369E+01
R * 0.10 L * 11 N * 9      P00T * 4.23908541428E+01
R * 0.10 L * 11 N * 10     P00T * 4.20751394280E+01
R * 0.10 L * 11 N * 11     P00T * 4.8867782945764E+01
R * 0.10 L * 11 N * 12     P00T * 5.211329319651E+01
R * 0.10 L * 11 N * 13     P00T * 5.444182815607E+01
R * 0.10 L * 11 N * 14     P00T * 5.8541581580762E+01
R * 0.10 L * 11 N * 15     P00T * 6.1743102527936E+01
R * 0.10 L * 11 N * 16     P00T * 6.48526121010E+01
R * 0.10 L * 11 N * 17     P00T * 6.8128591053054E+01
R * 0.10 L * 11 N * 18     P00T * 7.1313955340543E+01
R * 0.10 L * 11 N * 19     P00T * 7.4339384015322E+01
R * 0.10 L * 11 N * 20     P00T * 7.6714978681617E+01
R * 0.10 L * 11 N * 21     P00T * 8.0843331623420E+01
R * 0.10 L * 11 N * 22     P00T * 8.4052331623420E+01
R * 0.10 L * 11 N * 23     P00T * 8.78774547359E+01
R * 0.10 L * 11 N * 24     P00T * 9.031825782659E+01
R * 0.10 L * 11 N * 25     P00T * 9.2082626121010E+01
R * 0.10 L * 11 N * 26     P00T * 9.4693339692315E+01
R * 0.10 L * 11 N * 27     P00T * 1.00023513225E+02
R * 0.10 L * 11 N * 28     P00T * 1.05136047245E+02
R * 0.10 L * 11 N * 30     P00T * 1.0838905381907E+02

```

11

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1 ROOTS OF EQUATION 3
R * 0.10 L * 12 N * 1      P00T * 1.42287348913425E+01
R * 0.10 L * 12 N * 2      P00T * 1.5270293740244E+01
R * 0.10 L * 12 N * 3      P00T * 2.3194596197805E+01
R * 0.10 L * 12 N * 4      P00T * 2.4592559717429E+01
R * 0.10 L * 12 N * 5      P00T * 2.5339384015322E+01
R * 0.10 L * 12 N * 6      P00T * 3.1375826015082E+01
R * 0.10 L * 12 N * 7      P00T * 3.711843042048E+01
R * 0.10 L * 12 N * 8      P00T * 4.2858081580762E+01
R * 0.10 L * 12 N * 9      P00T * 4.3732713520147E+01
R * 0.10 L * 12 N * 10     P00T * 4.7082744426854E+01
R * 0.10 L * 12 N * 11     P00T * 5.0000000000000E+01
R * 0.10 L * 12 N * 12     P00T * 5.3493514855112E+01
R * 0.10 L * 12 N * 13     P00T * 5.6220553550246E+01
R * 0.10 L * 12 N * 14     P00T * 5.8639339692315E+01
R * 0.10 L * 12 N * 15     P00T * 6.3147036149854E+01
R * 0.10 L * 12 N * 16     P00T * 6.6349635356717E+01
R * 0.10 L * 12 N * 17     P00T * 6.9200000000000E+01
R * 0.10 L * 12 N * 18     P00T * 7.2738228117383E+01
R * 0.10 L * 12 N * 19     P00T * 7.552580646255E+01
R * 0.10 L * 12 N * 20     P00T * 7.83131434177E+01
R * 0.10 L * 12 N * 21     P00T * 8.2268957303015E+01
R * 0.10 L * 12 N * 22     P00T * 8.5464331434177E+01
R * 0.10 L * 12 N * 23     P00T * 8.8683176161612E+01
R * 0.10 L * 12 N * 24     P00T * 9.1803176161612E+01
R * 0.10 L * 12 N * 25     P00T * 9.4964368025824E+01
R * 0.10 L * 12 N * 26     P00T * 9.8126191642042E+01
R * 0.10 L * 12 N * 27     P00T * 1.0126191642042E+02
R * 0.10 L * 12 N * 28     P00T * 1.0439395611188E+02
R * 0.10 L * 12 N * 29     P00T * 1.08128132535E+02
R * 0.10 L * 12 N * 30     P00T * 1.10617239474E+02

```

12

## 1 ROOTS OF EQUATION 3

```

R + 8.18 L + 13 N + 1      ROOT = 1.5316687393719E+01
R + 8.18 L + 13 N + 2      ROOT = 2.157126536219E+01
R + 8.18 L + 13 N + 3      ROOT = 2.4392837523169E+01
R + 8.18 L + 13 N + 4      ROOT = 2.8862136576737E+01
R + 8.18 L + 13 N + 5      ROOT = 3.0000000000000E+01
R + 8.18 L + 13 N + 6      ROOT = 3.5835981842492E+01
R + 8.18 L + 13 N + 7      ROOT = 3.8417958326127E+01
R + 8.18 L + 13 N + 8      ROOT = 4.0000000000000E+01
R + 8.18 L + 13 N + 9      ROOT = 4.2665266504368E+01
R + 8.18 L + 13 N + 10     ROOT = 4.8348628919338E+01
R + 8.18 L + 13 N + 11     ROOT = 5.1812525971438E+01
R + 8.18 L + 13 N + 12     ROOT = 5.89586863645846E+01
R + 8.18 L + 13 N + 13     ROOT = 6.1326533000232E+01
R + 8.18 L + 13 N + 14     ROOT = 6.4220295945231E+01
R + 8.18 L + 13 N + 15     ROOT = 6.7752198566525E+01
R + 8.18 L + 13 N + 16     ROOT = 7.0000000000000E+01
R + 8.18 L + 13 N + 17     ROOT = 7.4137773436115E+01
R + 8.18 L + 13 N + 18     ROOT = 7.7347804461195E+01
R + 8.18 L + 13 N + 19     ROOT = 8.0000000000000E+01
R + 8.18 L + 13 N + 20     ROOT = 8.2722018962335E+01
R + 8.18 L + 13 N + 21     ROOT = 8.6982961398408E+01
R + 8.18 L + 13 N + 22     ROOT = 9.0881439258463E+01
R + 8.18 L + 13 N + 23     ROOT = 9.4000000000000E+01
R + 8.18 L + 13 N + 24     ROOT = 9.6428390198550E+01
R + 8.18 L + 13 N + 25     ROOT = 9.9596112492255E+01
R + 8.18 L + 13 N + 26     ROOT = 1.0000000000000E+02
R + 8.18 L + 13 N + 27     ROOT = 1.059136069687E+02
R + 8.18 L + 13 N + 28     ROOT = 1.0966164311469E+02
R + 8.18 L + 13 N + 30     ROOT = 1.1226139856873E+02

```

13

## ROOTS OF EQUATION 3

```

R + 8.18 L + 14 N + 1      ROOT = 1.6368623746487E+01
R + 8.18 L + 14 N + 2      ROOT = 2.157126536219E+01
R + 8.18 L + 14 N + 3      ROOT = 2.556183317037E+01
R + 8.18 L + 14 N + 4      ROOT = 2.9278739849054E+01
R + 8.18 L + 14 N + 5      ROOT = 3.0000000000000E+01
R + 8.18 L + 14 N + 6      ROOT = 3.636592794335E+01
R + 8.18 L + 14 N + 7      ROOT = 3.97685506287932E+01
R + 8.18 L + 14 N + 8      ROOT = 4.3000000000000E+01
R + 8.18 L + 14 N + 9      ROOT = 4.6389839468442E+01
R + 8.18 L + 14 N + 10     ROOT = 4.9686194572224E+01
R + 8.18 L + 14 N + 11     ROOT = 5.2000000000000E+01
R + 8.18 L + 14 N + 12     ROOT = 5.6222600050893E+01
R + 8.18 L + 14 N + 13     ROOT = 5.9468920618573E+01
R + 8.18 L + 14 N + 14     ROOT = 6.2000000000000E+01
R + 8.18 L + 14 N + 15     ROOT = 6.592377157640E+01
R + 8.18 L + 14 N + 16     ROOT = 6.914673216545E+01
R + 8.18 L + 14 N + 17     ROOT = 7.2561581647935E+01
R + 8.18 L + 14 N + 18     ROOT = 7.6768621971929E+01
R + 8.18 L + 14 N + 19     ROOT = 8.0952618261934E+01
R + 8.18 L + 14 N + 20     ROOT = 8.413352618291E+01
R + 8.18 L + 14 N + 21     ROOT = 8.8332340921889E+01
R + 8.18 L + 14 N + 22     ROOT = 9.151583961889E+01
R + 8.18 L + 14 N + 23     ROOT = 9.477277298080E+01
R + 8.18 L + 14 N + 24     ROOT = 9.7873852832144E+01
R + 8.18 L + 14 N + 25     ROOT = 1.018562922694E+02
R + 8.18 L + 14 N + 26     ROOT = 1.052852978840E+02
R + 8.18 L + 14 N + 27     ROOT = 1.0838849585674E+02
R + 8.18 L + 14 N + 28     ROOT = 1.1055235677739E+02
R + 8.18 L + 14 N + 30     ROOT = 1.1371130901626E+02

```

14

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1 ROOTS OF EQUATION 3
A = 0.10 L = 15 N = 1      ROOT = 1.7498833803807E+01
A = 0.10 L = 15 N = 2      ROOT = 2.2662493433694E+01
A = 0.10 L = 15 N = 3      ROOT = 2.7826880194715E+01
A = 0.10 L = 15 N = 4      ROOT = 3.46488081947915E+01
A = 0.10 L = 15 N = 5      ROOT = 3.4877867704482E+01
A = 0.10 L = 15 N = 6      ROOT = 3.4988527678175E+01
A = 0.10 L = 15 N = 7      ROOT = 4.6958527678175E+01
A = 0.10 L = 15 N = 8      ROOT = 4.4365571824680E+01
A = 0.10 L = 15 N = 9      ROOT = 4.4365571824680E+01
A = 0.10 L = 15 N = 10     ROOT = 5.1815137766332E+01
A = 0.10 L = 15 N = 11     ROOT = 5.4383875982655E+01
A = 0.10 L = 15 N = 12     ROOT = 5.4383875982655E+01
A = 0.10 L = 15 N = 13     ROOT = 6.081965324318E+01
A = 0.10 L = 15 N = 14     ROOT = 6.4075020466804E+01
A = 0.10 L = 15 N = 15     ROOT = 6.7368139379156E+01
A = 0.10 L = 15 N = 16     ROOT = 6.7368139379156E+01
A = 0.10 L = 15 N = 17     ROOT = 7.3751836007535E+01
A = 0.10 L = 15 N = 18     ROOT = 7.6961867677528E+01
A = 0.10 L = 15 N = 19     ROOT = 8.0178866666667E+01
A = 0.10 L = 15 N = 20     ROOT = 8.3367879464745E+01
A = 0.10 L = 15 N = 21     ROOT = 8.4562734384448E+01
A = 0.10 L = 15 N = 22     ROOT = 8.4562734384448E+01
A = 0.10 L = 15 N = 23     ROOT = 9.2942612203897E+01
A = 0.10 L = 15 N = 24     ROOT = 9.6127596892893E+01
A = 0.10 L = 15 N = 25     ROOT = 9.6127596892893E+01
A = 0.10 L = 15 N = 26     ROOT = 1.024896222185E+02
A = 0.10 L = 15 N = 27     ROOT = 1.056588895635E+02
A = 0.10 L = 15 N = 28     ROOT = 1.056588895635E+02
A = 0.10 L = 15 N = 29     ROOT = 1.1201116535559E+02
A = 0.10 L = 15 N = 30     ROOT = 1.1518842507804E+02

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15

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1 ROOTS OF EQUATION 3
A = 0.20 L = 1 N = 1      ROOT = 2.0564616363988E+00
A = 0.20 L = 1 N = 2      ROOT = 5.795774217535E+00
A = 0.20 L = 1 N = 3      ROOT = 9.1869959389746E+00
A = 0.20 L = 1 N = 4      ROOT = 1.2651128654798E+01
A = 0.20 L = 1 N = 5      ROOT = 1.4154342549586E+01
A = 0.20 L = 1 N = 6      ROOT = 2.0154342549586E+01
A = 0.20 L = 1 N = 7      ROOT = 2.3952867524088E+01
A = 0.20 L = 1 N = 8      ROOT = 3.17372776693547E+01
A = 0.20 L = 1 N = 9      ROOT = 3.5628953817271E+01
A = 0.20 L = 1 N = 10     ROOT = 3.5628953817271E+01
A = 0.20 L = 1 N = 11     ROOT = 4.3429638266590E+01
A = 0.20 L = 1 N = 12     ROOT = 4.7337962416095E+01
A = 0.20 L = 1 N = 13     ROOT = 5.1228762416095E+01
A = 0.20 L = 1 N = 14     ROOT = 5.5160379972943E+01
A = 0.20 L = 1 N = 15     ROOT = 5.9875131683948E+01
A = 0.20 L = 1 N = 16     ROOT = 6.453881398448E+01
A = 0.20 L = 1 N = 17     ROOT = 6.5968353899116E+01
A = 0.20 L = 1 N = 18     ROOT = 7.6827600724224E+01
A = 0.20 L = 1 N = 19     ROOT = 7.8667356292613E+01
A = 0.20 L = 1 N = 20     ROOT = 7.8667356292613E+01
A = 0.20 L = 1 N = 21     ROOT = 8.2588245987209E+01
A = 0.20 L = 1 N = 22     ROOT = 8.2588245987209E+01
A = 0.20 L = 1 N = 23     ROOT = 9.6431647854632E+01
A = 0.20 L = 1 N = 24     ROOT = 9.43540808637965E+01
A = 0.20 L = 1 N = 25     ROOT = 9.43540808637965E+01
A = 0.20 L = 1 N = 26     ROOT = 9.8215988183287E+01
A = 0.20 L = 1 N = 27     ROOT = 1.0213988183287E+02
A = 0.20 L = 1 N = 28     ROOT = 1.0612315453355E+02
A = 0.20 L = 1 N = 29     ROOT = 1.1884676001730E+02
A = 0.20 L = 1 N = 30     ROOT = 1.1397601480393E+02

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16

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ROOTS OF EQUATION 3
A = 0.20 L = 2 N = 1      ROOT = 3.232780713998E+00
A = 0.20 L = 2 N = 2      ROOT = 1.040796315702E+01
A = 0.20 L = 2 N = 3      ROOT = 2.088442763131E+01
A = 0.20 L = 2 N = 4      ROOT = 1.7088442763131E+01
A = 0.20 L = 2 N = 5      ROOT = 2.0711741985192E+01
A = 0.20 L = 2 N = 6      ROOT = 2.8239122801772E+01
A = 0.20 L = 2 N = 7      ROOT = 2.8239122801772E+01
A = 0.20 L = 2 N = 8      ROOT = 3.2067907633112E+01
A = 0.20 L = 2 N = 9      ROOT = 3.5913750000000E+01
A = 0.20 L = 2 N = 10     ROOT = 3.16431653E+01
A = 0.20 L = 2 N = 11     ROOT = 4.3656845049668E+01
A = 0.20 L = 2 N = 12     ROOT = 4.755388159522E+01
A = 0.20 L = 2 N = 13     ROOT = 4.755388159522E+01
A = 0.20 L = 2 N = 14     ROOT = 5.924639708173E+01
A = 0.20 L = 2 N = 15     ROOT = 5.924639708173E+01
A = 0.20 L = 2 N = 16     ROOT = 5.924639708173E+01
A = 0.20 L = 2 N = 17     ROOT = 6.01804133733E+01
A = 0.20 L = 2 N = 18     ROOT = 6.766004133733E+01
A = 0.20 L = 2 N = 19     ROOT = 7.057013430397E+01
A = 0.20 L = 2 N = 20     ROOT = 7.057013430397E+01
A = 0.20 L = 2 N = 21     ROOT = 7.8795453539313E+01
A = 0.20 L = 2 N = 22     ROOT = 8.271018344146E+01
A = 0.20 L = 2 N = 23     ROOT = 8.271018344146E+01
A = 0.20 L = 2 N = 24     ROOT = 9.0542871978715E+01
A = 0.20 L = 2 N = 25     ROOT = 9.446055342146E+01
A = 0.20 L = 2 N = 26     ROOT = 9.446055342146E+01
A = 0.20 L = 2 N = 27     ROOT = 1.021909423310E+02
A = 0.20 L = 2 N = 28     ROOT = 1.062177819216E+02
A = 0.20 L = 2 N = 29     ROOT = 1.101375344638E+02
A = 0.20 L = 2 N = 30     ROOT = 1.14079877145011E+02

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17

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ROOTS OF EQUATION 3
A = 0.20 L = 3 N = 1      ROOT = 4.5136764203096E+00
A = 0.20 L = 3 N = 2      ROOT = 1.5685259389504E+00
A = 0.20 L = 3 N = 3      ROOT = 1.187319518408E+01
A = 0.20 L = 3 N = 4      ROOT = 1.818712338914E+01
A = 0.20 L = 3 N = 5      ROOT = 2.157423795671E+01
A = 0.20 L = 3 N = 6      ROOT = 2.882047476156E+01
A = 0.20 L = 3 N = 7      ROOT = 3.25683176966124E+01
A = 0.20 L = 3 N = 8      ROOT = 3.882047476156E+01
A = 0.20 L = 3 N = 9      ROOT = 4.0180115811025E+01
A = 0.20 L = 3 N = 10     ROOT = 4.4021186503323E+01
A = 0.20 L = 3 N = 11     ROOT = 4.7831613160332E+01
A = 0.20 L = 3 N = 12     ROOT = 5.1444165693933E+01
A = 0.20 L = 3 N = 13     ROOT = 5.5621124420046E+01
A = 0.20 L = 3 N = 14     ROOT = 5.959379467552E+01
A = 0.20 L = 3 N = 15     ROOT = 6.338379467552E+01
A = 0.20 L = 3 N = 16     ROOT = 6.728676766513E+01
A = 0.20 L = 3 N = 17     ROOT = 7.1184046102843E+01
A = 0.20 L = 3 N = 18     ROOT = 7.598767011874E+01
A = 0.20 L = 3 N = 19     ROOT = 7.898767011874E+01
A = 0.20 L = 3 N = 20     ROOT = 8.2893133608833E+01
A = 0.20 L = 3 N = 21     ROOT = 8.5893133608833E+01
A = 0.20 L = 3 N = 22     ROOT = 9.0709472948672E+01
A = 0.20 L = 3 N = 23     ROOT = 9.0709472948672E+01
A = 0.20 L = 3 N = 24     ROOT = 9.4620416074816E+01
A = 0.20 L = 3 N = 25     ROOT = 9.4620416074816E+01
A = 0.20 L = 3 N = 26     ROOT = 1.0244555666729E+02
A = 0.20 L = 3 N = 27     ROOT = 1.0535974332142E+02
A = 0.20 L = 3 N = 28     ROOT = 1.101375344638E+02
A = 0.20 L = 3 N = 29     ROOT = 1.141987660321E+02

```

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## 1 ROOTS OF EQUATION 3

```

A = 0.20 L = 4 N = 1      ROOT = 5.6466683460851E+00
A = 0.20 L = 4 N = 2      ROOT = 9.8379812118479E+00
A = 0.20 L = 4 N = 3      ROOT = 1.4595909627462E+01
A = 0.20 L = 4 N = 4      ROOT = 1.6495909627462E+01
A = 0.20 L = 4 N = 5      ROOT = 1.96878713798984E+01
A = 0.20 L = 4 N = 6      ROOT = 2.16878713798984E+01
A = 0.20 L = 4 N = 7      ROOT = 2.6182894891618E+01
A = 0.20 L = 4 N = 8      ROOT = 2.9615644627460E+01
A = 0.20 L = 4 N = 9      ROOT = 3.26514627460E+01
A = 0.20 L = 4 N = 10     ROOT = 3.6593267575275E+01
A = 0.20 L = 4 N = 11     ROOT = 4.0797573292255E+01
A = 0.20 L = 4 N = 12     ROOT = 4.4897573292255E+01
A = 0.20 L = 4 N = 13     ROOT = 4.8311472116864E+01
A = 0.20 L = 4 N = 14     ROOT = 5.2143977065492E+01
A = 0.20 L = 4 N = 15     ROOT = 5.59585788224E+01
A = 0.20 L = 4 N = 16     ROOT = 5.97585788224E+01
A = 0.20 L = 4 N = 17     ROOT = 6.3715286321669E+01
A = 0.20 L = 4 N = 18     ROOT = 6.7569375966813E+01
A = 0.20 L = 4 N = 19     ROOT = 7.144667657139E+01
A = 0.20 L = 4 N = 20     ROOT = 7.535467657139E+01
A = 0.20 L = 4 N = 21     ROOT = 7.9244106156207E+01
A = 0.20 L = 4 N = 22     ROOT = 8.313339175768E+01
A = 0.20 L = 4 N = 23     ROOT = 8.703339175768E+01
A = 0.20 L = 4 N = 24     ROOT = 9.09323280765913E+01
A = 0.20 L = 4 N = 25     ROOT = 9.48323280765913E+01
A = 0.20 L = 4 N = 26     ROOT = 9.8737005767008E+01
A = 0.20 L = 4 N = 27     ROOT = 1.0264222133034E+02
A = 0.20 L = 4 N = 28     ROOT = 1.0754222133034E+02
A = 0.20 L = 4 N = 29     ROOT = 1.10457653945794E+02
A = 0.20 L = 4 N = 30     ROOT = 1.1346696202748E+02

```

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## 1 ROOTS OF EQUATION 3

```

A = 0.20 L = 5 N = 1      ROOT = 6.7564521721165E+00
A = 0.20 L = 5 N = 2      ROOT = 1.1865910696593E+01
A = 0.20 L = 5 N = 3      ROOT = 1.7713455836455E+01
A = 0.20 L = 5 N = 4      ROOT = 2.1110238271385E+01
A = 0.20 L = 5 N = 5      ROOT = 2.4514951651252E+01
A = 0.20 L = 5 N = 6      ROOT = 2.734994951651252E+01
A = 0.20 L = 5 N = 7      ROOT = 3.0650435286085E+01
A = 0.20 L = 5 N = 8      ROOT = 3.376954876795138E+01
A = 0.20 L = 5 N = 9      ROOT = 3.77684951651252E+01
A = 0.20 L = 5 N = 10     ROOT = 4.176136467382E+01
A = 0.20 L = 5 N = 11     ROOT = 4.576136467382E+01
A = 0.20 L = 5 N = 12     ROOT = 4.98574326295137E+01
A = 0.20 L = 5 N = 13     ROOT = 5.3954879961928E+01
A = 0.20 L = 5 N = 14     ROOT = 5.76454879961928E+01
A = 0.20 L = 5 N = 15     ROOT = 6.13454879961928E+01
A = 0.20 L = 5 N = 16     ROOT = 6.411856746798E+01
A = 0.20 L = 5 N = 17     ROOT = 6.796826746798E+01
A = 0.20 L = 5 N = 18     ROOT = 7.177826746798E+01
A = 0.20 L = 5 N = 19     ROOT = 7.5692708729513E+01
A = 0.20 L = 5 N = 20     ROOT = 7.956492146396E+01
A = 0.20 L = 5 N = 21     ROOT = 8.34376492146396E+01
A = 0.20 L = 5 N = 22     ROOT = 8.732459884969E+01
A = 0.20 L = 5 N = 23     ROOT = 9.1210698754735E+01
A = 0.20 L = 5 N = 24     ROOT = 9.5098458754735E+01
A = 0.20 L = 5 N = 25     ROOT = 9.8992897631646E+01
A = 0.20 L = 5 N = 26     ROOT = 1.0288813731967E+02
A = 0.20 L = 5 N = 27     ROOT = 1.068556649292E+02
A = 0.20 L = 5 N = 28     ROOT = 1.1068556649292E+02
A = 0.20 L = 5 N = 29     ROOT = 1.1456723599435E+02

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```

1 ROOTS OF EQUATION 3
R = 0.20 L = 6 N = 1      P00T = 7.8518772059495E+00
R = 0.20 L = 6 N = 2      P00T = 1.22732908077467E+01
R = 0.20 L = 6 N = 3      P00T = 1.5862215864577E+01
R = 0.20 L = 6 N = 4      P00T = 1.8451112561454E+01
R = 0.20 L = 6 N = 5      P00T = 2.25381314237375E+01
R = 0.20 L = 6 N = 6      P00T = 2.5718794281768E+01
R = 0.20 L = 6 N = 7      P00T = 2.8900000000000E+01
R = 0.20 L = 6 N = 8      P00T = 3.1941923915440E+01
R = 0.20 L = 6 N = 9      P00T = 3.5212672944320E+01
R = 0.20 L = 6 N = 10     P00T = 3.8443800000000E+01
R = 0.20 L = 6 N = 11     P00T = 4.1674956547760E+01
R = 0.20 L = 6 N = 12     P00T = 4.5828442989332E+01
R = 0.20 L = 6 N = 13     P00T = 4.9960000000000E+01
R = 0.20 L = 6 N = 14     P00T = 5.3200871498252E+01
R = 0.20 L = 6 N = 15     P00T = 5.7012956194989E+01
R = 0.20 L = 6 N = 16     P00T = 6.082391326261E+01
R = 0.20 L = 6 N = 17     P00T = 6.468186320000E+01
R = 0.20 L = 6 N = 18     P00T = 6.8433846590552E+01
R = 0.20 L = 6 N = 19     P00T = 7.2256234295301E+01
R = 0.20 L = 6 N = 20     P00T = 7.6078520000000E+01
R = 0.20 L = 6 N = 21     P00T = 7.9895036558710E+01
R = 0.20 L = 6 N = 22     P00T = 8.3809176523632E+01
R = 0.20 L = 6 N = 23     P00T = 8.7621200000000E+01
R = 0.20 L = 6 N = 24     P00T = 9.1544985602562E+01
R = 0.20 L = 6 N = 25     P00T = 9.5428419865439E+01
R = 0.20 L = 6 N = 26     P00T = 9.9250000000000E+01
R = 0.20 L = 6 N = 27     P00T = 1.0318337634485E+02
R = 0.20 L = 6 N = 28     P00T = 1.0706393831403E+02
R = 0.20 L = 6 N = 29     P00T = 1.1055951697250E+02
R = 0.20 L = 6 N = 30     P00T = 1.135154520963E+02

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1 ROOTS OF EQUATION 3
R = 0.20 L = 7 N = 1      P00T = 8.3348388439976E+00
R = 0.20 L = 7 N = 2      P00T = 1.3472043517283E+01
R = 0.20 L = 7 N = 3      P00T = 1.7083333333333E+01
R = 0.20 L = 7 N = 4      P00T = 2.0557609480567E+01
R = 0.20 L = 7 N = 5      P00T = 2.3895709551644E+01
R = 0.20 L = 7 N = 6      P00T = 2.7233750000000E+01
R = 0.20 L = 7 N = 7      P00T = 3.0326571623634E+01
R = 0.20 L = 7 N = 8      P00T = 3.3423647647077E+01
R = 0.20 L = 7 N = 9      P00T = 3.6520544666667E+01
R = 0.20 L = 7 N = 10     P00T = 3.9617334986333E+01
R = 0.20 L = 7 N = 11     P00T = 4.18122717540177E+01
R = 0.20 L = 7 N = 12     P00T = 4.6105583593542E+01
R = 0.20 L = 7 N = 13     P00T = 5.0398800000000E+01
R = 0.20 L = 7 N = 14     P00T = 5.3964630033398E+01
R = 0.20 L = 7 N = 15     P00T = 5.7678015602343E+01
R = 0.20 L = 7 N = 16     P00T = 6.1391200000000E+01
R = 0.20 L = 7 N = 17     P00T = 6.5172495209014E+01
R = 0.20 L = 7 N = 18     P00T = 6.8957166524806E+01
R = 0.20 L = 7 N = 19     P00T = 7.2734444444444E+01
R = 0.20 L = 7 N = 20     P00T = 7.6573865524968E+01
R = 0.20 L = 7 N = 21     P00T = 8.04040810277059E+01
R = 0.20 L = 7 N = 22     P00T = 8.4131333333333E+01
R = 0.20 L = 7 N = 23     P00T = 8.8862838457849E+01
R = 0.20 L = 7 N = 24     P00T = 9.1953572864846E+01
R = 0.20 L = 7 N = 25     P00T = 9.5125000000000E+01
R = 0.20 L = 7 N = 26     P00T = 9.8658690336454E+01
R = 0.20 L = 7 N = 27     P00T = 1.0352804049984E+02
R = 0.20 L = 7 N = 28     P00T = 1.0815000000000E+02
R = 0.20 L = 7 N = 29     P00T = 1.1127926443967E+02
R = 0.20 L = 7 N = 30     P00T = 1.151627179838E+02

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| ROOTS OF EQUATION 3
A = 0.20 L = 8 N = 1      ROOT = 1.0919379743727E+01
A = 0.20 L = 8 N = 2      ROOT = 1.46512619686830E+01
A = 0.20 L = 8 N = 3      ROOT = 1.8356292660696E+01
A = 0.20 L = 8 N = 4      ROOT = 2.2071565176607E+01
A = 0.20 L = 8 N = 5      ROOT = 2.5216123618993E+01
A = 0.20 L = 8 N = 6      ROOT = 2.8521565176607E+01
A = 0.20 L = 8 N = 7      ROOT = 3.1934187639685E+01
A = 0.20 L = 8 N = 8      ROOT = 3.4934187639685E+01
A = 0.20 L = 8 N = 9      ROOT = 3.8831955395499E+01
A = 0.20 L = 8 N = 10     ROOT = 4.116481198679E+01
A = 0.20 L = 8 N = 11     ROOT = 4.346423434022E+01
A = 0.20 L = 8 N = 12     ROOT = 4.7733002951464E+01
A = 0.20 L = 8 N = 13     ROOT = 5.1290077330638E+01
A = 0.20 L = 8 N = 14     ROOT = 5.4851733725620E+01
A = 0.20 L = 8 N = 15     ROOT = 5.8429833021657E+01
A = 0.20 L = 8 N = 16     ROOT = 6.2118707463838E+01
A = 0.20 L = 8 N = 17     ROOT = 6.5788777442876E+01
A = 0.20 L = 8 N = 18     ROOT = 6.9568772442876E+01
A = 0.20 L = 8 N = 19     ROOT = 7.3334838911896E+01
A = 0.20 L = 8 N = 20     ROOT = 7.7111888911896E+01
A = 0.20 L = 8 N = 21     ROOT = 8.091681180679E+01
A = 0.20 L = 8 N = 22     ROOT = 8.4729166427522E+01
A = 0.20 L = 8 N = 23     ROOT = 8.8544444444444E+01
A = 0.20 L = 8 N = 24     ROOT = 9.2382124948917E+01
A = 0.20 L = 8 N = 25     ROOT = 9.6221979685516E+01
A = 0.20 L = 8 N = 26     ROOT = 1.0000000000000E+02
A = 0.20 L = 8 N = 27     ROOT = 1.0392222295673E+02
A = 0.20 L = 8 N = 28     ROOT = 1.0779113069575E+02
A = 0.20 L = 8 N = 29     ROOT = 1.11649415963E+02
A = 0.20 L = 8 N = 30     ROOT = 1.151317995792E+02

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| ROOTS OF EQUATION 3
A = 0.20 L = 9 N = 1      ROOT = 1.1079418389691E+01
A = 0.20 L = 9 N = 2      ROOT = 1.482057850935E+01
A = 0.20 L = 9 N = 3      ROOT = 1.9581489313110E+01
A = 0.20 L = 9 N = 4      ROOT = 2.3106594004038E+01
A = 0.20 L = 9 N = 5      ROOT = 2.6516063964685E+01
A = 0.20 L = 9 N = 6      ROOT = 3.0000000000000E+01
A = 0.20 L = 9 N = 7      ROOT = 3.3144057850935E+01
A = 0.20 L = 9 N = 8      ROOT = 3.6377482934822E+01
A = 0.20 L = 9 N = 9      ROOT = 4.0111111111111E+01
A = 0.20 L = 9 N = 10     ROOT = 4.2641187452486E+01
A = 0.20 L = 9 N = 11     ROOT = 4.5744548514579E+01
A = 0.20 L = 9 N = 12     ROOT = 4.9077622865407E+01
A = 0.20 L = 9 N = 13     ROOT = 5.2292172587479E+01
A = 0.20 L = 9 N = 14     ROOT = 5.57526933390904E+01
A = 0.20 L = 9 N = 15     ROOT = 5.9270000000000E+01
A = 0.20 L = 9 N = 16     ROOT = 6.2910944797560E+01
A = 0.20 L = 9 N = 17     ROOT = 6.6568908438784E+01
A = 0.20 L = 9 N = 18     ROOT = 7.0200000000000E+01
A = 0.20 L = 9 N = 19     ROOT = 7.3986493376911E+01
A = 0.20 L = 9 N = 20     ROOT = 7.7733153756602E+01
A = 0.20 L = 9 N = 21     ROOT = 8.1500000000000E+01
A = 0.20 L = 9 N = 22     ROOT = 8.5281496376567E+01
A = 0.20 L = 9 N = 23     ROOT = 8.9077622865407E+01
A = 0.20 L = 9 N = 24     ROOT = 9.2895717180915E+01
A = 0.20 L = 9 N = 25     ROOT = 9.6699188917515E+01
A = 0.20 L = 9 N = 26     ROOT = 1.0053113772513E+02
A = 0.20 L = 9 N = 27     ROOT = 1.04366268589196E+02
A = 0.20 L = 9 N = 28     ROOT = 1.0820000000000E+02
A = 0.20 L = 9 N = 29     ROOT = 1.1205666334323E+02
A = 0.20 L = 9 N = 30     ROOT = 1.1591048921340E+02

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1 ROOTS OF EQUATION 3

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A = 0.20 L = 10 N = 1      ROOT = 1.21423941099315E+01
A = 0.20 L = 10 N = 2      ROOT = 1.69775499695650E+01
A = 0.20 L = 10 N = 3      ROOT = 2.0795956730823E+01
A = 0.20 L = 10 N = 4      ROOT = 2.4614466682524E+01
A = 0.20 L = 10 N = 5      ROOT = 2.7891779596484E+01
A = 0.20 L = 10 N = 6      ROOT = 3.1169043714539E+01
A = 0.20 L = 10 N = 7      ROOT = 3.4487801516540E+01
A = 0.20 L = 10 N = 8      ROOT = 3.7768101563933E+01
A = 0.20 L = 10 N = 9      ROOT = 4.0986415558399E+01
A = 0.20 L = 10 N = 10     ROOT = 4.4205207841935E+01
A = 0.20 L = 10 N = 11     ROOT = 4.7251164350165E+01
A = 0.20 L = 10 N = 12     ROOT = 5.035044596656E+01
A = 0.20 L = 10 N = 13     ROOT = 5.3469536078616E+01
A = 0.20 L = 10 N = 14     ROOT = 5.6598536078616E+01
A = 0.20 L = 10 N = 15     ROOT = 6.0294049216265E+01
A = 0.20 L = 10 N = 16     ROOT = 6.4062033665132E+01
A = 0.20 L = 10 N = 17     ROOT = 6.7840234932522E+01
A = 0.20 L = 10 N = 18     ROOT = 7.1641743920168E+01
A = 0.20 L = 10 N = 19     ROOT = 7.442327841935E+01
A = 0.20 L = 10 N = 20     ROOT = 7.7205007841935E+01
A = 0.20 L = 10 N = 21     ROOT = 8.10149166674337E+01
A = 0.20 L = 10 N = 22     ROOT = 8.38945329868057E+01
A = 0.20 L = 10 N = 23     ROOT = 8.6774509380540E+01
A = 0.20 L = 10 N = 24     ROOT = 9.3443378686562E+01
A = 0.20 L = 10 N = 25     ROOT = 9.2240545867372E+01
A = 0.20 L = 10 N = 26     ROOT = 9.4545867372E+01
A = 0.20 L = 10 N = 27     ROOT = 1.0486029025916E+02
A = 0.20 L = 10 N = 28     ROOT = 1.0860365785950E+02
A = 0.20 L = 10 N = 29     ROOT = 1.1236036578595E+02
A = 0.20 L = 10 N = 30     ROOT = 1.1635235293281E+02

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1 ROOTS OF EQUATION 3

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A = 0.20 L = 11 N = 1      ROOT = 1.3202620396826E+01
A = 0.20 L = 11 N = 2      ROOT = 1.7027536515955E+01
A = 0.20 L = 11 N = 3      ROOT = 2.1992553915930E+01
A = 0.20 L = 11 N = 4      ROOT = 2.5664055193057E+01
A = 0.20 L = 11 N = 5      ROOT = 2.9875797513414E+01
A = 0.20 L = 11 N = 6      ROOT = 3.4097379301655E+01
A = 0.20 L = 11 N = 7      ROOT = 3.5988378938323E+01
A = 0.20 L = 11 N = 8      ROOT = 3.9198827468126E+01
A = 0.20 L = 11 N = 9      ROOT = 4.24108827468126E+01
A = 0.20 L = 11 N = 10     ROOT = 4.5544509586857E+01
A = 0.20 L = 11 N = 11     ROOT = 4.8757584298664E+01
A = 0.20 L = 11 N = 12     ROOT = 5.19707784298664E+01
A = 0.20 L = 11 N = 13     ROOT = 5.4957393030165E+01
A = 0.20 L = 11 N = 14     ROOT = 5.8132764030568E+01
A = 0.20 L = 11 N = 15     ROOT = 6.1350000000000E+01
A = 0.20 L = 11 N = 16     ROOT = 6.4843283610130E+01
A = 0.20 L = 11 N = 17     ROOT = 6.8344665693053E+01
A = 0.20 L = 11 N = 18     ROOT = 7.185209672154930E+01
A = 0.20 L = 11 N = 19     ROOT = 7.5182180906838E+01
A = 0.20 L = 11 N = 20     ROOT = 7.8512145716507E+01
A = 0.20 L = 11 N = 21     ROOT = 8.1598448762526E+01
A = 0.20 L = 11 N = 22     ROOT = 8.4598448762526E+01
A = 0.20 L = 11 N = 23     ROOT = 9.0313753725294E+01
A = 0.20 L = 11 N = 24     ROOT = 9.3513753725294E+01
A = 0.20 L = 11 N = 25     ROOT = 9.78321831185395E+01
A = 0.20 L = 11 N = 26     ROOT = 1.0161252630140E+02
A = 0.20 L = 11 N = 27     ROOT = 1.0548452630140E+02
A = 0.20 L = 11 N = 28     ROOT = 1.09352985263014E+02
A = 0.20 L = 11 N = 29     ROOT = 1.1301984354203E+02
A = 0.20 L = 11 N = 30     ROOT = 1.1603897234250E+02

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1 ROOTS OF EQUATION 3
A + 0.20 L + 12 N + 1      ROOT = 1.4259149912425E+01
A + 0.20 L + 12 N + 2      ROOT = 1.92702937401214E+01
A + 0.20 L + 12 N + 3      ROOT = 2.31949569189408E+01
A + 0.20 L + 12 N + 4      ROOT = 2.68620375228645E+01
A + 0.20 L + 12 N + 5      ROOT = 3.0339500662646E+01
A + 0.20 L + 12 N + 6      ROOT = 3.37569351413442E+01
A + 0.20 L + 12 N + 7      ROOT = 3.71838601111111E+01
A + 0.20 L + 12 N + 8      ROOT = 4.0439837149726E+01
A + 0.20 L + 12 N + 9      ROOT = 4.3727499338406E+01
A + 0.20 L + 12 N + 10     ROOT = 4.70653811111111E+01
A + 0.20 L + 12 N + 11     ROOT = 5.0292648228276E+01
A + 0.20 L + 12 N + 12     ROOT = 5.3365463668873E+01
A + 0.20 L + 12 N + 13     ROOT = 5.64799212222222E+01
A + 0.20 L + 12 N + 14     ROOT = 5.956652856475E+01
A + 0.20 L + 12 N + 15     ROOT = 6.2729411192646E+01
A + 0.20 L + 12 N + 16     ROOT = 6.698811165677E+01
A + 0.20 L + 12 N + 17     ROOT = 7.025681755889E+01
A + 0.20 L + 12 N + 18     ROOT = 7.387892178752E+01
A + 0.20 L + 12 N + 19     ROOT = 7.642543481324E+01
A + 0.20 L + 12 N + 20     ROOT = 7.897285915894E+01
A + 0.20 L + 12 N + 21     ROOT = 8.3660047484341E+01
A + 0.20 L + 12 N + 22     ROOT = 8.7329576776747E+01
A + 0.20 L + 12 N + 23     ROOT = 9.08968888888889E+01
A + 0.20 L + 12 N + 24     ROOT = 9.4742599219265E+01
A + 0.20 L + 12 N + 25     ROOT = 9.8453786844675E+01
A + 0.20 L + 12 N + 26     ROOT = 1.02226888888889E+02
A + 0.20 L + 12 N + 27     ROOT = 1.0606084832533E+02
A + 0.20 L + 12 N + 28     ROOT = 1.0977967355948E+02
A + 0.20 L + 12 N + 29     ROOT = 1.13526268311111E+02
A + 0.20 L + 12 N + 30     ROOT = 1.1737061315389E+02

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1 ROOTS OF EQUATION 3
A + 0.20 L + 13 N + 1      ROOT = 1.5310887383718E+01
A + 0.20 L + 13 N + 2      ROOT = 2.08620375228645E+01
A + 0.20 L + 13 N + 3      ROOT = 2.6862136644515E+01
A + 0.20 L + 13 N + 4      ROOT = 3.1553687124517E+01
A + 0.20 L + 13 N + 5      ROOT = 3.624438229568E+01
A + 0.20 L + 13 N + 6      ROOT = 3.8417981558175E+01
A + 0.20 L + 13 N + 7      ROOT = 4.1757128080505E+01
A + 0.20 L + 13 N + 8      ROOT = 4.51928111111111E+01
A + 0.20 L + 13 N + 9      ROOT = 4.8343123238997E+01
A + 0.20 L + 13 N + 10     ROOT = 5.1594338229568E+01
A + 0.20 L + 13 N + 11     ROOT = 5.5194338229568E+01
A + 0.20 L + 13 N + 12     ROOT = 5.8793473832618E+01
A + 0.20 L + 13 N + 13     ROOT = 5.7973473832618E+01
A + 0.20 L + 13 N + 14     ROOT = 6.1093389874849E+01
A + 0.20 L + 13 N + 15     ROOT = 6.4326862334621E+01
A + 0.20 L + 13 N + 16     ROOT = 6.7326862334621E+01
A + 0.20 L + 13 N + 17     ROOT = 7.05896390641261E+01
A + 0.20 L + 13 N + 18     ROOT = 7.39568390641261E+01
A + 0.20 L + 13 N + 19     ROOT = 7.7329163893170E+01
A + 0.20 L + 13 N + 20     ROOT = 8.0948397656593E+01
A + 0.20 L + 13 N + 21     ROOT = 8.451495311989E+01
A + 0.20 L + 13 N + 22     ROOT = 8.814683505809E+01
A + 0.20 L + 13 N + 23     ROOT = 9.18011134736871E+01
A + 0.20 L + 13 N + 24     ROOT = 9.3461412835332E+01
A + 0.20 L + 13 N + 25     ROOT = 9.412835332E+01
A + 0.20 L + 13 N + 26     ROOT = 1.0298739304181E+02
A + 0.20 L + 13 N + 27     ROOT = 1.0654693518939E+02
A + 0.20 L + 13 N + 28     ROOT = 1.092136518939E+02
A + 0.20 L + 13 N + 29     ROOT = 1.1416871986255E+02
A + 0.20 L + 13 N + 30     ROOT = 1.1794762446162E+02

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ROOTS OF EQUATION 3

```

A • 0.20 L • 14 N • 1      ROOT • 1.630672740457E+01
A • 0.20 L • 14 N • 2      ROOT • 2.1537120336218E+01
A • 0.20 L • 14 N • 3      ROOT • 2.5561873316915E+01
A • 0.20 L • 14 N • 4      ROOT • 2.862457136454E+01
A • 0.20 L • 14 N • 5      ROOT • 3.2819275645169E+01
A • 0.20 L • 14 N • 6      ROOT • 3.5859591694853E+01
A • 0.20 L • 14 N • 7      ROOT • 3.8062501513495E+01
A • 0.20 L • 14 N • 8      ROOT • 3.96561513495E+01
A • 0.20 L • 14 N • 9      ROOT • 4.0588570384787E+01
A • 0.20 L • 14 N • 10     ROOT • 4.1662537645485E+01
A • 0.20 L • 14 N • 11     ROOT • 4.286317526485E+01
A • 0.20 L • 14 N • 12     ROOT • 4.42000000000E+01
A • 0.20 L • 14 N • 13     ROOT • 4.5616851321781E+01
A • 0.20 L • 14 N • 14     ROOT • 4.6984842588404E+01
A • 0.20 L • 14 N • 15     ROOT • 4.8594476259755E+01
A • 0.20 L • 14 N • 16     ROOT • 5.0367457133647E+01
A • 0.20 L • 14 N • 17     ROOT • 5.22307457133647E+01
A • 0.20 L • 14 N • 18     ROOT • 5.4174947098355E+01
A • 0.20 L • 14 N • 19     ROOT • 5.6207323598901E+01
A • 0.20 L • 14 N • 20     ROOT • 5.82300000000E+01
A • 0.20 L • 14 N • 21     ROOT • 6.025266389392E+01
A • 0.20 L • 14 N • 22     ROOT • 6.22750000000E+01
A • 0.20 L • 14 N • 23     ROOT • 6.42977500000E+01
A • 0.20 L • 14 N • 24     ROOT • 6.6282566168055E+01
A • 0.20 L • 14 N • 25     ROOT • 6.8269874678050E+01
A • 0.20 L • 14 N • 26     ROOT • 7.02410000000E+01
A • 0.20 L • 14 N • 27     ROOT • 7.2212195219E+01
A • 0.20 L • 14 N • 28     ROOT • 7.4183397905740E+01
A • 0.20 L • 14 N • 29     ROOT • 7.61545442736E+01
A • 0.20 L • 14 N • 30     ROOT • 7.81257000000E+01

```

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1 ROOTS OF EQUATION 3

```

A • 0.20 L • 15 N • 1      ROOT • 1.7408833803097E+01
A • 0.20 L • 15 N • 2      ROOT • 2.2662453433694E+01
A • 0.20 L • 15 N • 3      ROOT • 2.6735177305355E+01
A • 0.20 L • 15 N • 4      ROOT • 3.080830221113E+01
A • 0.20 L • 15 N • 5      ROOT • 3.4077867691380E+01
A • 0.20 L • 15 N • 6      ROOT • 3.7568918307348E+01
A • 0.20 L • 15 N • 7      ROOT • 4.10423944479E+01
A • 0.20 L • 15 N • 8      ROOT • 4.435642567145E+01
A • 0.20 L • 15 N • 9      ROOT • 4.7704239444970E+01
A • 0.20 L • 15 N • 10     ROOT • 5.1052394444970E+01
A • 0.20 L • 15 N • 11     ROOT • 5.4302646665512E+01
A • 0.20 L • 15 N • 12     ROOT • 5.7568302221113E+01
A • 0.20 L • 15 N • 13     ROOT • 6.0825726491512E+01
A • 0.20 L • 15 N • 14     ROOT • 6.4022726491512E+01
A • 0.20 L • 15 N • 15     ROOT • 6.71895277666936E+01
A • 0.20 L • 15 N • 16     ROOT • 7.0356372666936E+01
A • 0.20 L • 15 N • 17     ROOT • 7.3398951086231E+01
A • 0.20 L • 15 N • 18     ROOT • 7.6533596120811E+01
A • 0.20 L • 15 N • 19     ROOT • 8.00000000000E+01
A • 0.20 L • 15 N • 20     ROOT • 8.3098240933956E+01
A • 0.20 L • 15 N • 21     ROOT • 8.652192723954E+01
A • 0.20 L • 15 N • 22     ROOT • 9.00000000000E+01
A • 0.20 L • 15 N • 23     ROOT • 9.3461652613974E+01
A • 0.20 L • 15 N • 24     ROOT • 9.7149654464291E+01
A • 0.20 L • 15 N • 25     ROOT • 1.0082312129842E+02
A • 0.20 L • 15 N • 26     ROOT • 1.044239312129842E+02
A • 0.20 L • 15 N • 27     ROOT • 1.0809941273051E+02
A • 0.20 L • 15 N • 28     ROOT • 1.1179556951677E+02
A • 0.20 L • 15 N • 29     ROOT • 1.15472200000E+02
A • 0.20 L • 15 N • 30     ROOT • 1.1923973817509E+02

```

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```

1 ROOTS OF EQUATION 3
A + 0.30 L + 1 N + 1      ROOT = 2.0861911515795E+00
A + 0.30 L + 1 N + 2      ROOT = 5.8159967819125E+00
A + 0.30 L + 1 N + 3      ROOT = 9.7239952285272E+00
A + 0.30 L + 1 N + 4      ROOT = 1.4326495425340E+01
A + 0.30 L + 1 N + 5      ROOT = 1.8326495425340E+01
A + 0.30 L + 1 N + 6      ROOT = 2.2738811370598E+01
A + 0.30 L + 1 N + 7      ROOT = 2.7176611259138E+01
A + 0.30 L + 1 N + 8      ROOT = 3.16286495425340E+01
A + 0.30 L + 1 N + 9      ROOT = 3.6890963725157E+01
A + 0.30 L + 1 N + 10     ROOT = 4.05573923217537E+01
A + 0.30 L + 1 N + 11     ROOT = 4.36286495425340E+01
A + 0.30 L + 1 N + 12     ROOT = 4.5983118666974E+01
A + 0.30 L + 1 N + 13     ROOT = 5.3979811377385E+01
A + 0.30 L + 1 N + 14     ROOT = 6.1328836504672E+01
A + 0.30 L + 1 N + 15     ROOT = 6.2938051787341E+01
A + 0.30 L + 1 N + 16     ROOT = 6.418950864987E+01
A + 0.30 L + 1 N + 17     ROOT = 6.5449111616433E+01
A + 0.30 L + 1 N + 18     ROOT = 6.6932344616778E+01
A + 0.30 L + 1 N + 19     ROOT = 6.8666381145522E+01
A + 0.30 L + 1 N + 20     ROOT = 7.0440954967608E+01
A + 0.30 L + 1 N + 21     ROOT = 8.3634954967608E+01
A + 0.30 L + 1 N + 22     ROOT = 9.4318543749956E+01
A + 0.30 L + 1 N + 23     ROOT = 9.8166666666666E+01
A + 0.30 L + 1 N + 24     ROOT = 1.0228836504672E+02
A + 0.30 L + 1 N + 25     ROOT = 1.0773366092563E+02
A + 0.30 L + 1 N + 26     ROOT = 1.1328836504672E+02
A + 0.30 L + 1 N + 27     ROOT = 1.187367488641E+02
A + 0.30 L + 1 N + 28     ROOT = 1.212307466783E+02
A + 0.30 L + 1 N + 29     ROOT = 1.2571676991598E+02
A + 0.30 L + 1 N + 30     ROOT = 1.3020232884649E+02

```

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1 ROOTS OF EQUATION 3
A + 0.30 L + 2 N + 1      ROOT = 3.3173341552458E+00
A + 0.30 L + 2 N + 2      ROOT = 7.0658897614283E+00
A + 0.30 L + 2 N + 3      ROOT = 1.0528111816433E+01
A + 0.30 L + 2 N + 4      ROOT = 1.4491340687566E+01
A + 0.30 L + 2 N + 5      ROOT = 1.8457446667161E+01
A + 0.30 L + 2 N + 6      ROOT = 2.3043725621810E+01
A + 0.30 L + 2 N + 7      ROOT = 2.7428745045854E+01
A + 0.30 L + 2 N + 8      ROOT = 3.1810444444444E+01
A + 0.30 L + 2 N + 9      ROOT = 3.6277705149843E+01
A + 0.30 L + 2 N + 10     ROOT = 4.0723715676529E+01
A + 0.30 L + 2 N + 11     ROOT = 4.42698652199E+01
A + 0.30 L + 2 N + 12     ROOT = 4.9638986527199E+01
A + 0.30 L + 2 N + 13     ROOT = 5.4104113974318E+01
A + 0.30 L + 2 N + 14     ROOT = 5.8570444444444E+01
A + 0.30 L + 2 N + 15     ROOT = 6.3044517290739E+01
A + 0.30 L + 2 N + 16     ROOT = 6.7518274325980E+01
A + 0.30 L + 2 N + 17     ROOT = 7.2095133333333E+01
A + 0.30 L + 2 N + 18     ROOT = 7.6470835986330E+01
A + 0.30 L + 2 N + 19     ROOT = 8.0949076326255E+01
A + 0.30 L + 2 N + 20     ROOT = 8.5426783333333E+01
A + 0.30 L + 2 N + 21     ROOT = 8.9968426904621E+01
A + 0.30 L + 2 N + 22     ROOT = 9.4389396563516E+01
A + 0.30 L + 2 N + 23     ROOT = 9.8821111111111E+01
A + 0.30 L + 2 N + 24     ROOT = 1.0335363131313E+02
A + 0.30 L + 2 N + 25     ROOT = 1.0783562637595E+02
A + 0.30 L + 2 N + 26     ROOT = 1.1235251888889E+02
A + 0.30 L + 2 N + 27     ROOT = 1.1682836366667E+02
A + 0.30 L + 2 N + 28     ROOT = 1.2128581366712E+02
A + 0.30 L + 2 N + 29     ROOT = 1.2576986681126E+02
A + 0.30 L + 2 N + 30     ROOT = 1.3025419105249E+02

```

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## ROOTS OF EQUATION 3

```

A = 0.30 L = 3 N = 1          ROOT = 4.5678785567162E+08
A = 0.30 L = 3 N = 2          ROOT = 1.40678500000000E+00
A = 0.30 L = 3 N = 3          ROOT = 1.1674867926407E+01
A = 0.30 L = 3 N = 4          ROOT = 1.5289712323501E+01
A = 0.30 L = 3 N = 5          ROOT = 1.00000000000000E+01
A = 0.30 L = 3 N = 6          ROOT = 2.359015786414E+01
A = 0.30 L = 3 N = 7          ROOT = 2.7966595363933E+01
A = 0.30 L = 3 N = 8          ROOT = 1.80000000000000E+01
A = 0.30 L = 3 N = 9          ROOT = 3.6559575470389E+01
A = 0.30 L = 3 N = 10         ROOT = 4.8972394870598E+01
A = 0.30 L = 3 N = 11         ROOT = 1.00000000000000E+01
A = 0.30 L = 3 N = 12         ROOT = 4.9842326494980E+01
A = 0.30 L = 3 N = 13         ROOT = 5.429050931352E+01
A = 0.30 L = 3 N = 14         ROOT = 2.00000000000000E+01
A = 0.30 L = 3 N = 15         ROOT = 3.3204879940405E+01
A = 0.30 L = 3 N = 16         ROOT = 6.7667147878155E+01
A = 0.30 L = 3 N = 17         ROOT = 1.00000000000000E+01
A = 0.30 L = 3 N = 18         ROOT = 7.6602129822807E+01
A = 0.30 L = 3 N = 19         ROOT = 8.1073951759791E+01
A = 0.30 L = 3 N = 20         ROOT = 9.00000000000000E+01
A = 0.30 L = 3 N = 21         ROOT = 0.00200370343628E+01
A = 0.30 L = 3 N = 22         ROOT = 9.44595676028234E+01
A = 0.30 L = 3 N = 23         ROOT = 9.89723153215059E+01
A = 0.30 L = 3 N = 24         ROOT = 1.00000000000000E+02
A = 0.30 L = 3 N = 25         ROOT = 1.0792854528466E+02
A = 0.30 L = 3 N = 26         ROOT = 1.1248085086601E+02
A = 0.30 L = 3 N = 27         ROOT = 1.17000000000000E+02
A = 0.30 L = 3 N = 28         ROOT = 1.2136839343202E+02
A = 0.30 L = 3 N = 29         ROOT = 1.2564949533895E+02
A = 0.30 L = 3 N = 30         ROOT = 1.3033106957475E+02

```

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## ROOTS OF EQUATION 3

```

A = 0.30 L = 4 N = 1          ROOT = 5.6453140840246E+08
A = 0.30 L = 4 N = 2          ROOT = 5.7941355125874E+08
A = 0.30 L = 4 N = 3          ROOT = 1.3033126561499E+01
A = 0.30 L = 4 N = 4          ROOT = 1.6328188174047E+01
A = 0.30 L = 4 N = 5          ROOT = 1.00000000000000E+01
A = 0.30 L = 4 N = 6          ROOT = 2.410818964615E+01
A = 0.30 L = 4 N = 7          ROOT = 2.63897395602327E+01
A = 0.30 L = 4 N = 8          ROOT = 3.00000000000000E+01
A = 0.30 L = 4 N = 9          ROOT = 3.6932137731741E+01
A = 0.30 L = 4 N = 10         ROOT = 4.1394414247046E+01
A = 0.30 L = 4 N = 11         ROOT = 4.60000000000000E+01
A = 0.30 L = 4 N = 12         ROOT = 5.0113985481710E+01
A = 0.30 L = 4 N = 13         ROOT = 5.4538982565959E+01
A = 0.30 L = 4 N = 14         ROOT = 5.90000000000000E+01
A = 0.30 L = 4 N = 15         ROOT = 6.3416578238029E+01
A = 0.30 L = 4 N = 16         ROOT = 6.7965435282692E+01
A = 0.30 L = 4 N = 17         ROOT = 7.25000000000000E+01
A = 0.30 L = 4 N = 18         ROOT = 7.6777540132088E+01
A = 0.30 L = 4 N = 19         ROOT = 8.1238228145293E+01
A = 0.30 L = 4 N = 20         ROOT = 8.60000000000000E+01
A = 0.30 L = 4 N = 21         ROOT = 9.0168671778163E+01
A = 0.30 L = 4 N = 22         ROOT = 9.4637155277195E+01
A = 0.30 L = 4 N = 23         ROOT = 9.912515177458E+01
A = 0.30 L = 4 N = 24         ROOT = 9.357322877768E+02
A = 0.30 L = 4 N = 25         ROOT = 1.08952358297251E+02
A = 0.30 L = 4 N = 26         ROOT = 1.12525000000000E+02
A = 0.30 L = 4 N = 27         ROOT = 1.1858383095E+02
A = 0.30 L = 4 N = 28         ROOT = 1.2147846129756E+02
A = 0.30 L = 4 N = 29         ROOT = 1.2595562791509E+02
A = 0.30 L = 4 N = 30         ROOT = 1.3043354199067E+02

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ROOTS OF EQUATION 3					
6.38	L	*	5	N	1
6.38	L	*	5	N	2
6.38	L	*	5	N	3
6.38	L	*	5	N	4
6.38	L	*	5	N	5
6.38	L	*	5	N	6
6.38	L	*	5	N	7
6.38	L	*	5	N	8
6.38	L	*	5	N	9
6.38	L	*	5	N	10
6.38	L	*	5	N	11
6.38	L	*	5	N	12
6.38	L	*	5	N	13
6.38	L	*	5	N	14
6.38	L	*	5	N	15
6.38	L	*	5	N	16
6.38	L	*	5	N	17
6.38	L	*	5	N	18
6.38	L	*	5	N	19
6.38	L	*	5	N	20
6.38	L	*	5	N	21
6.38	L	*	5	N	22
6.38	L	*	5	N	23
6.38	L	*	5	N	24
6.38	L	*	5	N	25
6.38	L	*	5	N	26
6.38	L	*	5	N	27
6.38	L	*	5	N	28
6.38	L	*	5	N	29
6.38	L	*	5	N	30
ROOT					6.7551659814466E+00
ROOT					1.18510737156E+01
ROOT					1.4439782457686E+01
ROOT					2.1460165245925E+01
ROOT					2.4876522412631E+01
ROOT					3.117284692949E+01
ROOT					3.735978570559916E+01
ROOT					4.6871942038635E+01
ROOT					5.4880526713635E+01
ROOT					6.36818134475750E+01
ROOT					6.811232474325E+01
ROOT					7.6959449987617E+01
ROOT					8.14445022685727E+01
ROOT					8.905312918274E+01
ROOT					9.48136397694E+01
ROOT					9.91625207457E+01
ROOT					1.037650227739E+02
ROOT					1.082079033352E+02
ROOT					1.127494236376E+02
ROOT					1.2161598467482E+02
ROOT					1.30515621951E+02
ROOT					1.39561528563E+02

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ROOTS OF EQUATION 3

R 0. 0.38 L 6 N * 1 ROOT 7.8510199529826E+00
R 0. 0.39 L 6 N * 2 ROOT 1.2273614565118E+01
R 0. 0.38 L 6 N * 3 ROOT 5.5796815967265E+01
R 0. 0.39 L 6 N * 4 ROOT 1.2273614565118E+01
R 0. 0.30 L 6 N * 5 ROOT 2.212437752577E+01
R 0. 0.30 L 6 N * 6 ROOT 5.579329655634E+01
R 0. 0.30 L 6 N * 7 ROOT 1.2273614565118E+01
R 0. 0.38 L 6 N * 8 ROOT 3.3767723882681E+01
R 0. 0.39 L 6 N * 9 ROOT 3.7595428668675E+01
R 0. 0.38 L 6 N * 10 ROOT 4.651637839566E+01
R 0. 0.39 L 6 N * 11 ROOT 4.651637839566E+01
R 0. 0.30 L 6 N * 12 ROOT 5.8855166733988E+01
R 0. 0.30 L 6 N * 13 ROOT 1.2273614565118E+01
R 0. 0.30 L 6 N * 14 ROOT 3.96151363131E+01
R 0. 0.30 L 6 N * 15 ROOT 6.399547927632E+01
R 0. 0.30 L 6 N * 16 ROOT 6.8489565685843E+01
R 0. 0.30 L 6 N * 17 ROOT 7.252718309037E+01
R 0. 0.38 L 6 N * 18 ROOT 8.1617947129316E+01
R 0. 0.39 L 6 N * 19 ROOT 8.1617947129316E+01
R 0. 0.30 L 6 N * 20 ROOT 9.8567857825266E+01
R 0. 0.30 L 6 N * 21 ROOT 9.8567857825266E+01
R 0. 0.38 L 6 N * 22 ROOT 9.5295863994981E+01
R 0. 0.39 L 6 N * 23 ROOT 9.5295863994981E+01
R 0. 0.30 L 6 N * 24 ROOT 1.0393424142109E+02
R 0. 0.30 L 6 N * 25 ROOT 1.039362033352E+02
R 0. 0.30 L 6 N * 26 ROOT 1.120261470733E+02
R 0. 0.38 L 6 N * 27 ROOT 1.120261470733E+02
R 0. 0.38 L 6 N * 28 ROOT 1.2176982332490E+02
R 0. 0.39 L 6 N * 29 ROOT 1.2624471815181E+02
R 0. 0.38 L 6 N * 30 ROOT 1.2624471815181E+02

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1 ROOTS OF EQUATION 3
A = 0.30 L = 7 N = 1      ROOT = 8.8749274109939E+01
A = 0.30 L = 7 N = 2      ROOT = 1.3479439265232E+01
A = 0.30 L = 7 N = 3      ROOT = 1.7091976984037E+01
A = 0.30 L = 7 N = 4      ROOT = 2.0592111828342E+01
A = 0.30 L = 7 N = 5      ROOT = 2.3552111828342E+01
A = 0.30 L = 7 N = 6      ROOT = 2.6864656761862E+01
A = 0.30 L = 7 N = 7      ROOT = 3.0276859863394E+01
A = 0.30 L = 7 N = 8      ROOT = 3.4515377901681E+01
A = 0.30 L = 7 N = 9      ROOT = 3.8685986339429E+01
A = 0.30 L = 7 N = 10     ROOT = 4.2858261964878E+01
A = 0.30 L = 7 N = 11     ROOT = 4.7034578641250E+01
A = 0.30 L = 7 N = 12     ROOT = 5.1325738673728E+01
A = 0.30 L = 7 N = 13     ROOT = 5.5678995257532E+01
A = 0.30 L = 7 N = 14     ROOT = 5.9899595257532E+01
A = 0.30 L = 7 N = 15     ROOT = 6.4359521305163E+01
A = 0.30 L = 7 N = 16     ROOT = 6.8759521305163E+01
A = 0.30 L = 7 N = 17     ROOT = 7.3125287460197E+01
A = 0.30 L = 7 N = 18     ROOT = 7.7562157482135E+01
A = 0.30 L = 7 N = 19     ROOT = 8.2000000000000E+01
A = 0.30 L = 7 N = 20     ROOT = 8.6464897411318E+01
A = 0.30 L = 7 N = 21     ROOT = 9.0836261964878E+01
A = 0.30 L = 7 N = 22     ROOT = 9.527301964878E+01
A = 0.30 L = 7 N = 23     ROOT = 9.97083332762E+01
A = 0.30 L = 7 N = 24     ROOT = 1.0415989332762E+02
A = 0.30 L = 7 N = 25     ROOT = 1.0868097676287E+02
A = 0.30 L = 7 N = 26     ROOT = 1.13229801812871E+02
A = 0.30 L = 7 N = 27     ROOT = 1.1751598980324E+02
A = 0.30 L = 7 N = 28     ROOT = 1.2197322976226E+02
A = 0.30 L = 7 N = 29     ROOT = 1.2638750000000E+02
A = 0.30 L = 7 N = 30     ROOT = 1.30893423166182E+02

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1 ROOTS OF EQUATION 3
A = 0.30 L = 8 N = 1      ROOT = 1.6910368550777E+01
A = 0.30 L = 8 N = 2      ROOT = 1.465084410541E+01
A = 0.30 L = 8 N = 3      ROOT = 1.238162444601E+01
A = 0.30 L = 8 N = 4      ROOT = 2.1771196977175E+01
A = 0.30 L = 8 N = 5      ROOT = 2.4963463867547E+01
A = 0.30 L = 8 N = 6      ROOT = 2.8153863626743E+01
A = 0.30 L = 8 N = 7      ROOT = 3.1680719333568E+01
A = 0.30 L = 8 N = 8      ROOT = 3.5374498865050E+01
A = 0.30 L = 8 N = 9      ROOT = 3.9065498865050E+01
A = 0.30 L = 8 N = 10     ROOT = 4.3445498157344E+01
A = 0.30 L = 8 N = 11     ROOT = 4.7624983626743E+01
A = 0.30 L = 8 N = 12     ROOT = 5.1804498865050E+01
A = 0.30 L = 8 N = 13     ROOT = 5.6141973000868E+01
A = 0.30 L = 8 N = 14     ROOT = 6.0454084172339E+01
A = 0.30 L = 8 N = 15     ROOT = 6.4864861946289E+01
A = 0.30 L = 8 N = 16     ROOT = 6.914861946289E+01
A = 0.30 L = 8 N = 17     ROOT = 7.3522923957833E+01
A = 0.30 L = 8 N = 18     ROOT = 7.7805710365496E+01
A = 0.30 L = 8 N = 19     ROOT = 8.2105710365496E+01
A = 0.30 L = 8 N = 20     ROOT = 8.6716447292485E+01
A = 0.30 L = 8 N = 21     ROOT = 9.1323221589520E+01
A = 0.30 L = 8 N = 22     ROOT = 9.5983221589520E+01
A = 0.30 L = 8 N = 23     ROOT = 9.9981720819689E+01
A = 0.30 L = 8 N = 24     ROOT = 1.044817531918E+02
A = 0.30 L = 8 N = 25     ROOT = 1.0914949175319E+02
A = 0.30 L = 8 N = 26     ROOT = 1.1329813573155E+02
A = 0.30 L = 8 N = 27     ROOT = 1.1774393215736E+02
A = 0.30 L = 8 N = 28     ROOT = 1.2238750000000E+02
A = 0.30 L = 8 N = 29     ROOT = 1.26644553511552E+02
A = 0.30 L = 8 N = 30     ROOT = 1.310987567200E+02

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1 ROOTS OF EQUATION 3
A = 0.39 L = 9 N = 1      ROOT = 1.10795417976709E+01
A = 0.39 L = 9 N = 2      ROOT = 1.5819109399657E+01
A = 0.39 L = 9 N = 3      ROOT = 1.957969805532E+01
A = 0.39 L = 9 N = 4      ROOT = 2.267967646724E+01
A = 0.39 L = 9 N = 5      ROOT = 2.6377406510172E+01
A = 0.39 L = 9 N = 6      ROOT = 2.9516065891568E+01
A = 0.39 L = 9 N = 7      ROOT = 3.2350865891568E+01
A = 0.39 L = 9 N = 8      ROOT = 3.635198189973E+01
A = 0.39 L = 9 N = 9      ROOT = 4.018721721814E+01
A = 0.39 L = 9 N = 10     ROOT = 4.4028828961298E+01
A = 0.39 L = 9 N = 11     ROOT = 4.8288289862198E+01
A = 0.39 L = 9 N = 12     ROOT = 5.2464491521809E+01
A = 0.39 L = 9 N = 13     ROOT = 5.6664491521809E+01
A = 0.39 L = 9 N = 14     ROOT = 6.0953973970637E+01
A = 0.39 L = 9 N = 15     ROOT = 6.5255189496822E+01
A = 0.39 L = 9 N = 16     ROOT = 6.966777784683E+01
A = 0.39 L = 9 N = 17     ROOT = 7.3937777784683E+01
A = 0.39 L = 9 N = 18     ROOT = 7.8398659884012E+01
A = 0.39 L = 9 N = 19     ROOT = 8.2759865988401E+01
A = 0.39 L = 9 N = 20     ROOT = 8.706642222840E+01
A = 0.39 L = 9 N = 21     ROOT = 9.1464942621115E+01
A = 0.39 L = 9 N = 22     ROOT = 9.5874942621115E+01
A = 0.39 L = 9 N = 23     ROOT = 1.0028631874257E+02
A = 0.39 L = 9 N = 24     ROOT = 1.0470765167692E+02
A = 0.39 L = 9 N = 25     ROOT = 1.135645386149E+02
A = 0.39 L = 9 N = 26     ROOT = 1.1800024713914E+02
A = 0.39 L = 9 N = 27     ROOT = 1.2208274183404E+02
A = 0.39 L = 9 N = 28     ROOT = 1.2628827418340E+02
A = 0.39 L = 9 N = 30     ROOT = 1.3132868395766E+02

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1 ROOTS OF EQUATION 3
A = 0.30 L = 10 N = 1      ROOT = 1.214328402421BE+01
A = 0.30 L = 10 N = 2      ROOT = 1.679512146454E+01
A = 0.30 L = 10 N = 3      ROOT = 2.43503623391128E+01
A = 0.30 L = 10 N = 4      ROOT = 2.763573811259E+01
A = 0.30 L = 10 N = 5      ROOT = 3.092001345394E+01
A = 0.30 L = 10 N = 6      ROOT = 3.40843577631134E+01
A = 0.30 L = 10 N = 7      ROOT = 3.74567753436617E+01
A = 0.30 L = 10 N = 8      ROOT = 4.082856666172E+01
A = 0.30 L = 10 N = 9      ROOT = 4.5080853987752E+01
A = 0.30 L = 10 N = 10     ROOT = 4.9024374440585E+01
A = 0.30 L = 10 N = 11     ROOT = 5.306162520588E+01
A = 0.30 L = 10 N = 12     ROOT = 5.7306162520588E+01
A = 0.30 L = 10 N = 13     ROOT = 6.1529857842973E+01
A = 0.30 L = 10 N = 14     ROOT = 6.5753227842973E+01
A = 0.30 L = 10 N = 15     ROOT = 6.988172029252E+01
A = 0.30 L = 10 N = 16     ROOT = 7.0081717202925E+01
A = 0.30 L = 10 N = 17     ROOT = 7.4397913553537E+01
A = 0.30 L = 10 N = 18     ROOT = 7.808737947168E+01
A = 0.30 L = 10 N = 19     ROOT = 8.308737947168E+01
A = 0.30 L = 10 N = 20     ROOT = 8.7454663350772E+01
A = 0.30 L = 10 N = 21     ROOT = 9.1854663350772E+01
A = 0.30 L = 10 N = 22     ROOT = 9.6223508890246E+01
A = 0.30 L = 10 N = 23     ROOT = 1.0062211268849E+02
A = 0.30 L = 10 N = 24     ROOT = 1.04944145226713E+02
A = 0.30 L = 10 N = 25     ROOT = 1.0944145226713E+02
A = 0.30 L = 10 N = 26     ROOT = 1.1396046874904E+02
A = 0.30 L = 10 N = 27     ROOT = 1.182861252765E+02
A = 0.30 L = 10 N = 28     ROOT = 1.227377986259E+02
A = 0.30 L = 10 N = 29     ROOT = 1.2714696684590E+02

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1 ROOTS OF EQUATION 3
A • 0 .39 L • 11 N • 1      ROOT • 1.320320302744E+01
A • 0 .39 L • 11 N • 2      ROOT • 1.8127558641051E+01
A • 0 .39 L • 11 N • 3      ROOT • 2.1999718684051E+01
A • 0 .39 L • 11 N • 4      ROOT • 2.5863816521451E+01
A • 0 .39 L • 11 N • 5      ROOT • 2.98476497246775E+01
A • 0 .39 L • 11 N • 6      ROOT • 3.2341394285572E+01
A • 0 .39 L • 11 N • 7      ROOT • 3.4820540111111E+01
A • 0 .39 L • 11 N • 8      ROOT • 3.6852917957635E+01
A • 0 .39 L • 11 N • 9      ROOT • 4.217791893289E+01
A • 0 .39 L • 11 N • 10     ROOT • 4.840361851365E+01
A • 0 .39 L • 11 N • 11     ROOT • 5.051680524038E+01
A • 0 .39 L • 11 N • 12     ROOT • 5.386731338394E+01
A • 0 .39 L • 11 N • 13     ROOT • 5.7978431661111E+01
A • 0 .39 L • 11 N • 14     ROOT • 6.2033917391E+01
A • 0 .39 L • 11 N • 15     ROOT • 6.6366641227264E+01
A • 0 .39 L • 11 N • 16     ROOT • 7.0626449754124E+01
A • 0 .39 L • 11 N • 17     ROOT • 7.4938480481111E+01
A • 0 .39 L • 11 N • 18     ROOT • 7.9214038552294E+01
A • 0 .39 L • 11 N • 19     ROOT • 8.352788736557E+01
A • 0 .39 L • 11 N • 20     ROOT • 8.7841891801111E+01
A • 0 .39 L • 11 N • 21     ROOT • 9.2339265523925E+01
A • 0 .39 L • 11 N • 22     ROOT • 9.6699813865931E+01
A • 0 .39 L • 11 N • 23     ROOT • 1.0144265616644E+02
A • 0 .39 L • 11 N • 24     ROOT • 1.0538138756673E+02
A • 0 .39 L • 11 N • 25     ROOT • 1.0977988246296E+02
A • 0 .39 L • 11 N • 26     ROOT • 1.1412281881111E+02
A • 0 .39 L • 11 N • 27     ROOT • 1.185974213488E+02
A • 0 .39 L • 11 N • 28     ROOT • 1.2301495024278E+02
A • 0 .39 L • 11 N • 29     ROOT • 1.2743748851659E+02
A • 0 .39 L • 11 N • 30     ROOT • 1.3217938623067E+02

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1 ROOTS OF EQUATION 3
A • 0 .39 L • 12 N • 1      ROOT • 1.4259340818864E+01
A • 0 .39 L • 12 N • 2      ROOT • 1.9270292344375E+01
A • 0 .39 L • 12 N • 3      ROOT • 2.319282954828E+01
A • 0 .39 L • 12 N • 4      ROOT • 2.6980417174151E+01
A • 0 .39 L • 12 N • 5      ROOT • 3.0328403186081E+01
A • 0 .39 L • 12 N • 6      ROOT • 3.3695387466135E+01
A • 0 .39 L • 12 N • 7      ROOT • 3.7070411111111E+01
A • 0 .39 L • 12 N • 8      ROOT • 4.0043496883923E+01
A • 0 .39 L • 12 N • 9      ROOT • 4.3345834173429E+01
A • 0 .39 L • 12 N • 10     ROOT • 4.6678081111111E+01
A • 0 .39 L • 12 N • 11     ROOT • 5.0726356707601E+01
A • 0 .39 L • 12 N • 12     ROOT • 5.4659656893322E+01
A • 0 .39 L • 12 N • 13     ROOT • 5.8592081111111E+01
A • 0 .39 L • 12 N • 14     ROOT • 6.2825397474914E+01
A • 0 .39 L • 12 N • 15     ROOT • 6.6924265752047E+01
A • 0 .39 L • 12 N • 16     ROOT • 7.0850000000000E+01
A • 0 .39 L • 12 N • 17     ROOT • 7.4522577449429E+01
A • 0 .39 L • 12 N • 18     ROOT • 7.9728975911995E+01
A • 0 .39 L • 12 N • 19     ROOT • 8.4650000000000E+01
A • 0 .39 L • 12 N • 20     ROOT • 8.8142955415352E+01
A • 0 .39 L • 12 N • 21     ROOT • 9.2686675483248E+01
A • 0 .39 L • 12 N • 22     ROOT • 9.7030000000000E+01
A • 0 .39 L • 12 N • 23     ROOT • 1.0139289277089E+02
A • 0 .39 L • 12 N • 24     ROOT • 1.0576596305575E+02
A • 0 .39 L • 12 N • 25     ROOT • 1.1018624956074E+02
A • 0 .39 L • 12 N • 26     ROOT • 1.1453700000000E+02
A • 0 .39 L • 12 N • 27     ROOT • 1.1893811653712E+02
A • 0 .39 L • 12 N • 28     ROOT • 1.2334215845298E+02
A • 0 .39 L • 12 N • 29     ROOT • 1.2774734833482E+02
A • 0 .39 L • 12 N • 30     ROOT • 1.3217938623067E+02

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1 ROOTS OF EQUATION 3
A • 0.30 L • 13 N • 1      ROOT • 1.5310897383256E+01
A • 0.30 L • 13 N • 2      ROOT • 2.482619262562E+01
A • 0.30 L • 13 N • 3      ROOT • 2.438219262562E+01
A • 0.30 L • 13 N • 4      ROOT • 2.8861759216987E+01
A • 0.30 L • 13 N • 5      ROOT • 3.1492352487749E+01
A • 0.30 L • 13 N • 6      ROOT • 3.5088868526257E+01
A • 0.30 L • 13 N • 7      ROOT • 3.8303401253926E+01
A • 0.30 L • 13 N • 8      ROOT • 4.1497352487749E+01
A • 0.30 L • 13 N • 9      ROOT • 4.45935276355E+01
A • 0.30 L • 13 N • 10     ROOT • 4.8838586267397E+01
A • 0.30 L • 13 N • 11     ROOT • 5.3008081952094E+01
A • 0.30 L • 13 N • 12     ROOT • 5.72059518471E+01
A • 0.30 L • 13 N • 13     ROOT • 5.95059766313741E+01
A • 0.30 L • 13 N • 14     ROOT • 6.3525617240772E+01
A • 0.30 L • 13 N • 15     ROOT • 6.71017240772E+01
A • 0.30 L • 13 N • 16     ROOT • 7.1840102693836E+01
A • 0.30 L • 13 N • 17     ROOT • 7.680559287630E+01
A • 0.30 L • 13 N • 18     ROOT • 8.188608827630E+01
A • 0.30 L • 13 N • 19     ROOT • 8.4556259682958E+01
A • 0.30 L • 13 N • 20     ROOT • 8.8647371375389E+01
A • 0.30 L • 13 N • 21     ROOT • 9.2738571375389E+01
A • 0.30 L • 13 N • 22     ROOT • 9.7485518370046E+01
A • 0.30 L • 13 N • 23     ROOT • 1.0182745105551E+02
A • 0.30 L • 13 N • 24     ROOT • 1.06361728841E+02
A • 0.30 L • 13 N • 25     ROOT • 1.1054757253303E+02
A • 0.30 L • 13 N • 26     ROOT • 1.1492286877669E+02
A • 0.30 L • 13 N • 27     ROOT • 1.20000000000E+02
A • 0.30 L • 13 N • 28     ROOT • 1.2369832320620E+02
A • 0.30 L • 13 N • 29     ROOT • 1.2895671727183E+02
A • 0.30 L • 13 N • 30     ROOT • 1.3258124841750E+02

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1 ROOTS OF EQUATION 3
A • 0.30 L • 14 N • 1      ROOT • 1.6360673749374E+01
A • 0.30 L • 14 N • 2      ROOT • 2.1537128269592E+01
A • 0.30 L • 14 N • 3      ROOT • 2.5561668542841E+01
A • 0.30 L • 14 N • 4      ROOT • 2.9278614361877E+01
A • 0.30 L • 14 N • 5      ROOT • 3.2990318729164E+01
A • 0.30 L • 14 N • 6      ROOT • 3.6294857128841E+01
A • 0.30 L • 14 N • 7      ROOT • 3.96524496560243E+01
A • 0.30 L • 14 N • 8      ROOT • 4.30160882180888E+01
A • 0.30 L • 14 N • 9      ROOT • 4.6010782180888E+01
A • 0.30 L • 14 N • 10     ROOT • 4.925879763772E+01
A • 0.30 L • 14 N • 11     ROOT • 5.25900000000E+01
A • 0.30 L • 14 N • 12     ROOT • 5.6487946229762E+01
A • 0.30 L • 14 N • 13     ROOT • 6.0363818374258E+01
A • 0.30 L • 14 N • 14     ROOT • 6.424463129164E+01
A • 0.30 L • 14 N • 15     ROOT • 6.8043643129164E+01
A • 0.30 L • 14 N • 16     ROOT • 7.2521670837244E+01
A • 0.30 L • 14 N • 17     ROOT • 7.680559287630E+01
A • 0.30 L • 14 N • 18     ROOT • 8.188608827630E+01
A • 0.30 L • 14 N • 19     ROOT • 8.5125431853496E+01
A • 0.30 L • 14 N • 20     ROOT • 8.92878230000E+01
A • 0.30 L • 14 N • 21     ROOT • 9.327864196E+01
A • 0.30 L • 14 N • 22     ROOT • 9.7974713720916E+01
A • 0.30 L • 14 N • 23     ROOT • 1.0229486886895E+02
A • 0.30 L • 14 N • 24     ROOT • 1.0697660445242E+02
A • 0.30 L • 14 N • 25     ROOT • 1.1097660445371E+02
A • 0.30 L • 14 N • 26     ROOT • 1.1503586445295E+02
A • 0.30 L • 14 N • 27     ROOT • 1.1974865242562E+02
A • 0.30 L • 14 N • 28     ROOT • 1.2408036125988E+02
A • 0.30 L • 14 N • 29     ROOT • 1.2846529344628E+02
A • 0.30 L • 14 N • 30     ROOT • 1.3289127650517E+02

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1 ROOTS OF EQUATION 3
A + 8.38 L * 15 N * 1      ROOT = 1.748033882879E+01
A + 8.38 L * 15 N * 2      ROOT = 2.622403418541E+01
A + 8.38 L * 15 N * 3      ROOT = 2.673517698822E+01
A + 8.38 L * 15 N * 4      ROOT = 3.081737715393E+01
A + 8.38 L * 15 N * 5      ROOT = 3.756368946141E+01
A + 8.38 L * 15 N * 6      ROOT = 4.095568949710E+01
A + 8.38 L * 15 N * 7      ROOT = 4.095568949710E+01
A + 8.38 L * 15 N * 8      ROOT = 4.743173275724E+01
A + 8.38 L * 15 N * 9      ROOT = 5.085865639538E+01
A + 8.38 L * 15 N * 10     ROOT = 5.085865639538E+01
A + 8.38 L * 15 N * 11     ROOT = 5.7513348251025E+01
A + 8.38 L * 15 N * 12     ROOT = 5.7513348251025E+01
A + 8.38 L * 15 N * 13     ROOT = 6.1287862651932E+01
A + 8.38 L * 15 N * 14     ROOT = 6.1287862651932E+01
A + 8.38 L * 15 N * 15     ROOT = 6.9186258276825E+01
A + 8.38 L * 15 N * 16     ROOT = 7.3251209622817E+01
A + 8.38 L * 15 N * 17     ROOT = 7.3251209622817E+01
A + 8.38 L * 15 N * 18     ROOT = 8.1534342865106E+01
A + 8.38 L * 15 N * 19     ROOT = 8.57341863985265E+01
A + 8.38 L * 15 N * 20     ROOT = 8.57341863985265E+01
A + 8.38 L * 15 N * 21     ROOT = 9.3220187536294E+01
A + 8.38 L * 15 N * 22     ROOT = 9.8497985434472E+01
A + 8.38 L * 15 N * 23     ROOT = 9.8497985434472E+01
A + 8.38 L * 15 N * 24     ROOT = 1.0710796395553E+02
A + 8.38 L * 15 N * 25     ROOT = 1.1143561783046E+02
A + 8.38 L * 15 N * 26     ROOT = 1.1143561783046E+02
A + 8.38 L * 15 N * 27     ROOT = 1.2012757761343E+02
A + 8.38 L * 15 N * 28     ROOT = 1.2448918736216E+02
A + 8.38 L * 15 N * 29     ROOT = 1.2865973986499E+02
A + 8.38 L * 15 N * 30     ROOT = 1.3123831796203E+02

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1 ROOTS OF EQUATION 3
A + 8.48 L * 1 N * 1      ROOT = 1.9384438265842E+00
A + 8.48 L * 1 N * 2      ROOT = 6.153894312312E+00
A + 8.48 L * 1 N * 3      ROOT = 1.09515272324713E+01
A + 8.48 L * 1 N * 4      ROOT = 1.10515272324713E+01
A + 8.48 L * 1 N * 5      ROOT = 2.1183342929283E+01
A + 8.48 L * 1 N * 6      ROOT = 2.63712985422716E+01
A + 8.48 L * 1 N * 7      ROOT = 2.63712985422716E+01
A + 8.48 L * 1 N * 8      ROOT = 3.678847532211E+01
A + 8.48 L * 1 N * 9      ROOT = 4.2697365256357E+01
A + 8.48 L * 1 N * 10     ROOT = 4.2697365256357E+01
A + 8.48 L * 1 N * 11     ROOT = 5.2455421112288E+01
A + 8.48 L * 1 N * 12     ROOT = 5.6827153248598E+01
A + 8.48 L * 1 N * 13     ROOT = 5.6827153248598E+01
A + 8.48 L * 1 N * 14     ROOT = 6.8141320289171E+01
A + 8.48 L * 1 N * 15     ROOT = 7.3372056575948E+01
A + 8.48 L * 1 N * 16     ROOT = 7.3372056575948E+01
A + 8.48 L * 1 N * 17     ROOT = 9.3835499796119E+01
A + 8.48 L * 1 N * 18     ROOT = 8.98679474781647E+01
A + 8.48 L * 1 N * 19     ROOT = 9.3835499796119E+01
A + 8.48 L * 1 N * 20     ROOT = 9.3835499796119E+01
A + 8.48 L * 1 N * 21     ROOT = 1.04767509889139E+02
A + 8.48 L * 1 N * 22     ROOT = 1.12042211399623E+02
A + 8.48 L * 1 N * 23     ROOT = 1.523151399623E+02
A + 8.48 L * 1 N * 24     ROOT = 1.2046924133667E+02
A + 8.48 L * 1 N * 25     ROOT = 1.2046924133667E+02
A + 8.48 L * 1 N * 26     ROOT = 1.3853789326826E+02
A + 8.48 L * 1 N * 27     ROOT = 1.3617241267796E+02
A + 8.48 L * 1 N * 28     ROOT = 1.4149741261948E+02
A + 8.48 L * 1 N * 29     ROOT = 1.4149741261948E+02
A + 8.48 L * 1 N * 30     ROOT = 1.5187657566654E+02

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1 ROOTS OF EQUATION 3
A = 0..40 L = 3 N = 1      ROOT = 3.2575286812941E+00
A = 0..40 L = 3 N = 2      ROOT = 3.88271294321E+00
A = 0..40 L = 3 N = 3      ROOT = 1.1448967569733E+01
A = 0..40 L = 3 N = 4      ROOT = 1.4252395298253E+01
A = 0..40 L = 3 N = 5      ROOT = 2.6563944826967E+01
A = 0..40 L = 3 N = 6      ROOT = 3.0535492771552E+01
A = 0..40 L = 3 N = 7      ROOT = 4.693497771552E+01
A = 0..40 L = 3 N = 8      ROOT = 4.21271451713403E+01
A = 0..40 L = 3 N = 9      ROOT = 4.21364125041353E+01
A = 0..40 L = 3 N = 10     ROOT = 2.51271451713403E+01
A = 0..40 L = 3 N = 11     ROOT = 5.7769686840654E+01
A = 0..40 L = 3 N = 12     ROOT = 6.2919168676105E+01
A = 0..40 L = 3 N = 13     ROOT = 7.1401482128959E+01
A = 0..40 L = 3 N = 14     ROOT = 7.344013424771E+01
A = 0..40 L = 3 N = 15     ROOT = 7.8657216548952E+01
A = 0..40 L = 3 N = 16     ROOT = 1.0725138323726E+01
A = 0..40 L = 3 N = 17     ROOT = 8.9124198398769E+01
A = 0..40 L = 3 N = 18     ROOT = 9.4353529319210E+01
A = 0..40 L = 3 N = 19     ROOT = 1.048528120593E+02
A = 0..40 L = 3 N = 20     ROOT = 1.048528120593E+02
A = 0..40 L = 3 N = 21     ROOT = 1.048528120593E+02
A = 0..40 L = 3 N = 22     ROOT = 1.1894671717442E+02
A = 0..40 L = 3 N = 23     ROOT = 1.2051672753911E+02
A = 0..40 L = 3 N = 24     ROOT = 1.2574330279681E+02
A = 0..40 L = 3 N = 25     ROOT = 1.3628915287310E+02
A = 0..40 L = 3 N = 26     ROOT = 1.3628915287310E+02
A = 0..40 L = 3 N = 27     ROOT = 1.4144241841781E+02
A = 0..40 L = 3 N = 28     ROOT = 1.4667587821352E+02
A = 0..40 L = 3 N = 29     ROOT = 1.51958971331895E+02

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1 ROOTS OF EQUATION 3
A = 0..40 L = 3 N = 1      ROOT = 4.4771917181613E+00
A = 0..40 L = 3 N = 2      ROOT = 8.27146600041E+00
A = 0..40 L = 3 N = 3      ROOT = 1.75138323726E+01
A = 0..40 L = 3 N = 4      ROOT = 1.6835631947098E+01
A = 0..40 L = 3 N = 5      ROOT = 2.1785393302536E+01
A = 0..40 L = 3 N = 6      ROOT = 2.1785393302536E+01
A = 0..40 L = 3 N = 7      ROOT = 3.1974682147677E+01
A = 0..40 L = 3 N = 8      ROOT = 3.7130450000841E+01
A = 0..40 L = 3 N = 9      ROOT = 4.7495750249384E+01
A = 0..40 L = 3 N = 10     ROOT = 5.2694465464792E+01
A = 0..40 L = 3 N = 11     ROOT = 6.110583167981E+01
A = 0..40 L = 3 N = 12     ROOT = 6.3110583167981E+01
A = 0..40 L = 3 N = 13     ROOT = 6.8325181316589E+01
A = 0..40 L = 3 N = 14     ROOT = 6.8325181316589E+01
A = 0..40 L = 3 N = 15     ROOT = 7.8762739805329E+01
A = 0..40 L = 3 N = 16     ROOT = 8.398478267592E+01
A = 0..40 L = 3 N = 17     ROOT = 8.398478267592E+01
A = 0..40 L = 3 N = 18     ROOT = 9.4433521981594E+01
A = 0..40 L = 3 N = 19     ROOT = 9.4433521981594E+01
A = 0..40 L = 3 N = 20     ROOT = 1.08027261326E+02
A = 0..40 L = 3 N = 21     ROOT = 1.08027261326E+02
A = 0..40 L = 3 N = 22     ROOT = 1.08114936511389E+02
A = 0..40 L = 3 N = 23     ROOT = 1.1534368469295E+02
A = 0..40 L = 3 N = 24     ROOT = 1.1534368469295E+02
A = 0..40 L = 3 N = 25     ROOT = 1.2890292619326E+02
A = 0..40 L = 3 N = 26     ROOT = 1.31033406596177E+02
A = 0..40 L = 3 N = 27     ROOT = 1.36261306596177E+02
A = 0..40 L = 3 N = 28     ROOT = 1.4672703967389E+02
A = 0..40 L = 3 N = 29     ROOT = 1.4672703967389E+02
A = 0..40 L = 3 N = 30     ROOT = 1.51958971331895E+02

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1 ROOTS OF EQUATION 3

```

R * 0.40 L = 4 N = 1      ROOT = 5.632493698888E+00
R * 0.40 L = 4 N = 2      ROOT = 9.579535616879E+00
R * 0.40 L = 4 N = 3      ROOT = 1.311898592589E+01
R * 0.40 L = 4 N = 4      ROOT = 1.747028118871E+01
R * 0.40 L = 4 N = 5      ROOT = 2.2266857912334E+01
R * 0.40 L = 4 N = 6      ROOT = 2.7311898559266E+01
R * 0.40 L = 4 N = 7      ROOT = 3.236446373944E+01
R * 0.40 L = 4 N = 8      ROOT = 3.7462598637294E+01
R * 0.40 L = 4 N = 9      ROOT = 4.2544633954493E+01
R * 0.40 L = 4 N = 10     ROOT = 4.762293574493E+01
R * 0.40 L = 4 N = 11     ROOT = 5.285179634856E+01
R * 0.40 L = 4 N = 12     ROOT = 5.8073393473165E+01
R * 0.40 L = 4 N = 13     ROOT = 6.3291188322813E+01
R * 0.40 L = 4 N = 14     ROOT = 6.8471883228133E+01
R * 0.40 L = 4 N = 15     ROOT = 7.36798005935389E+01
R * 0.40 L = 4 N = 16     ROOT = 7.88700000000000E+01
R * 0.40 L = 4 N = 17     ROOT = 8.4046776145889E+01
R * 0.40 L = 4 N = 18     ROOT = 8.93287530845498E+01
R * 0.40 L = 4 N = 19     ROOT = 9.45065530845498E+01
R * 0.40 L = 4 N = 20     ROOT = 9.976293577423E+01
R * 0.40 L = 4 N = 21     ROOT = 1.04962336537788E+02
R * 0.40 L = 4 N = 22     ROOT = 1.10820000000000E+02
R * 0.40 L = 4 N = 23     ROOT = 1.166845971840E+02
R * 0.40 L = 4 N = 24     ROOT = 1.2065607603935E+02
R * 0.40 L = 4 N = 25     ROOT = 1.24632000000000E+02
R * 0.40 L = 4 N = 26     ROOT = 1.3118978217278E+02
R * 0.40 L = 4 N = 27     ROOT = 1.3633768931156E+02
R * 0.40 L = 4 N = 28     ROOT = 1.4156763501000E+02
R * 0.40 L = 4 N = 29     ROOT = 1.46800000000000E+02
R * 0.40 L = 4 N = 30     ROOT = 1.5203475460755E+02

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1 ROOTS OF EQUATION 3

```

R * 0.40 L = 5 N = 1      ROOT = 6.7513623516615E+00
R * 0.40 L = 5 N = 2      ROOT = 9.09389840000000E+00
R * 0.40 L = 5 N = 3      ROOT = 1.423509869731E+01
R * 0.40 L = 5 N = 4      ROOT = 1.8252177966978E+01
R * 0.40 L = 5 N = 5      ROOT = 2.2266857912334E+01
R * 0.40 L = 5 N = 6      ROOT = 2.770347787965E+01
R * 0.40 L = 5 N = 7      ROOT = 3.2686023994192E+01
R * 0.40 L = 5 N = 8      ROOT = 3.77122800000000E+01
R * 0.40 L = 5 N = 9      ROOT = 4.2841228172725E+01
R * 0.40 L = 5 N = 10     ROOT = 4.7971536138983E+01
R * 0.40 L = 5 N = 11     ROOT = 5.31020000000000E+01
R * 0.40 L = 5 N = 12     ROOT = 5.8289675462725E+01
R * 0.40 L = 5 N = 13     ROOT = 6.34679336368428E+01
R * 0.40 L = 5 N = 14     ROOT = 6.8653592050083E+01
R * 0.40 L = 5 N = 15     ROOT = 7.3851530357481E+01
R * 0.40 L = 5 N = 16     ROOT = 7.9046828269709E+01
R * 0.40 L = 5 N = 17     ROOT = 8.425383330374E+01
R * 0.40 L = 5 N = 18     ROOT = 8.94460000000000E+01
R * 0.40 L = 5 N = 19     ROOT = 9.4672025537166E+01
R * 0.40 L = 5 N = 20     ROOT = 9.9685760218319E+01
R * 0.40 L = 5 N = 21     ROOT = 1.04702000000000E+02
R * 0.40 L = 5 N = 22     ROOT = 1.1031941916193E+02
R * 0.40 L = 5 N = 23     ROOT = 1.153388495523E+02
R * 0.40 L = 5 N = 24     ROOT = 1.20360000000000E+02
R * 0.40 L = 5 N = 25     ROOT = 1.2598194423678E+02
R * 0.40 L = 5 N = 26     ROOT = 1.3126528776226E+02
R * 0.40 L = 5 N = 27     ROOT = 1.3633768931156E+02
R * 0.40 L = 5 N = 28     ROOT = 1.4156763501000E+02
R * 0.40 L = 5 N = 29     ROOT = 1.46800000000000E+02
R * 0.40 L = 5 N = 30     ROOT = 1.521673261772E+02

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1 ROOTS OF EQUATION 3
R = 0.20 L = 9 N = 1      ROOT = 1.0016370743273E+01
R = 0.20 L = 9 N = 2      ROOT = 1.4651261986639E+01
R = 0.20 L = 9 N = 3      ROOT = 1.835626265685E+01
R = 0.20 L = 9 N = 4      ROOT = 2.1336262631763E+01
R = 0.20 L = 9 N = 5      ROOT = 2.5216123618093E+01
R = 0.20 L = 9 N = 6      ROOT = 2.89215176959E+01
R = 0.20 L = 9 N = 7      ROOT = 3.26272351618E+01
R = 0.20 L = 9 N = 8      ROOT = 3.4934187699685E+01
R = 0.20 L = 9 N = 9      ROOT = 3.801955359495E+01
R = 0.20 L = 9 N = 10     ROOT = 4.0481955359495E+01
R = 0.20 L = 9 N = 11     ROOT = 4.4364234534022E+01
R = 0.20 L = 9 N = 12     ROOT = 4.7738062394546E+01
R = 0.20 L = 9 N = 13     ROOT = 5.088338133048E+01
R = 0.20 L = 9 N = 14     ROOT = 5.4794517314925E+01
R = 0.20 L = 9 N = 15     ROOT = 5.84293913021657E+01
R = 0.20 L = 9 N = 16     ROOT = 6.18624078270E+01
R = 0.20 L = 9 N = 17     ROOT = 6.5026424078270E+01
R = 0.20 L = 9 N = 18     ROOT = 6.9565572442876E+01
R = 0.20 L = 9 N = 19     ROOT = 7.399192851618E+01
R = 0.20 L = 9 N = 20     ROOT = 7.7118248922527E+01
R = 0.20 L = 9 N = 21     ROOT = 8.0916811806797E+01
R = 0.20 L = 9 N = 22     ROOT = 8.4361130875495E+01
R = 0.20 L = 9 N = 23     ROOT = 8.8550441389689E+01
R = 0.20 L = 9 N = 24     ROOT = 9.2382124948817E+01
R = 0.20 L = 9 N = 25     ROOT = 9.6019361964881E+01
R = 0.20 L = 9 N = 26     ROOT = 9.988689184352E+02
R = 0.20 L = 9 N = 27     ROOT = 1.039222726673E+02
R = 0.20 L = 9 N = 28     ROOT = 1.0741113057495E+02
R = 0.20 L = 9 N = 29     ROOT = 1.1162019438495E+02
R = 0.20 L = 9 N = 30     ROOT = 1.1551317955393E+02

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1 ROOTS OF EQUATION 3
R = 0.20 L = 9 N = 1      ROOT = 1.1075418188691E+01
R = 0.20 L = 9 N = 2      ROOT = 1.5912121534255E+01
R = 0.20 L = 9 N = 3      ROOT = 1.95818531310E+01
R = 0.20 L = 9 N = 4      ROOT = 2.3106595940438E+01
R = 0.20 L = 9 N = 5      ROOT = 2.677044404381E+01
R = 0.20 L = 9 N = 6      ROOT = 2.9856201843481E+01
R = 0.20 L = 9 N = 7      ROOT = 3.3144057858035E+01
R = 0.20 L = 9 N = 8      ROOT = 3.6322851758035E+01
R = 0.20 L = 9 N = 9      ROOT = 3.9541853354175E+01
R = 0.20 L = 9 N = 10     ROOT = 4.264119452486E+01
R = 0.20 L = 9 N = 11     ROOT = 4.574226126582E+01
R = 0.20 L = 9 N = 12     ROOT = 4.8949448126959E+01
R = 0.20 L = 9 N = 13     ROOT = 5.229217597479E+01
R = 0.20 L = 9 N = 14     ROOT = 5.5634447128479E+01
R = 0.20 L = 9 N = 15     ROOT = 5.9300192912847E+01
R = 0.20 L = 9 N = 16     ROOT = 6.2910944797560E+01
R = 0.20 L = 9 N = 17     ROOT = 6.6578521045841E+01
R = 0.20 L = 9 N = 18     ROOT = 7.0261268924389E+01
R = 0.20 L = 9 N = 19     ROOT = 7.3986493376911E+01
R = 0.20 L = 9 N = 20     ROOT = 7.7710912565682E+01
R = 0.20 L = 9 N = 21     ROOT = 8.1499192851618E+01
R = 0.20 L = 9 N = 22     ROOT = 8.5281496376967E+01
R = 0.20 L = 9 N = 23     ROOT = 8.9877622865487E+01
R = 0.20 L = 9 N = 24     ROOT = 9.4565312512847E+01
R = 0.20 L = 9 N = 25     ROOT = 9.6703891159915E+01
R = 0.20 L = 9 N = 26     ROOT = 1.0053113772513E+02
R = 0.20 L = 9 N = 27     ROOT = 1.0428036897134E+02
R = 0.20 L = 9 N = 28     ROOT = 1.0820836897134E+02
R = 0.20 L = 9 N = 29     ROOT = 1.1285666334232E+02
R = 0.20 L = 9 N = 30     ROOT = 1.1591848921340E+02

```

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## 1 ROOTS OF EQUATION 3

```

R • 0.20 L • 10 N • 1
R • 0.20 L • 10 N • 2
R • 0.20 L • 10 N • 3
R • 0.20 L • 10 N • 4
R • 0.20 L • 10 N • 5
R • 0.20 L • 10 N • 6
R • 0.20 L • 10 N • 7
R • 0.20 L • 10 N • 8
R • 0.20 L • 10 N • 9
R • 0.20 L • 10 N • 10
R • 0.20 L • 10 N • 11
R • 0.20 L • 10 N • 12
R • 0.20 L • 10 N • 13
R • 0.20 L • 10 N • 14
R • 0.20 L • 10 N • 15
R • 0.20 L • 10 N • 16
R • 0.20 L • 10 N • 17
R • 0.20 L • 10 N • 18
R • 0.20 L • 10 N • 19
R • 0.20 L • 10 N • 20
R • 0.20 L • 10 N • 21
R • 0.20 L • 10 N • 22
R • 0.20 L • 10 N • 23
R • 0.20 L • 10 N • 24
R • 0.20 L • 10 N • 25
R • 0.20 L • 10 N • 26
R • 0.20 L • 10 N • 27
R • 0.20 L • 10 N • 28
R • 0.20 L • 10 N • 29
R • 0.20 L • 10 N • 30

```

ROOT • -1.2143264188921E+01  
 ROOT • 1.69775499565650E+01  
 ROOT • 2.0729556730823E+01  
 ROOT • 2.450175535964E+01  
 ROOT • 2.788177959648E+01  
 ROOT • 3.1165943714533E+01  
 ROOT • 3.450001595648E+01  
 ROOT • 3.7760191569396E+01  
 ROOT • 4.098641558395E+01  
 ROOT • 4.4270001562110E+01  
 ROOT • 4.7251164358165E+01  
 ROOT • 5.03564845969656E+01  
 ROOT • 5.3538560156210E+01  
 ROOT • 5.685853687676E+01  
 ROOT • 6.0294049216265E+01  
 ROOT • 6.373455156210E+01  
 ROOT • 6.74052365846926E+01  
 ROOT • 7.1041733820168E+01  
 ROOT • 7.454550973729E+01  
 ROOT • 7.8426278413322E+01  
 ROOT • 8.2149166574337E+01  
 ROOT • 8.5750000000000E+01  
 ROOT • 8.9665867284574E+01  
 ROOT • 9.3446378685625E+01  
 ROOT • 9.7322500000000E+01  
 ROOT • 1.0184558973729E+02  
 ROOT • 1.0486029823916E+02  
 ROOT • 1.0803616521107E+02  
 ROOT • 1.12511621107E+02  
 ROOT • 1.163523529330E+02

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## 1 ROOTS OF EQUATION 3

```

R • 0.20 L • 11 N • 1
R • 0.20 L • 11 N • 2
R • 0.20 L • 11 N • 3
R • 0.20 L • 11 N • 4
R • 0.20 L • 11 N • 5
R • 0.20 L • 11 N • 6
R • 0.20 L • 11 N • 7
R • 0.20 L • 11 N • 8
R • 0.20 L • 11 N • 9
R • 0.20 L • 11 N • 10
R • 0.20 L • 11 N • 11
R • 0.20 L • 11 N • 12
R • 0.20 L • 11 N • 13
R • 0.20 L • 11 N • 14
R • 0.20 L • 11 N • 15
R • 0.20 L • 11 N • 16
R • 0.20 L • 11 N • 17
R • 0.20 L • 11 N • 18
R • 0.20 L • 11 N • 19
R • 0.20 L • 11 N • 20
R • 0.20 L • 11 N • 21
R • 0.20 L • 11 N • 22
R • 0.20 L • 11 N • 23
R • 0.20 L • 11 N • 24
R • 0.20 L • 11 N • 25
R • 0.20 L • 11 N • 26
R • 0.20 L • 11 N • 27
R • 0.20 L • 11 N • 28
R • 0.20 L • 11 N • 29
R • 0.20 L • 11 N • 30

```

ROOT • 1.3392629196926E+01  
 ROOT • 1.5123254893930E+01  
 ROOT • 2.1999355915998E+01  
 ROOT • 2.5604055119905E+01  
 ROOT • 2.9250000000000E+01  
 ROOT • 3.24684748222E+01  
 ROOT • 3.5088378939323E+01  
 ROOT • 3.7719578581265E+01  
 ROOT • 4.2105272916210E+01  
 ROOT • 4.5594509596857E+01  
 ROOT • 4.829455986564E+01  
 ROOT • 5.196152146383E+01  
 ROOT • 5.4957981030165E+01  
 ROOT • 5.8132763853855E+01  
 ROOT • 6.1327638535192E+01  
 ROOT • 6.4843283610130E+01  
 ROOT • 6.8344663936535E+01  
 ROOT • 7.1883403348304E+01  
 ROOT • 7.5326972154938E+01  
 ROOT • 7.918218096938E+01  
 ROOT • 8.2942333333333E+01  
 ROOT • 8.6586467817622E+01  
 ROOT • 9.0313753725294E+01  
 ROOT • 9.4080808080808E+01  
 ROOT • 9.7832103118549E+01  
 ROOT • 1.0161252638148E+02  
 ROOT • 1.0538600000000E+02  
 ROOT • 1.0920725362835E+02  
 ROOT • 1.1301984354293E+02  
 ROOT • 1.1683897234259E+02

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1 ROOTS OF EQUATION 3
R = 0.20 L = 14 N = 1
ROOT = 1.6366673748457E+01
R = 0.20 L = 14 N = 2
ROOT = 2.1537128330218E+01
R = 0.20 L = 14 N = 3
ROOT = 2.7262457311631E+01
R = 0.20 L = 14 N = 4
ROOT = 3.278731654652E+01
R = 0.20 L = 14 N = 5
ROOT = 3.839775645169E+01
R = 0.20 L = 14 N = 6
ROOT = 4.319981654652E+01
R = 0.20 L = 14 N = 7
ROOT = 4.786731654652E+01
R = 0.20 L = 14 N = 8
ROOT = 5.2586515134856E+01
R = 0.20 L = 14 N = 9
ROOT = 5.638857154797E+01
R = 0.20 L = 14 N = 10
ROOT = 6.010021821052E+01
R = 0.20 L = 14 N = 11
ROOT = 6.2956537845198E+01
R = 0.20 L = 14 N = 12
ROOT = 6.6203175476136E+01
R = 0.20 L = 14 N = 13
ROOT = 6.98571875476136E+01
R = 0.20 L = 14 N = 14
ROOT = 7.2581584465759E+01
R = 0.20 L = 14 N = 15
ROOT = 7.5694476238755E+01
R = 0.20 L = 14 N = 16
ROOT = 7.8660000000000E+01
R = 0.20 L = 14 N = 17
ROOT = 7.1930183871826E+01
R = 0.20 L = 14 N = 18
ROOT = 7.5174947898355E+01
R = 0.20 L = 14 N = 19
ROOT = 7.8219821898355E+01
R = 0.20 L = 14 N = 20
ROOT = 8.19686752309399E+01
R = 0.20 L = 14 N = 21
ROOT = 8.5478452653892E+01
R = 0.20 L = 14 N = 22
ROOT = 8.8886672653892E+01
R = 0.20 L = 14 N = 23
ROOT = 9.261325062532E+01
R = 0.20 L = 14 N = 24
ROOT = 9.628256160595E+01
R = 0.20 L = 14 N = 25
ROOT = 9.936710913716E+01
R = 0.20 L = 14 N = 26
ROOT = 1.0363710913716E+02
R = 0.20 L = 14 N = 27
ROOT = 1.0734630292519E+02
R = 0.20 L = 14 N = 28
ROOT = 1.1107726396048E+02
R = 0.20 L = 14 N = 29
ROOT = 1.1484946480741E+02
R = 0.20 L = 14 N = 30
ROOT = 1.1857946480741E+02

```

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1 ROOTS OF EQUATION 3
R = 0.20 L = 15 N = 1
ROOT = 1.74088338803057E+01
R = 0.20 L = 15 N = 2
ROOT = 2.2662457434362E+01
R = 0.20 L = 15 N = 3
ROOT = 2.8000000000000E+01
R = 0.20 L = 15 N = 4
ROOT = 3.0488001947323E+01
R = 0.20 L = 15 N = 5
ROOT = 3.40778676591305E+01
R = 0.20 L = 15 N = 6
ROOT = 3.7666666666667E+01
R = 0.20 L = 15 N = 7
ROOT = 4.0998925756453E+01
R = 0.20 L = 15 N = 8
ROOT = 4.435642567145E+01
R = 0.20 L = 15 N = 9
ROOT = 4.7714444444444E+01
R = 0.20 L = 15 N = 10
ROOT = 5.1014697493519E+01
R = 0.20 L = 15 N = 11
ROOT = 5.4382646665512E+01
R = 0.20 L = 15 N = 12
ROOT = 5.7659226339954E+01
R = 0.20 L = 15 N = 13
ROOT = 6.0811254533649E+01
R = 0.20 L = 15 N = 14
ROOT = 6.4022726491512E+01
R = 0.20 L = 15 N = 15
ROOT = 6.7233333333333E+01
R = 0.20 L = 15 N = 16
ROOT = 7.0387295371338E+01
R = 0.20 L = 15 N = 17
ROOT = 7.339861686291E+01
R = 0.20 L = 15 N = 18
ROOT = 7.652143193665E+01
R = 0.20 L = 15 N = 19
ROOT = 7.964474193665E+01
R = 0.20 L = 15 N = 20
ROOT = 8.30982469339954E+01
R = 0.20 L = 15 N = 21
ROOT = 8.62579226339954E+01
R = 0.20 L = 15 N = 22
ROOT = 8.94244722633995E+01
R = 0.20 L = 15 N = 23
ROOT = 9.3561056263974E+01
R = 0.20 L = 15 N = 24
ROOT = 9.76496464646464E+01
R = 0.20 L = 15 N = 25
ROOT = 1.0080000000000E+02
R = 0.20 L = 15 N = 26
ROOT = 1.04423935356732E+02
R = 0.20 L = 15 N = 27
ROOT = 1.0800000000000E+02
R = 0.20 L = 15 N = 28
ROOT = 1.11559767322471E+02
R = 0.20 L = 15 N = 29
ROOT = 1.15509767322471E+02
R = 0.20 L = 15 N = 30
ROOT = 1.1923973817589E+02

```

30

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1 ROOTS OF EQUATION 3
R = 0.38 L = 1 N = 1
ROOT = 2.0061911513759E+00
R = 0.38 L = 1 N = 2
ROOT = 5.8159967819125E+00
R = 0.38 L = 1 N = 3
ROOT = 9.7235952285272E+00
R = 0.38 L = 1 N = 4
ROOT = 1.4008500000000E+01
R = 0.38 L = 1 N = 5
ROOT = 1.8326499640403E+01
R = 0.38 L = 1 N = 6
ROOT = 2.2738811370594E+01
R = 0.38 L = 1 N = 7
ROOT = 2.6880000000000E+01
R = 0.38 L = 1 N = 8
ROOT = 3.1628843899099E+01
R = 0.38 L = 1 N = 9
ROOT = 3.6899693725157E+01
R = 0.38 L = 1 N = 10
ROOT = 4.2080000000000E+01
R = 0.38 L = 1 N = 11
ROOT = 4.528653514801E+01
R = 0.38 L = 1 N = 12
ROOT = 4.9503118866974E+01
R = 0.38 L = 1 N = 13
ROOT = 5.3400000000000E+01
R = 0.38 L = 1 N = 14
ROOT = 5.8456247493087E+01
R = 0.38 L = 1 N = 15
ROOT = 6.2938651707341E+01
R = 0.38 L = 1 N = 16
ROOT = 6.6700000000000E+01
R = 0.38 L = 1 N = 17
ROOT = 7.09067366811E+01
R = 0.38 L = 1 N = 18
ROOT = 7.6381254441677E+01
R = 0.38 L = 1 N = 19
ROOT = 8.083861145225E+01
R = 0.38 L = 1 N = 20
ROOT = 8.4580000000000E+01
R = 0.38 L = 1 N = 21
ROOT = 8.834095496760E+01
R = 0.38 L = 1 N = 22
ROOT = 9.4318543748965E+01
R = 0.38 L = 1 N = 23
ROOT = 9.9800000000000E+01
R = 0.38 L = 1 N = 24
ROOT = 1.0328836546767E+02
R = 0.38 L = 1 N = 25
ROOT = 1.0782366929563E+02
R = 0.38 L = 1 N = 26
ROOT = 1.1222000000000E+02
R = 0.38 L = 1 N = 27
ROOT = 1.1674487486541E+02
R = 0.38 L = 1 N = 28
ROOT = 1.2123874657836E+02
R = 0.38 L = 1 N = 29
ROOT = 1.2574493158643E+02
R = 0.38 L = 1 N = 30
ROOT = 1.3028328840495E+02

```

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```

1 ROOTS OF EQUATION 3
R = 0.38 L = 2 N = 1
ROOT = 3.3177341592459E+00
R = 0.38 L = 2 N = 2
ROOT = 7.0558078142883E+00
R = 0.38 L = 2 N = 3
ROOT = 1.0528111810433E+01
R = 0.38 L = 2 N = 4
ROOT = 1.3500000000000E+01
R = 0.38 L = 2 N = 5
ROOT = 1.6712595864339E+01
R = 0.38 L = 2 N = 6
ROOT = 2.0043725621610E+01
R = 0.38 L = 2 N = 7
ROOT = 2.3400000000000E+01
R = 0.38 L = 2 N = 8
ROOT = 3.1843942889546E+01
R = 0.38 L = 2 N = 9
ROOT = 3.6277705149643E+01
R = 0.38 L = 2 N = 10
ROOT = 4.1000000000000E+01
R = 0.38 L = 2 N = 11
ROOT = 5.1782314695716E+01
R = 0.38 L = 2 N = 12
ROOT = 4.963896527119E+01
R = 0.38 L = 2 N = 13
ROOT = 5.4695200000000E+01
R = 0.38 L = 2 N = 14
ROOT = 6.05264917939E+01
R = 0.38 L = 2 N = 15
ROOT = 6.3043517290739E+01
R = 0.38 L = 2 N = 16
ROOT = 6.5388114320580E+01
R = 0.38 L = 2 N = 17
ROOT = 6.9386114320580E+01
R = 0.38 L = 2 N = 18
ROOT = 7.6470835986370E+01
R = 0.38 L = 2 N = 19
ROOT = 8.0970973326255E+01
R = 0.38 L = 2 N = 20
ROOT = 8.4280000000000E+01
R = 0.38 L = 2 N = 21
ROOT = 8.9998492004621E+01
R = 0.38 L = 2 N = 22
ROOT = 9.4389386563516E+01
R = 0.38 L = 2 N = 23
ROOT = 9.8000000000000E+01
R = 0.38 L = 2 N = 24
ROOT = 1.0335383131359E+02
R = 0.38 L = 2 N = 25
ROOT = 1.0783562617595E+02
R = 0.38 L = 2 N = 26
ROOT = 1.1230000000000E+02
R = 0.38 L = 2 N = 27
ROOT = 1.1680266386680E+02
R = 0.38 L = 2 N = 28
ROOT = 1.2128581366712E+02
R = 0.38 L = 2 N = 29
ROOT = 1.2574493158643E+02
R = 0.38 L = 2 N = 30
ROOT = 1.3025413185249E+02

```

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```

    ROOTS OF EQUATION 3

A = 0.30 L = 3 N = 1          ROOT = 4.5078795557162E+00
A = 0.30 L = 3 N = 2          ROOT = 0.4479983859430E+00
A = 0.30 L = 3 N = 3          ROOT = 1.1694957926487E+01
A = 0.30 L = 3 N = 4          ROOT = 0.2808208000000E+01
A = 0.30 L = 3 N = 5          ROOT = 1.9291415652827E+01
A = 0.30 L = 3 N = 6          ROOT = 2.359815756414E+01
A = 0.30 L = 3 N = 7          ROOT = 2.7898520575641E+01
A = 0.30 L = 3 N = 8          ROOT = 3.2145860540762E+01
A = 0.30 L = 3 N = 9          ROOT = 3.6558575470389E+01
A = 0.30 L = 3 N = 10         ROOT = 4.0968385205754E+01
A = 0.30 L = 3 N = 11         ROOT = 4.5462209524073E+01
A = 0.30 L = 3 N = 12         ROOT = 4.9842326494486E+01
A = 0.30 L = 3 N = 13         ROOT = 5.4226073795238E+01
A = 0.30 L = 3 N = 14         ROOT = 5.8744873795238E+01
A = 0.30 L = 3 N = 15         ROOT = 6.3284078944865E+01
A = 0.30 L = 3 N = 16         ROOT = 6.778085159265E+01
A = 0.30 L = 3 N = 17         ROOT = 7.2133350159265E+01
A = 0.30 L = 3 N = 18         ROOT = 7.6693126822897E+01
A = 0.30 L = 3 N = 19         ROOT = 8.1258852482897E+01
A = 0.30 L = 3 N = 20         ROOT = 8.5845778476916E+01
A = 0.30 L = 3 N = 21         ROOT = 9.0420937834386E+01
A = 0.30 L = 3 N = 22         ROOT = 9.5000000000000E+01
A = 0.30 L = 3 N = 23         ROOT = 9.8972316513865E+01
A = 0.30 L = 3 N = 24         ROOT = 1.034499757197E+02
A = 0.30 L = 3 N = 25         ROOT = 1.0808549528486E+02
A = 0.30 L = 3 N = 26         ROOT = 1.1248787816000E+02
A = 0.30 L = 3 N = 27         ROOT = 1.1688782438952E+02
A = 0.30 L = 3 N = 28         ROOT = 1.2136839343282E+02
A = 0.30 L = 3 N = 29         ROOT = 1.2592673098139E+02
A = 0.30 L = 3 N = 30         ROOT = 1.303318695475E+02

```

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```

    ROOTS OF EQUATION 3

A = 0.30 L = 4 N = 1          ROOT = 5.643140948248E+00
A = 0.30 L = 4 N = 2          ROOT = 9.7841355126874E+00
A = 0.30 L = 4 N = 3          ROOT = 1.303326561499E+01
A = 0.30 L = 4 N = 4          ROOT = 1.6488085481710E+01
A = 0.30 L = 4 N = 5          ROOT = 2.0865433302591E+01
A = 0.30 L = 4 N = 6          ROOT = 2.4801895604615E+01
A = 0.30 L = 4 N = 7          ROOT = 2.8136213771741E+01
A = 0.30 L = 4 N = 8          ROOT = 3.2593963607615E+01
A = 0.30 L = 4 N = 9          ROOT = 3.63213771741E+01
A = 0.30 L = 4 N = 10         ROOT = 4.0118652482779E+01
A = 0.30 L = 4 N = 11         ROOT = 4.5780254837797E+01
A = 0.30 L = 4 N = 12         ROOT = 5.0113685481710E+01
A = 0.30 L = 4 N = 13         ROOT = 5.4417227227715E+01
A = 0.30 L = 4 N = 14         ROOT = 5.8973781216303E+01
A = 0.30 L = 4 N = 15         ROOT = 6.3416578238029E+01
A = 0.30 L = 4 N = 16         ROOT = 6.8000000000000E+01
A = 0.30 L = 4 N = 17         ROOT = 7.2319217802114E+01
A = 0.30 L = 4 N = 18         ROOT = 7.6772648132088E+01
A = 0.30 L = 4 N = 19         ROOT = 8.1258852482897E+01
A = 0.30 L = 4 N = 20         ROOT = 8.57823247595910E+01
A = 0.30 L = 4 N = 21         ROOT = 9.0168671779103E+01
A = 0.30 L = 4 N = 22         ROOT = 9.467227227715E+01
A = 0.30 L = 4 N = 23         ROOT = 9.9167417227715E+01
A = 0.30 L = 4 N = 24         ROOT = 1.03579322447768E+02
A = 0.30 L = 4 N = 25         ROOT = 1.0808549528486E+02
A = 0.30 L = 4 N = 26         ROOT = 1.1252673098139E+02
A = 0.30 L = 4 N = 27         ROOT = 1.1768212958309E+02
A = 0.30 L = 4 N = 28         ROOT = 1.22226889816E+02
A = 0.30 L = 4 N = 29         ROOT = 1.2695562791586E+02
A = 0.30 L = 4 N = 30         ROOT = 1.3843354199867E+02

```

```

ROOTS OF EQUATION 3
R = 0.30 L = 5 N = 1          ROOT = 6.7561598814486E+00
R = 0.30 L = 5 N = 2          ROOT = 1.1851167737156E+01
R = 0.30 L = 5 N = 3          ROOT = 1.7660436479162E+01
R = 0.30 L = 5 N = 4          ROOT = 2.1848165942585E+01
R = 0.30 L = 5 N = 5          ROOT = 2.8914952412631E+01
R = 0.30 L = 5 N = 6          ROOT = 3.1127868029449E+01
R = 0.30 L = 5 N = 7          ROOT = 3.4119576595916E+01
R = 0.30 L = 5 N = 8          ROOT = 4.1717704463704E+01
R = 0.30 L = 5 N = 9          ROOT = 5.8456827613695E+01
R = 0.30 L = 5 N = 10         ROOT = 6.4071942463869E+01
R = 0.30 L = 5 N = 11         ROOT = 5.9259444462847E+01
R = 0.30 L = 5 N = 12         ROOT = 6.3681813447595E+01
R = 0.30 L = 5 N = 13         ROOT = 6.8020511111111E+01
R = 0.30 L = 5 N = 14         ROOT = 7.255126463558E+01
R = 0.30 L = 5 N = 15         ROOT = 7.6995449988717E+01
R = 0.30 L = 5 N = 16         ROOT = 8.0333333333333E+01
R = 0.30 L = 5 N = 17         ROOT = 8.589766524534E+01
R = 0.30 L = 5 N = 18         ROOT = 9.035431928174E+01
R = 0.30 L = 5 N = 19         ROOT = 9.4811111111111E+01
R = 0.30 L = 5 N = 20         ROOT = 9.9276198078362E+01
R = 0.30 L = 5 N = 21         ROOT = 1.037466027793E+02
R = 0.30 L = 5 N = 22         ROOT = 1.1821111111111E+02
R = 0.30 L = 5 N = 23         ROOT = 1.1267525322521E+02
R = 0.30 L = 5 N = 24         ROOT = 1.171494012936E+02
R = 0.30 L = 5 N = 25         ROOT = 1.2167777777777E+02
R = 0.30 L = 5 N = 26         ROOT = 1.2688624061961E+02
R = 0.30 L = 5 N = 27         ROOT = 1.305615265409E+02

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ROOTS OF EQUATION 3
R = 0.30 L = 6 N = 1          ROOT = 7.8510190529826E+00
R = 0.30 L = 6 N = 2          ROOT = 1.0729111111111E+01
R = 0.30 L = 6 N = 3          ROOT = 1.5736616967266E+01
R = 0.30 L = 6 N = 4          ROOT = 1.9800829381330E+01
R = 0.30 L = 6 N = 5          ROOT = 2.3800000000000E+01
R = 0.30 L = 6 N = 6          ROOT = 2.574328575227E+01
R = 0.30 L = 6 N = 7          ROOT = 2.9688634880124E+01
R = 0.30 L = 6 N = 8          ROOT = 3.1627111111111E+01
R = 0.30 L = 6 N = 9          ROOT = 3.7954288818E+01
R = 0.30 L = 6 N = 10         ROOT = 4.2212451356304E+01
R = 0.30 L = 6 N = 11         ROOT = 4.651637839566E+01
R = 0.30 L = 6 N = 12         ROOT = 5.0818725715527E+01
R = 0.30 L = 6 N = 13         ROOT = 5.5218725715527E+01
R = 0.30 L = 6 N = 14         ROOT = 5.9601581162331E+01
R = 0.30 L = 6 N = 15         ROOT = 6.3711111111111E+01
R = 0.30 L = 6 N = 16         ROOT = 6.8495568598433E+01
R = 0.30 L = 6 N = 17         ROOT = 7.2829367972674E+01
R = 0.30 L = 6 N = 18         ROOT = 7.7000000000000E+01
R = 0.30 L = 6 N = 19         ROOT = 8.1691749192616E+01
R = 0.30 L = 6 N = 20         ROOT = 8.6131923565492E+01
R = 0.30 L = 6 N = 21         ROOT = 9.0631111111111E+01
R = 0.30 L = 6 N = 22         ROOT = 9.5025958064961E+01
R = 0.30 L = 6 N = 23         ROOT = 9.9478556202608E+01
R = 0.30 L = 6 N = 24         ROOT = 1.0390000000000E+02
R = 0.30 L = 6 N = 25         ROOT = 1.08392620313375E+02
R = 0.30 L = 6 N = 26         ROOT = 1.1265316933886E+02
R = 0.30 L = 6 N = 27         ROOT = 1.1700000000000E+02
R = 0.30 L = 6 N = 28         ROOT = 1.2178924332484E+02
R = 0.30 L = 6 N = 29         ROOT = 1.2624729541815E+02
R = 0.30 L = 6 N = 30         ROOT = 1.3071515680095E+02

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I ROOTS OF EQUATION 3
R = 0.50 L = 5 N = 1          ROOT = 6.7175337349846E+00
R = 0.50 L = 5 N = 2          ROOT = 1.915263091252E+01
R = 0.50 L = 5 N = 3          ROOT = 3.959364349257E+01
R = 0.50 L = 5 N = 4          ROOT = 2.0525268945477E+01
R = 0.50 L = 5 N = 5          ROOT = 2.524291554724E+01
R = 0.50 L = 5 N = 6          ROOT = 1.4299911534744E+01
R = 0.50 L = 5 N = 7          ROOT = 3.8544645711569E+01
R = 0.50 L = 5 N = 8          ROOT = 4.079871984896E+01
R = 0.50 L = 5 N = 9          ROOT = 0.8996711984339E+01
R = 0.50 L = 5 N = 10         ROOT = 5.7113539591757E+01
R = 0.50 L = 5 N = 11         ROOT = 6.3464985536568E+01
R = 0.50 L = 5 N = 12         ROOT = 1.9316648275424E+01
R = 0.50 L = 5 N = 13         ROOT = 7.5822294081850E+01
R = 0.50 L = 5 N = 14         ROOT = 8.037218373811E+01
R = 0.50 L = 5 N = 15         ROOT = 8.818108281844E+01
R = 0.50 L = 5 N = 16         ROOT = 9.4587087215646E+01
R = 0.50 L = 5 N = 17         ROOT = 1.0694967085576E+02
R = 0.50 L = 5 N = 18         ROOT = 1.1338014620863E+02
R = 0.50 L = 5 N = 19         ROOT = 1.1338014620863E+02
R = 0.50 L = 5 N = 20         ROOT = 1.1964845121757E+02
R = 0.50 L = 5 N = 21         ROOT = 1.2189331359198E+02
R = 0.50 L = 5 N = 22         ROOT = 1.32189331359198E+02
R = 0.50 L = 5 N = 23         ROOT = 1.3846158379446E+02
R = 0.50 L = 5 N = 24         ROOT = 1.4477252071442E+02
R = 0.50 L = 5 N = 25         ROOT = 1.5106859917510E+02
R = 0.50 L = 5 N = 26         ROOT = 1.5728338251766E+02
R = 0.50 L = 5 N = 27         ROOT = 1.6350000000000E+02
R = 0.50 L = 5 N = 28         ROOT = 1.6981459296183E+02
R = 0.50 L = 5 N = 29         ROOT = 1.761184542378E+02
R = 0.50 L = 5 N = 30         ROOT = 1.8238796205962E+02

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I ROOTS OF EQUATION 3
R = 0.50 L = 6 N = 1          ROOT = 7.0311178626560E+00
R = 0.50 L = 6 N = 2          ROOT = 1.915263091252E+01
R = 0.50 L = 6 N = 3          ROOT = 1.5926424117329E+01
R = 0.50 L = 6 N = 4          ROOT = 2.1130518152758E+01
R = 0.50 L = 6 N = 5          ROOT = 2.1130518152758E+01
R = 0.50 L = 6 N = 6          ROOT = 1.280264749542E+01
R = 0.50 L = 6 N = 7          ROOT = 3.885897442924E+01
R = 0.50 L = 6 N = 8          ROOT = 4.490218252044E+01
R = 0.50 L = 6 N = 9          ROOT = 4.13727392935E+01
R = 0.50 L = 6 N = 10         ROOT = 5.7324237622704E+01
R = 0.50 L = 6 N = 11         ROOT = 6.37428262723551E+01
R = 0.50 L = 6 N = 12         ROOT = 7.5980713341114E+01
R = 0.50 L = 6 N = 13         ROOT = 8.2219221575215E+01
R = 0.50 L = 6 N = 14         ROOT = 8.8546257520408E+01
R = 0.50 L = 6 N = 15         ROOT = 9.4714078337207E+01
R = 0.50 L = 6 N = 16         ROOT = 1.0896418232032E+02
R = 0.50 L = 6 N = 17         ROOT = 1.1254254393906E+02
R = 0.50 L = 6 N = 18         ROOT = 1.1348689518445E+02
R = 0.50 L = 6 N = 19         ROOT = 1.1574815151698E+02
R = 0.50 L = 6 N = 20         ROOT = 1.1574815151698E+02
R = 0.50 L = 6 N = 21         ROOT = 1.3228015526364E+02
R = 0.50 L = 6 N = 22         ROOT = 1.3228015526364E+02
R = 0.50 L = 6 N = 23         ROOT = 1.3854820539673E+02
R = 0.50 L = 6 N = 24         ROOT = 1.3854820539673E+02
R = 0.50 L = 6 N = 25         ROOT = 1.5108889479215E+02
R = 0.50 L = 6 N = 26         ROOT = 1.57335962444413E+02
R = 0.50 L = 6 N = 27         ROOT = 1.6350000000000E+02
R = 0.50 L = 6 N = 28         ROOT = 1.6990527984572E+02
R = 0.50 L = 6 N = 29         ROOT = 1.7617929387416E+02
R = 0.50 L = 6 N = 30         ROOT = 1.8245377281294E+02

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1 ROOTS OF EQUATION 3
A = 0.50 L = 7 N = 1      ROOT = 8.9249488762364E+01
A = 0.50 L = 7 N = 2      ROOT = 1.3177792612584E+01
A = 0.50 L = 7 N = 3      ROOT = 2.6822798566952E+01
A = 0.50 L = 7 N = 4      ROOT = 2.7398516561964E+01
A = 0.50 L = 7 N = 5      ROOT = 3.3254853235568E+01
A = 0.50 L = 7 N = 6      ROOT = 3.6222798566952E+01
A = 0.50 L = 7 N = 7      ROOT = 4.5290472010100E+01
A = 0.50 L = 7 N = 8      ROOT = 5.1421219783718E+01
A = 0.50 L = 7 N = 9      ROOT = 6.0222798566952E+01
A = 0.50 L = 7 N = 10     ROOT = 6.3751226112257E+01
A = 0.50 L = 7 N = 11     ROOT = 6.9951483714937E+01
A = 0.50 L = 7 N = 12     ROOT = 7.6222798566952E+01
A = 0.50 L = 7 N = 13     ROOT = 8.2389768885275E+01
A = 0.50 L = 7 N = 14     ROOT = 8.8622577368883E+01
A = 0.50 L = 7 N = 15     ROOT = 9.5000000000000E+01
A = 0.50 L = 7 N = 16     ROOT = 1.01166927577356E+02
A = 0.50 L = 7 N = 17     ROOT = 1.0735637659752E+02
A = 0.50 L = 7 N = 18     ROOT = 1.1986598755125E+02
A = 0.50 L = 7 N = 19     ROOT = 1.2612477952874E+02
A = 0.50 L = 7 N = 20     ROOT = 1.3231987342343E+02
A = 0.50 L = 7 N = 21     ROOT = 1.3864939962473E+02
A = 0.50 L = 7 N = 22     ROOT = 1.4491429581531E+02
A = 0.50 L = 7 N = 23     ROOT = 1.51144862762536E+02
A = 0.50 L = 7 N = 24     ROOT = 1.5744862762536E+02
A = 0.50 L = 7 N = 25     ROOT = 1.6371763965529E+02
A = 0.50 L = 7 N = 26     ROOT = 1.6989763976156E+02
A = 0.50 L = 7 N = 27     ROOT = 1.7606981036304E+02
A = 0.50 L = 7 N = 28     ROOT = 1.8235052708129E+02

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1 ROOTS OF EQUATION 3
A = 0.50 L = 8 N = 1      ROOT = 1.0685566574688E+01
A = 0.50 L = 8 N = 2      ROOT = 1.2425425424984E+01
A = 0.50 L = 8 N = 3      ROOT = 1.7977527218522E+01
A = 0.50 L = 8 N = 4      ROOT = 2.2598075496421E+01
A = 0.50 L = 8 N = 5      ROOT = 2.712477952874E+01
A = 0.50 L = 8 N = 6      ROOT = 3.2233987342343E+01
A = 0.50 L = 8 N = 7      ROOT = 3.9633067974898E+01
A = 0.50 L = 8 N = 8      ROOT = 4.5621095135350E+01
A = 0.50 L = 8 N = 9      ROOT = 5.240676151352E+01
A = 0.50 L = 8 N = 10     ROOT = 5.7848244880161E+01
A = 0.50 L = 8 N = 11     ROOT = 6.4682955425161E+01
A = 0.50 L = 8 N = 12     ROOT = 7.1524868161632E+01
A = 0.50 L = 8 N = 13     ROOT = 7.63758801035231E+01
A = 0.50 L = 8 N = 14     ROOT = 8.2584397385657E+01
A = 0.50 L = 8 N = 15     ROOT = 8.8081961961631E+01
A = 0.50 L = 8 N = 16     ROOT = 9.50389491961655E+01
A = 0.50 L = 8 N = 17     ROOT = 1.0126540359781E+02
A = 0.50 L = 8 N = 18     ROOT = 1.0735637659752E+02
A = 0.50 L = 8 N = 19     ROOT = 1.1375487542793E+02
A = 0.50 L = 8 N = 20     ROOT = 1.1999393692117E+02
A = 0.50 L = 8 N = 21     ROOT = 1.2644862762536E+02
A = 0.50 L = 8 N = 22     ROOT = 1.3256598831985E+02
A = 0.50 L = 8 N = 23     ROOT = 1.3876477657291E+02
A = 0.50 L = 8 N = 24     ROOT = 1.4512477952874E+02
A = 0.50 L = 8 N = 25     ROOT = 1.5126668197152E+02
A = 0.50 L = 8 N = 26     ROOT = 1.5755829481557E+02
A = 0.50 L = 8 N = 27     ROOT = 1.63881961961655E+02
A = 0.50 L = 8 N = 28     ROOT = 1.6980185896598E+02
A = 0.50 L = 8 N = 29     ROOT = 1.7634950135926E+02
A = 0.50 L = 8 N = 30     ROOT = 1.8261821339655E+02

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1 ROOTS OF EQUATION 3
A = 0.50 L = 9 N = 1      ROOT = 1.107714439741E+01
A = 0.50 L = 9 N = 2      ROOT = 1.5671111831280E+01
A = 0.50 L = 9 N = 3      ROOT = 2.026895956524E+01
A = 0.50 L = 9 N = 4      ROOT = 2.34528995956524E+01
A = 0.50 L = 9 N = 5      ROOT = 2.86542313338763E+01
A = 0.50 L = 9 N = 6      ROOT = 3.2265888437619E+01
A = 0.50 L = 9 N = 7      ROOT = 4.0692447714815E+01
A = 0.50 L = 9 N = 8      ROOT = 4.6843594428143E+01
A = 0.50 L = 9 N = 9      ROOT = 5.00000000000000E+01
A = 0.50 L = 9 N = 10     ROOT = 5.816888437619E+01
A = 0.50 L = 9 N = 11     ROOT = 6.4285218937826E+01
A = 0.50 L = 9 N = 12     ROOT = 6.80000000000000E+01
A = 0.50 L = 9 N = 13     ROOT = 7.5612048947811E+01
A = 0.50 L = 9 N = 14     ROOT = 8.2802713285202E+01
A = 0.50 L = 9 N = 15     ROOT = 8.98000000000000E+01
A = 0.50 L = 9 N = 16     ROOT = 9.60000000000000E+01
A = 0.50 L = 9 N = 17     ROOT = 1.0144339123661E+02
A = 0.50 L = 9 N = 18     ROOT = 1.07600000000000E+02
A = 0.50 L = 9 N = 19     ROOT = 1.256888437619E+02
A = 0.50 L = 9 N = 20     ROOT = 1.2814953783132E+02
A = 0.50 L = 9 N = 21     ROOT = 1.263932167817E+02
A = 0.50 L = 9 N = 22     ROOT = 1.30000000000000E+02
A = 0.50 L = 9 N = 23     ROOT = 1.3889459234151E+02
A = 0.50 L = 9 N = 24     ROOT = 1.491489505853E+02
A = 0.50 L = 9 N = 25     ROOT = 1.53000000000000E+02
A = 0.50 L = 9 N = 26     ROOT = 1.576640508526E+02
A = 0.50 L = 9 N = 27     ROOT = 1.6392531432352E+02
A = 0.50 L = 9 N = 28     ROOT = 1.68000000000000E+02
A = 0.50 L = 9 N = 29     ROOT = 1.7645161474546E+02
A = 0.50 L = 9 N = 30     ROOT = 1.8271681868343E+02

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1 ROOTS OF EQUATION 3
A = 0.50 L = 10 N = 1      ROOT = 1.2142137762025E+01
A = 0.50 L = 10 N = 2      ROOT = 1.80848000000000E+01
A = 0.50 L = 10 N = 3      ROOT = 2.0350728138296E+01
A = 0.50 L = 10 N = 4      ROOT = 2.4384283165606E+01
A = 0.50 L = 10 N = 5      ROOT = 2.93884823165606E+01
A = 0.50 L = 10 N = 6      ROOT = 3.4598117205325E+01
A = 0.50 L = 10 N = 7      ROOT = 4.059811864459E+01
A = 0.50 L = 10 N = 8      ROOT = 4.5487851424459E+01
A = 0.50 L = 10 N = 9      ROOT = 5.0236487424459E+01
A = 0.50 L = 10 N = 10     ROOT = 5.8565118438096E+01
A = 0.50 L = 10 N = 11     ROOT = 6.495764058959E+01
A = 0.50 L = 10 N = 12     ROOT = 7.00000000000000E+01
A = 0.50 L = 10 N = 13     ROOT = 7.69738030394592E+01
A = 0.50 L = 10 N = 14     ROOT = 8.384481280367E+01
A = 0.50 L = 10 N = 15     ROOT = 9.00000000000000E+01
A = 0.50 L = 10 N = 16     ROOT = 9.54310515958529E+01
A = 0.50 L = 10 N = 17     ROOT = 1.0164065290733E+02
A = 0.50 L = 10 N = 18     ROOT = 1.08000000000000E+02
A = 0.50 L = 10 N = 19     ROOT = 1.1485467522462E+02
A = 0.50 L = 10 N = 20     ROOT = 1.2031617908487E+02
A = 0.50 L = 10 N = 21     ROOT = 1.267384871390E+02
A = 0.50 L = 10 N = 22     ROOT = 1.327384871390E+02
A = 0.50 L = 10 N = 23     ROOT = 1.39038693387592E+02
A = 0.50 L = 10 N = 24     ROOT = 1.453791545134E+02
A = 0.50 L = 10 N = 25     ROOT = 1.513791545134E+02
A = 0.50 L = 10 N = 26     ROOT = 1.5779153584715E+02
A = 0.50 L = 10 N = 27     ROOT = 1.64000000000000E+02
A = 0.50 L = 10 N = 28     ROOT = 1.693051878914E+02
A = 0.50 L = 10 N = 29     ROOT = 1.7565591650842E+02
A = 0.50 L = 10 N = 30     ROOT = 1.828263262721E+02

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1 ROOTS OF EQUATION 3
R = 0.59 L = 11 N = 1      ROOT = 1.320212560567E+01
R = 0.59 L = 11 N = 2      ROOT = 1.069523840216E+01
R = 0.59 L = 11 N = 3      ROOT = 2.1693165404295E+01
R = 0.59 L = 11 N = 4      ROOT = 2.167394840216E+01
R = 0.59 L = 11 N = 5      ROOT = 0.0167394840216E+01
R = 0.59 L = 11 N = 6      ROOT = 3.5511249933678E+01
R = 0.59 L = 11 N = 7      ROOT = 2.1693165404295E+01
R = 0.59 L = 11 N = 8      ROOT = 4.636873396752E+01
R = 0.59 L = 11 N = 9      ROOT = 5.2884530627563E+01
R = 0.59 L = 11 N = 10     ROOT = 5.8864530627563E+01
R = 0.59 L = 11 N = 11     ROOT = 5.8864530627563E+01
R = 0.59 L = 11 N = 12     ROOT = 7.10351798520829E+01
R = 0.59 L = 11 N = 13     ROOT = 7.1689516185287E+01
R = 0.59 L = 11 N = 14     ROOT = 8.1852658951525E+01
R = 0.59 L = 11 N = 15     ROOT = 8.9478745405963E+01
R = 0.59 L = 11 N = 16     ROOT = 9.5462658951525E+01
R = 0.59 L = 11 N = 17     ROOT = 1.01852658951525E+02
R = 0.59 L = 11 N = 18     ROOT = 1.0866349253013E+02
R = 0.59 L = 11 N = 19     ROOT = 1.14277748962814E+02
R = 0.59 L = 11 N = 20     ROOT = 1.20389659132396E+02
R = 0.59 L = 11 N = 21     ROOT = 1.2672685253460E+02
R = 0.59 L = 11 N = 22     ROOT = 1.3295969132396E+02
R = 0.59 L = 11 N = 23     ROOT = 1.3839965558161E+02
R = 0.59 L = 11 N = 24     ROOT = 1.4543948779687E+02
R = 0.59 L = 11 N = 25     ROOT = 1.5168328857378E+02
R = 0.59 L = 11 N = 26     ROOT = 1.5708161812627E+02
R = 0.59 L = 11 N = 27     ROOT = 1.6418161812627E+02
R = 0.59 L = 11 N = 28     ROOT = 1.79434579305325E+02
R = 0.59 L = 11 N = 29     ROOT = 1.7685969856148E+02
R = 0.59 L = 11 N = 30     ROOT = 1.8294672391217E+02

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1 ROOTS OF EQUATION 3
R = 0.59 L = 12 N = 1      ROOT = 1.4258113337800E+01
R = 0.59 L = 12 N = 2      ROOT = 1.92359836471380E+01
R = 0.59 L = 12 N = 3      ROOT = 2.2463051521040E+01
R = 0.59 L = 12 N = 4      ROOT = 2.464893584262E+01
R = 0.59 L = 12 N = 5      ROOT = 3.012647655700E+01
R = 0.59 L = 12 N = 6      ROOT = 3.620964155700E+01
R = 0.59 L = 12 N = 7      ROOT = 4.033816681700E+01
R = 0.59 L = 12 N = 8      ROOT = 4.7478637143159E+01
R = 0.59 L = 12 N = 9      ROOT = 5.3346567741615E+01
R = 0.59 L = 12 N = 10     ROOT = 5.8556593564000E+01
R = 0.59 L = 12 N = 11     ROOT = 6.531633307247E+01
R = 0.59 L = 12 N = 12     ROOT = 7.1374635695623E+01
R = 0.59 L = 12 N = 13     ROOT = 7.7000000000000E+01
R = 0.59 L = 12 N = 14     ROOT = 8.3599524998933E+01
R = 0.59 L = 12 N = 15     ROOT = 8.9747719945889E+01
R = 0.59 L = 12 N = 16     ROOT = 9.5700000000000E+01
R = 0.59 L = 12 N = 17     ROOT = 1.0293919151571E+02
R = 0.59 L = 12 N = 18     ROOT = 1.0828599576720E+02
R = 0.59 L = 12 N = 19     ROOT = 1.13669873151789E+02
R = 0.59 L = 12 N = 20     ROOT = 1.2069873151789E+02
R = 0.59 L = 12 N = 21     ROOT = 1.2691648942678E+02
R = 0.59 L = 12 N = 22     ROOT = 1.332381648942678E+02
R = 0.59 L = 12 N = 23     ROOT = 1.39369567897960E+02
R = 0.59 L = 12 N = 24     ROOT = 1.45603591737066E+02
R = 0.59 L = 12 N = 25     ROOT = 1.5182681555649E+02
R = 0.59 L = 12 N = 26     ROOT = 1.5808811555649E+02
R = 0.59 L = 12 N = 27     ROOT = 1.6432791197081E+02
R = 0.59 L = 12 N = 28     ROOT = 1.69575497116108E+02
R = 0.59 L = 12 N = 29     ROOT = 1.7580811516108E+02
R = 0.59 L = 12 N = 30     ROOT = 1.8387759378793E+02

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ROOTS OF EQUATION 3

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R = 0.50 L = 13 N = 1
ROOT = 1.5310783379659E+01
R = 0.50 L = 13 N = 2
ROOT = 2.4134931382440E+01
R = 0.50 L = 13 N = 3
ROOT = 2.7634051529487E+01
R = 0.50 L = 13 N = 4
ROOT = 3.1524951520857E+01
R = 0.50 L = 13 N = 5
ROOT = 3.695505620208E+01
R = 0.50 L = 13 N = 6
ROOT = 4.23826532208E+01
R = 0.50 L = 13 N = 7
ROOT = 4.803464150973E+01
R = 0.50 L = 13 N = 8
ROOT = 5.383571397759E+01
R = 0.50 L = 13 N = 9
ROOT = 5.9737687516E+01
R = 0.50 L = 13 N = 10
ROOT = 6.56423298716E+01
R = 0.50 L = 13 N = 11
ROOT = 7.1740911239205E+01
R = 0.50 L = 13 N = 12
ROOT = 7.7816719881843E+01
R = 0.50 L = 13 N = 13
ROOT = 8.388365379717E+01
R = 0.50 L = 13 N = 14
ROOT = 9.008365379739E+01
R = 0.50 L = 13 N = 15
ROOT = 9.6185401366894E+01
R = 0.50 L = 13 N = 16
ROOT = 1.0398501366894E+02
R = 0.50 L = 13 N = 17
ROOT = 1.0852662508897E+02
R = 0.50 L = 13 N = 18
ROOT = 1.1471568895289E+02
R = 0.50 L = 13 N = 19
ROOT = 1.2108468895289E+02
R = 0.50 L = 13 N = 20
ROOT = 1.271216543792E+02
R = 0.50 L = 13 N = 21
ROOT = 1.3333597120317E+02
R = 0.50 L = 13 N = 22
ROOT = 1.395505620208E+02
R = 0.50 L = 13 N = 23
ROOT = 1.4579231662538E+02
R = 0.50 L = 13 N = 24
ROOT = 1.5201299193894E+02
R = 0.50 L = 13 N = 25
ROOT = 1.58230818895289E+02
R = 0.50 L = 13 N = 26
ROOT = 1.6428627516896E+02
R = 0.50 L = 13 N = 27
ROOT = 1.7027805019627E+02
R = 0.50 L = 13 N = 28
ROOT = 1.7697276389604E+02
R = 0.50 L = 13 N = 29
ROOT = 1.8322011239322E-02

```

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ROOTS OF EQUATION 3

```

R = 0.50 L = 14 N = 1
ROOT = 1.6360626698580E+01
R = 0.50 L = 14 N = 2
ROOT = 2.1526026242630E+01
R = 0.50 L = 14 N = 3
ROOT = 2.5383526158165E+01
R = 0.50 L = 14 N = 4
ROOT = 2.9165662539857E+01
R = 0.50 L = 14 N = 5
ROOT = 3.2874421079394E+01
R = 0.50 L = 14 N = 6
ROOT = 3.7748204143152E+01
R = 0.50 L = 14 N = 7
ROOT = 4.246204143152E+01
R = 0.50 L = 14 N = 8
ROOT = 4.628542539859E+01
R = 0.50 L = 14 N = 9
ROOT = 5.4362707828243E+01
R = 0.50 L = 14 N = 10
ROOT = 6.0241889523E+01
R = 0.50 L = 14 N = 11
ROOT = 6.41403732132E+01
R = 0.50 L = 14 N = 12
ROOT = 7.2133687575342E+01
R = 0.50 L = 14 N = 13
ROOT = 8.113919513091E+01
R = 0.50 L = 14 N = 14
ROOT = 8.746252475346E+01
R = 0.50 L = 14 N = 15
ROOT = 9.0358511752146E+01
R = 0.50 L = 14 N = 16
ROOT = 9.6404453978120E+01
R = 0.50 L = 14 N = 17
ROOT = 1.026204143152E+02
R = 0.50 L = 14 N = 18
ROOT = 1.0878525698875E+02
R = 0.50 L = 14 N = 19
ROOT = 1.1496311239322E+02
R = 0.50 L = 14 N = 20
ROOT = 1.2084411239322E+02
R = 0.50 L = 14 N = 21
ROOT = 1.2734231880923E+02
R = 0.50 L = 14 N = 22
ROOT = 1.33546384532275E+02
R = 0.50 L = 14 N = 23
ROOT = 1.39746384532275E+02
R = 0.50 L = 14 N = 24
ROOT = 1.459746384532275E+02
R = 0.50 L = 14 N = 25
ROOT = 1.5219741298458E+02
R = 0.50 L = 14 N = 26
ROOT = 1.5844841239322E+02
R = 0.50 L = 14 N = 27
ROOT = 1.6465667892477E+02
R = 0.50 L = 14 N = 28
ROOT = 1.7089221141514E+02
R = 0.50 L = 14 N = 29
ROOT = 1.7723361239322E+02

```

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ROOTS OF EQUATION 3

```

R • 0.59 L • 15 N • 1      ROOT • 1.74988123598275E+01
R • 0.59 L • 15 N • 2      ROOT • 2.26563843339948E+01
R • 0.59 L • 15 N • 3      ROOT • 2.6613146173078E+01
R • 0.59 L • 15 N • 4      ROOT • 2.99861468440E+01
R • 0.59 L • 15 N • 5      ROOT • 3.38951468440E+01
R • 0.59 L • 15 N • 6      ROOT • 3.858743684849E+01
R • 0.59 L • 15 N • 7      ROOT • 4.35218368440E+01
R • 0.59 L • 15 N • 8      ROOT • 4.9258713860770E+01
R • 0.59 L • 15 N • 9      ROOT • 5.4923822750529E+01
R • 0.59 L • 15 N • 10     ROOT • 6.040822750529E+01
R • 0.59 L • 15 N • 11     ROOT • 6.699558010715E+01
R • 0.59 L • 15 N • 12     ROOT • 7.2552617055339E+01
R • 0.59 L • 15 N • 13     ROOT • 7.8570477843941E+01
R • 0.59 L • 15 N • 14     ROOT • 8.45921477843941E+01
R • 0.59 L • 15 N • 15     ROOT • 9.06833984821375E+01
R • 0.59 L • 15 N • 16     ROOT • 9.6916254108022E+01
R • 0.59 L • 15 N • 17     ROOT • 1.02916254108022E+02
R • 0.59 L • 15 N • 18     ROOT • 1.0961182987159E+02
R • 0.59 L • 15 N • 19     ROOT • 1.1591193891159E+02
R • 0.59 L • 15 N • 20     ROOT • 1.2231939579732E+02
R • 0.59 L • 15 N • 21     ROOT • 1.2757938362984E+02
R • 0.59 L • 15 N • 22     ROOT • 1.3377139311804E+02
R • 0.59 L • 15 N • 23     ROOT • 1.3997144462557E+02
R • 0.59 L • 15 N • 24     ROOT • 1.4618051799532E+02
R • 0.59 L • 15 N • 25     ROOT • 1.5239415139879E+02
R • 0.59 L • 15 N • 26     ROOT • 1.5860415139879E+02
R • 0.59 L • 15 N • 27     ROOT • 1.6483989239250E+02
R • 0.59 L • 15 N • 28     ROOT • 1.7106795352085E+02
R • 0.59 L • 15 N • 29     ROOT • 1.76986983746E+02
R • 0.59 L • 15 N • 30     ROOT • 1.835981755588E+02

```

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ROOTS OF EQUATION 3

```

R • 0.60 L • 1 N • 1      ROOT • 1.746110208298E+00
R • 0.60 L • 1 N • 2      ROOT • 0.2767639802650E+01
R • 0.60 L • 1 N • 3      ROOT • 0.3592639952250E+01
R • 0.60 L • 1 N • 4      ROOT • 0.44238246280E+01
R • 0.60 L • 1 N • 5      ROOT • 0.522657339838E+01
R • 0.60 L • 1 N • 6      ROOT • 0.59346034155879E+01
R • 0.60 L • 1 N • 7      ROOT • 0.6574034155879E+01
R • 0.60 L • 1 N • 8      ROOT • 0.5038507568795E+01
R • 0.60 L • 1 N • 9      ROOT • 0.2884989564071E+01
R • 0.60 L • 1 N • 10     ROOT • 0.1082259651544E+01
R • 0.60 L • 1 N • 11     ROOT • 7.8582259651544E+01
R • 0.60 L • 1 N • 12     ROOT • 0.6432382493933E+01
R • 0.60 L • 1 N • 13     ROOT • 0.5038507568795E+01
R • 0.60 L • 1 N • 14     ROOT • 0.62134489312527E+02
R • 0.60 L • 1 N • 15     ROOT • 1.05986698983746E+02
R • 0.60 L • 1 N • 16     ROOT • 1.4866003049529E+02
R • 0.60 L • 1 N • 17     ROOT • 1.2569823246895E+02
R • 0.60 L • 1 N • 18     ROOT • 1.3354265367861E+02
R • 0.60 L • 1 N • 19     ROOT • 1.412132246227E+02
R • 0.60 L • 1 N • 20     ROOT • 1.4924798867679E+02
R • 0.60 L • 1 N • 21     ROOT • 1.5710893359199E+02
R • 0.60 L • 1 N • 22     ROOT • 1.650766867646227E+02
R • 0.60 L • 1 N • 23     ROOT • 1.72986867646227E+02
R • 0.60 L • 1 N • 24     ROOT • 1.8066003049529E+02
R • 0.60 L • 1 N • 25     ROOT • 1.8863247506646E+02
R • 0.60 L • 1 N • 26     ROOT • 1.963617506646E+02
R • 0.60 L • 1 N • 27     ROOT • 2.0421984618285E+02
R • 0.60 L • 1 N • 28     ROOT • 2.12832246227E+02
R • 0.60 L • 1 N • 29     ROOT • 2.202434545732E+02
R • 0.60 L • 1 N • 30     ROOT • 2.2778010240592E+02

```

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```

1 ROOTS OF EQUATION 3
A * 0.60 L * 2 N * 1
ROOT = 3.02457758395E+00
A * 0.60 L * 2 N * 2
ROOT = 0.7057257572658E+00
A * 0.60 L * 2 N * 3
ROOT = -1.6133831185867E+01
A * 0.60 L * 2 N * 4
ROOT = -2.00000000000E+01
A * 0.60 L * 2 N * 5
ROOT = 1.628347762386E+01
A * 0.60 L * 2 N * 6
ROOT = 3.9439785261845E+01
A * 0.60 L * 2 N * 7
ROOT = 4.728511564819E+01
A * 0.60 L * 2 N * 8
ROOT = 5.899173701238E+01
A * 0.60 L * 2 N * 9
ROOT = 6.2937984161946E+01
A * 0.60 L * 2 N * 10
ROOT = 7.00000000000E+01
A * 0.60 L * 2 N * 11
ROOT = 8.8624126126574E+01
A * 0.60 L * 2 N * 12
ROOT = 9.6470974759348E+01
A * 0.60 L * 2 N * 13
ROOT = 1.04375000000E+02
A * 0.60 L * 2 N * 14
ROOT = 1.0216786218254E+02
A * 0.60 L * 2 N * 15
ROOT = 1.0816577855761E+02
A * 0.60 L * 2 N * 16
ROOT = 1.1571674171864E+02
A * 0.60 L * 2 N * 17
ROOT = 1.231674171864E+02
A * 0.60 L * 2 N * 18
ROOT = 1.3356762166332E+02
A * 0.60 L * 2 N * 19
ROOT = 1.4156882889459E+02
A * 0.60 L * 2 N * 20
ROOT = 1.4927882889459E+02
A * 0.60 L * 2 N * 21
ROOT = 1.5712307579412E+02
A * 0.60 L * 2 N * 22
ROOT = 1.6497403616859E+02
A * 0.60 L * 2 N * 23
ROOT = 1.728347762386E+02
A * 0.60 L * 2 N * 24
ROOT = 1.8067848425719E+02
A * 0.60 L * 2 N * 25
ROOT = 1.8853895882072E+02
A * 0.60 L * 2 N * 26
ROOT = 1.9639857882072E+02
A * 0.60 L * 2 N * 27
ROOT = 2.0423617746945E+02
A * 0.60 L * 2 N * 28
ROOT = 2.1208694296152E+02
A * 0.60 L * 2 N * 29
ROOT = 2.1994188163381E+02
A * 0.60 L * 2 N * 30
ROOT = 2.277347761464E+02

```

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```

1 ROOTS OF EQUATION 3
A * 0.60 L * 3 N * 1
ROOT = 4.2361967929793E+00
A * 0.60 L * 3 N * 2
ROOT = 9.1649377191864E+00
A * 0.60 L * 3 N * 3
ROOT = 6.6493751938732E+01
A * 0.60 L * 3 N * 4
ROOT = 2.4856855133381E+01
A * 0.60 L * 3 N * 5
ROOT = 3.1787189565993E+01
A * 0.60 L * 3 N * 6
ROOT = 4.8211682348968E+01
A * 0.60 L * 3 N * 7
ROOT = 4.7371435296923E+01
A * 0.60 L * 3 N * 8
ROOT = 5.5198695768671E+01
A * 0.60 L * 3 N * 9
ROOT = 6.2523252325232E+01
A * 0.60 L * 3 N * 10
ROOT = 7.0850873724403E+01
A * 0.60 L * 3 N * 11
ROOT = 7.8680354778272E+01
A * 0.60 L * 3 N * 12
ROOT = 8.6413651761066E+01
A * 0.60 L * 3 N * 13
ROOT = 9.4371563176106E+01
A * 0.60 L * 3 N * 14
ROOT = 1.0221682348968E+02
A * 0.60 L * 3 N * 15
ROOT = 1.10000000000E+02
A * 0.60 L * 3 N * 16
ROOT = 1.1790875246335E+02
A * 0.60 L * 3 N * 17
ROOT = 1.2579554568372E+02
A * 0.60 L * 3 N * 18
ROOT = 1.33683333333E+02
A * 0.60 L * 3 N * 19
ROOT = 1.414541931264E+02
A * 0.60 L * 3 N * 20
ROOT = 1.4930383131123E+02
A * 0.60 L * 3 N * 21
ROOT = 1.571674171864E+02
A * 0.60 L * 3 N * 22
ROOT = 1.6500434916982E+02
A * 0.60 L * 3 N * 23
ROOT = 1.728511564819E+02
A * 0.60 L * 3 N * 24
ROOT = 1.805882889459E+02
A * 0.60 L * 3 N * 25
ROOT = 1.885574523523527E+02
A * 0.60 L * 3 N * 26
ROOT = 1.9646895829532E+02
A * 0.60 L * 3 N * 27
ROOT = 2.0423617746945E+02
A * 0.60 L * 3 N * 28
ROOT = 2.1211252012373E+02
A * 0.60 L * 3 N * 29
ROOT = 2.2701668940866E+02

```

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## 1 ROOTS OF EQUATION 3

```

R • 8.68 L • 4 N • 1      ROOT • 5.4383384496110E+00
R • 8.68 L • 4 N • 2      ROOT • 1.08632174367672E+01
R • 8.68 L • 4 N • 3      ROOT • 1.48632174367672E+01
R • 8.68 L • 4 N • 4      ROOT • 2.4383384496110E+01
R • 8.68 L • 4 N • 5      ROOT • 3.48632174367672E+01
R • 8.68 L • 4 N • 6      ROOT • 3.73592313806540E+01
R • 8.68 L • 4 N • 7      ROOT • 4.7514492486689E+01
R • 8.68 L • 4 N • 8      ROOT • 5.51818514193620E+01
R • 8.68 L • 4 N • 9      ROOT • 6.1218880828710E+01
R • 8.68 L • 4 N • 10     ROOT • 7.09458526878707E+01
R • 8.68 L • 4 N • 11     ROOT • 8.042137481119E+01
R • 8.68 L • 4 N • 12     ROOT • 8.65091882138050E+01
R • 8.68 L • 4 N • 13     ROOT • 9.444240739592E+01
R • 8.68 L • 4 N • 14     ROOT • 1.0228127220086E+02
R • 8.68 L • 4 N • 15     ROOT • 1.1082127220086E+02
R • 8.68 L • 4 N • 16     ROOT • 1.1796531109562E+02
R • 8.68 L • 4 N • 17     ROOT • 1.2586957214454E+02
R • 8.68 L • 4 N • 18     ROOT • 1.3377401112056E+02
R • 8.68 L • 4 N • 19     ROOT • 1.4159133292513E+02
R • 8.68 L • 4 N • 20     ROOT • 1.4934849193647E+02
R • 8.68 L • 4 N • 21     ROOT • 1.57156188217435E+02
R • 8.68 L • 4 N • 22     ROOT • 1.6504475862141E+02
R • 8.68 L • 4 N • 23     ROOT • 1.7289368921735E+02
R • 8.68 L • 4 N • 24     ROOT • 1.807818821735E+02
R • 8.68 L • 4 N • 25     ROOT • 1.885291284561E+02
R • 8.68 L • 4 N • 26     ROOT • 1.964428491598E+02
R • 8.68 L • 4 N • 27     ROOT • 2.043449396139E+02
R • 8.68 L • 4 N • 28     ROOT • 2.121439722824E+02
R • 8.68 L • 4 N • 29     ROOT • 2.199948477607E+02
X • 8.68 L • 4 N • 30     ROOT • 2.2788259516078E+02

```

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## 1 ROOTS OF EQUATION 3

```

R • 8.68 L • 5 N • 1      ROOT • 6.5973033957449E+00
R • 8.68 L • 5 N • 2      ROOT • 1.26862397570126E+01
R • 8.68 L • 5 N • 3      ROOT • 2.4681866327863E+01
R • 8.68 L • 5 N • 4      ROOT • 3.22595460514641E+01
R • 8.68 L • 5 N • 5      ROOT • 4.0837852187222E+01
R • 8.68 L • 5 N • 6      ROOT • 4.7688189712648E+01
R • 8.68 L • 5 N • 7      ROOT • 5.5461910733686E+01
R • 8.68 L • 5 N • 8      ROOT • 6.3147777524648E+01
R • 8.68 L • 5 N • 9      ROOT • 7.1862615243565E+01
R • 8.68 L • 5 N • 10     ROOT • 7.9878995491235E+01
R • 8.68 L • 5 N • 11     ROOT • 8.7570000000000E+01
R • 8.68 L • 5 N • 12     ROOT • 9.4530528187222E+01
R • 8.68 L • 5 N • 13     ROOT • 1.0236277953267E+02
R • 8.68 L • 5 N • 14     ROOT • 1.09236277953267E+02
R • 8.68 L • 5 N • 15     ROOT • 1.1603597468519E+02
R • 8.68 L • 5 N • 16     ROOT • 1.1883597468519E+02
R • 8.68 L • 5 N • 17     ROOT • 1.2587592749664E+02
R • 8.68 L • 5 N • 18     ROOT • 1.3287592749664E+02
R • 8.68 L • 5 N • 19     ROOT • 1.4156023749664E+02
R • 8.68 L • 5 N • 20     ROOT • 1.4940439831832E+02
R • 8.68 L • 5 N • 21     ROOT • 1.57156188217435E+02
R • 8.68 L • 5 N • 22     ROOT • 1.6504475862141E+02
R • 8.68 L • 5 N • 23     ROOT • 1.7294189517508E+02
R • 8.68 L • 5 N • 24     ROOT • 1.807818821735E+02
R • 8.68 L • 5 N • 25     ROOT • 1.8863796731262E+02
R • 8.68 L • 5 N • 26     ROOT • 1.9648533668043E+02
R • 8.68 L • 5 N • 27     ROOT • 2.043449396139E+02
R • 8.68 L • 5 N • 28     ROOT • 2.121439722824E+02
R • 8.68 L • 5 N • 29     ROOT • 2.199948477607E+02
R • 8.68 L • 5 N • 30     ROOT • 2.2788259516078E+02

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1 ROOTS OF EQUATION 3
R = 0.68 L = 6 N = 1          ROOT = 7.7391115195673E+00
R = 0.68 L = 6 N = 2          ROOT = 1.1976319613171E+01
R = 0.68 L = 6 N = 3          ROOT = 2.5898953343101E+01
R = 0.68 L = 6 N = 4          ROOT = 3.2571079592401E+01
R = 0.68 L = 6 N = 5          ROOT = 3.9243875592401E+01
R = 0.68 L = 6 N = 6          ROOT = 4.7898316480773E+01
R = 0.68 L = 6 N = 7          ROOT = 5.5642487554264E+01
R = 0.68 L = 6 N = 8          ROOT = 6.3380854854264E+01
R = 0.68 L = 6 N = 9          ROOT = 7.1261457945454E+01
R = 0.68 L = 6 N = 10         ROOT = 7.9085864178570E+01
R = 0.68 L = 6 N = 11         ROOT = 8.6808584178570E+01
R = 0.68 L = 6 N = 12         ROOT = 9.4636356736917E+01
R = 0.68 L = 6 N = 13         ROOT = 1.0246951144013E+02
R = 0.68 L = 6 N = 14         ROOT = 1.1012627051703E+02
R = 0.68 L = 6 N = 15         ROOT = 1.1812627051703E+02
R = 0.68 L = 6 N = 16         ROOT = 1.25955229287807E+02
R = 0.68 L = 6 N = 17         ROOT = 1.337895229287807E+02
R = 0.68 L = 6 N = 18         ROOT = 1.4163889375793E+02
R = 0.68 L = 6 N = 19         ROOT = 1.49471234549053E+02
R = 0.68 L = 6 N = 20         ROOT = 1.5729992618465E+02
R = 0.68 L = 6 N = 21         ROOT = 1.65153820865E+02
R = 0.68 L = 6 N = 22         ROOT = 1.730992618465E+02
R = 0.68 L = 6 N = 23         ROOT = 1.809992618465E+02
R = 0.68 L = 6 N = 24         ROOT = 1.8869902389264E+02
R = 0.68 L = 6 N = 25         ROOT = 1.9653623059237E+02
R = 0.68 L = 6 N = 26         ROOT = 2.0438337622989E+02
R = 0.68 L = 6 N = 27         ROOT = 2.12238337622989E+02
R = 0.68 L = 6 N = 28         ROOT = 2.2007819243620E+02
R = 0.68 L = 6 N = 29         ROOT = 2.279768670278E+02
R = 0.68 L = 6 N = 30         ROOT = 2.3592641833127E+02

```

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```

1 ROOTS OF EQUATION 3
R = 0.68 L = 7 N = 1          ROOT = 8.0589188932394E+00
R = 0.68 L = 7 N = 2          ROOT = 1.38472268569E+01
R = 0.68 L = 7 N = 3          ROOT = 1.863925329909E+01
R = 0.68 L = 7 N = 4          ROOT = 2.5561197565267E+01
R = 0.68 L = 7 N = 5          ROOT = 3.2571079592401E+01
R = 0.68 L = 7 N = 6          ROOT = 4.048534949195E+01
R = 0.68 L = 7 N = 7          ROOT = 4.8142411289513E+01
R = 0.68 L = 7 N = 8          ROOT = 5.5642487554264E+01
R = 0.68 L = 7 N = 9          ROOT = 6.3398045141936E+01
R = 0.68 L = 7 N = 10         ROOT = 7.1367456314852E+01
R = 0.68 L = 7 N = 11         ROOT = 7.9085864178570E+01
R = 0.68 L = 7 N = 12         ROOT = 8.6808584178570E+01
R = 0.68 L = 7 N = 13         ROOT = 9.4636356736917E+01
R = 0.68 L = 7 N = 14         ROOT = 1.0246951144013E+02
R = 0.68 L = 7 N = 15         ROOT = 1.1012627051703E+02
R = 0.68 L = 7 N = 16         ROOT = 1.1812627051703E+02
R = 0.68 L = 7 N = 17         ROOT = 1.25955229287807E+02
R = 0.68 L = 7 N = 18         ROOT = 1.337895229287807E+02
R = 0.68 L = 7 N = 19         ROOT = 1.4163889375793E+02
R = 0.68 L = 7 N = 20         ROOT = 1.49471234549053E+02
R = 0.68 L = 7 N = 21         ROOT = 1.5729992618465E+02
R = 0.68 L = 7 N = 22         ROOT = 1.65153820865E+02
R = 0.68 L = 7 N = 23         ROOT = 1.730992618465E+02
R = 0.68 L = 7 N = 24         ROOT = 1.809992618465E+02
R = 0.68 L = 7 N = 25         ROOT = 1.8869902389264E+02
R = 0.68 L = 7 N = 26         ROOT = 1.9653623059237E+02
R = 0.68 L = 7 N = 27         ROOT = 2.0438337622989E+02
R = 0.68 L = 7 N = 28         ROOT = 2.12238337622989E+02
R = 0.68 L = 7 N = 29         ROOT = 2.2007819243620E+02
R = 0.68 L = 7 N = 30         ROOT = 2.279768670278E+02

```

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```

1 ROOTS OF EQUATION 3
R = 0.60 L = 8 N = 1
ROOT = 9.36818847855E+00
R = 0.60 L = 8 N = 2
ROOT = -1.41746192198E+01
R = 0.60 L = 8 N = 3
ROOT = 1.93752292522E+01
R = 0.60 L = 8 N = 4
ROOT = 2.00000000000E+01
R = 0.60 L = 8 N = 5
ROOT = 3.3338695275065E+01
R = 0.60 L = 8 N = 6
ROOT = 4.8819851498119E+01
R = 0.60 L = 8 N = 7
ROOT = 5.00000000000E+01
R = 0.60 L = 8 N = 8
ROOT = 5.6891604783958E+01
R = 0.60 L = 8 N = 9
ROOT = 6.3887366715267E+01
R = 0.60 L = 8 N = 10
ROOT = 7.00000000000E+01
R = 0.60 L = 8 N = 11
ROOT = 7.93222112128E+01
R = 0.60 L = 8 N = 12
ROOT = 8.7185595428785E+01
R = 0.60 L = 8 N = 13
ROOT = 9.27000000000E+01
R = 0.60 L = 8 N = 14
ROOT = 9.79442795848E+02
R = 0.60 L = 8 N = 15
ROOT = 1.1851556159871E+02
R = 0.60 L = 8 N = 16
ROOT = 1.26133743439112E+02
R = 0.60 L = 8 N = 17
ROOT = 1.3397698232770E+02
R = 0.60 L = 8 N = 18
ROOT = 1.3397698232770E+02
R = 0.60 L = 8 N = 19
ROOT = 1.42666666666E+02
R = 0.60 L = 8 N = 20
ROOT = 1.496384963744E+02
R = 0.60 L = 8 N = 21
ROOT = 1.5747186628486E+02
R = 0.60 L = 8 N = 22
ROOT = 1.6530728889479E+02
R = 0.60 L = 8 N = 23
ROOT = 1.73188666666E+02
R = 0.60 L = 8 N = 24
ROOT = 1.809827340307E+02
R = 0.60 L = 8 N = 25
ROOT = 1.88825956971E+02
R = 0.60 L = 8 N = 26
ROOT = 1.96668888889E+02
R = 0.60 L = 8 N = 27
ROOT = 2.0458534989279E+02
R = 0.60 L = 8 N = 28
ROOT = 2.1234615383643E+02
R = 0.60 L = 8 N = 29
ROOT = 2.20188666666E+02
R = 0.60 L = 8 N = 30
ROOT = 2.2803689917231E+02

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1 ROOTS OF EQUATION 3
R = 0.60 L = 9 N = 1
ROOT = 1.18462956731894E+01
R = 0.60 L = 9 N = 2
ROOT = 1.5339542054191E+01
R = 0.60 L = 9 N = 3
ROOT = 2.0188271495449E+01
R = 0.60 L = 9 N = 4
ROOT = 2.6674006235085E+01
R = 0.60 L = 9 N = 5
ROOT = 3.42000000000E+01
R = 0.60 L = 9 N = 6
ROOT = 4.18867150891E+01
R = 0.60 L = 9 N = 7
ROOT = 4.8730661748316E+01
R = 0.60 L = 9 N = 8
ROOT = 5.6339542054191E+01
R = 0.60 L = 9 N = 9
ROOT = 6.403732330377E+01
R = 0.60 L = 9 N = 10
ROOT = 7.176432620525E+01
R = 0.60 L = 9 N = 11
ROOT = 7.951487925891E+01
R = 0.60 L = 9 N = 12
ROOT = 8.77744444444E+01
R = 0.60 L = 9 N = 13
ROOT = 9.5858633334739E+01
R = 0.60 L = 9 N = 14
ROOT = 1.0285491384849E+02
R = 0.60 L = 9 N = 15
ROOT = 1.1024242424242E+02
R = 0.60 L = 9 N = 16
ROOT = 1.1845915220333E+02
R = 0.60 L = 9 N = 17
ROOT = 1.26272656666E+02
R = 0.60 L = 9 N = 18
ROOT = 1.34111561764E+02
R = 0.60 L = 9 N = 19
ROOT = 1.4191315641764E+02
R = 0.60 L = 9 N = 20
ROOT = 1.4973973535997E+02
R = 0.60 L = 9 N = 21
ROOT = 1.57567744444E+02
R = 0.60 L = 9 N = 22
ROOT = 1.6539795808394E+02
R = 0.60 L = 9 N = 23
ROOT = 1.7323687450181E+02
R = 0.60 L = 9 N = 24
ROOT = 1.81065888889E+02
R = 0.60 L = 9 N = 25
ROOT = 1.8890196610288E+02
R = 0.60 L = 9 N = 26
ROOT = 1.9673971833367E+02
R = 0.60 L = 9 N = 27
ROOT = 2.0446818473172E+02
R = 0.60 L = 9 N = 28
ROOT = 2.1218818473172E+02
R = 0.60 L = 9 N = 29
ROOT = 2.2003998389440E+02
R = 0.60 L = 9 N = 30
ROOT = 2.2810186462787E+02

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1 ROOTS OF EQUATION 3
R • 0.60 L • 10 N • 1      ROOT • 1.2122616689653E+01
R • 0.60 L • 10 N • 2      ROOT • 1.6527342082656E+01
R • 0.60 L • 10 N • 3      ROOT • 2.1000000000000E+01
R • 0.60 L • 10 N • 4      ROOT • 2.7316984742597E+01
R • 0.60 L • 10 N • 5      ROOT • 3.4289451673985E+01
R • 0.60 L • 10 N • 6      ROOT • 4.14662689171E+01
R • 0.60 L • 10 N • 7      ROOT • 4.9073744462597E+01
R • 0.60 L • 10 N • 8      ROOT • 5.665895726141E+01
R • 0.60 L • 10 N • 9      ROOT • 6.4246815615965E+01
R • 0.60 L • 10 N • 10     ROOT • 7.1835829312946E+01
R • 0.60 L • 10 N • 11     ROOT • 7.9721387317681E+01
R • 0.60 L • 10 N • 12     ROOT • 8.7424546878433E+01
R • 0.60 L • 10 N • 13     ROOT • 9.52348446878433E+01
R • 0.60 L • 10 N • 14     ROOT • 1.0381273235585E+02
R • 0.60 L • 10 N • 15     ROOT • 1.1089284356752E+02
R • 0.60 L • 10 N • 16     ROOT • 1.1786244356752E+02
R • 0.60 L • 10 N • 17     ROOT • 1.246473332725E+02
R • 0.60 L • 10 N • 18     ROOT • 1.3421530617338E+02
R • 0.60 L • 10 N • 19     ROOT • 1.4408263057338E+02
R • 0.60 L • 10 N • 20     ROOT • 1.4985808710567E+02
R • 0.60 L • 10 N • 21     ROOT • 1.5767294849434E+02
R • 0.60 L • 10 N • 22     ROOT • 1.6544968750000E+02
R • 0.60 L • 10 N • 23     ROOT • 1.7312710359875E+02
R • 0.60 L • 10 N • 24     ROOT • 1.8115768136758E+02
R • 0.60 L • 10 N • 25     ROOT • 1.8892443764594E+02
R • 0.60 L • 10 N • 26     ROOT • 1.9682443767364E+02
R • 0.60 L • 10 N • 27     ROOT • 2.0466018576894E+02
R • 0.60 L • 10 N • 28     ROOT • 2.125358089673E+02
R • 0.60 L • 10 N • 29     ROOT • 2.2017495932463E+02
R • 0.60 L • 10 N • 30     ROOT • 2.2817495932463E+02

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1 ROOTS OF EQUATION 3
R • 0.60 L • 11 N • 1      ROOT • 1.318971906054E+01
R • 0.60 L • 11 N • 2      ROOT • 1.7726858569287E+01
R • 0.60 L • 11 N • 3      ROOT • 2.2299867479392E+01
R • 0.60 L • 11 N • 4      ROOT • 2.799867284295E+01
R • 0.60 L • 11 N • 5      ROOT • 3.4029637284295E+01
R • 0.60 L • 11 N • 6      ROOT • 4.0156694915823E+01
R • 0.60 L • 11 N • 7      ROOT • 4.9446694915823E+01
R • 0.60 L • 11 N • 8      ROOT • 5.698829491524E+01
R • 0.60 L • 11 N • 9      ROOT • 6.3521956115216E+01
R • 0.60 L • 11 N • 10     ROOT • 7.2251956115216E+01
R • 0.60 L • 11 N • 11     ROOT • 7.995153312546E+01
R • 0.60 L • 11 N • 12     ROOT • 8.7000000000000E+01
R • 0.60 L • 11 N • 13     ROOT • 9.4267345159407E+01
R • 0.60 L • 11 N • 14     ROOT • 1.0193681773779E+02
R • 0.60 L • 11 N • 15     ROOT • 1.1896752438852E+02
R • 0.60 L • 11 N • 16     ROOT • 1.3600000000000E+02
R • 0.60 L • 11 N • 17     ROOT • 1.2524993018838E+02
R • 0.60 L • 11 N • 18     ROOT • 1.3424993018838E+02
R • 0.60 L • 11 N • 19     ROOT • 1.4125000000000E+02
R • 0.60 L • 11 N • 20     ROOT • 1.4997246715352E+02
R • 0.60 L • 11 N • 21     ROOT • 1.5776924531188E+02
R • 0.60 L • 11 N • 22     ROOT • 1.65566924531188E+02
R • 0.60 L • 11 N • 23     ROOT • 1.7343289938946E+02
R • 0.60 L • 11 N • 24     ROOT • 1.8125895223563E+02
R • 0.60 L • 11 N • 25     ROOT • 1.8892443764594E+02
R • 0.60 L • 11 N • 26     ROOT • 1.9691759814508E+02
R • 0.60 L • 11 N • 27     ROOT • 2.047497789712E+02
R • 0.60 L • 11 N • 28     ROOT • 2.125358089673E+02
R • 0.60 L • 11 N • 29     ROOT • 2.2017495932463E+02
R • 0.60 L • 11 N • 30     ROOT • 2.2825331689324E+02

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1 ROOTS OF EQUATION 3
R • 0.60 L • 12 N • 1 ROOT • 1.425831770939E+01
R • 0.60 L • 12 N • 2 ROOT • 1.892851837206E+01
R • 0.60 L • 12 N • 3 ROOT • 2.3592851837206E+01
R • 0.60 L • 12 N • 4 ROOT • 2.8732657568379E+01
R • 0.60 L • 12 N • 5 ROOT • 3.5416987986934E+01
R • 0.60 L • 12 N • 6 ROOT • 4.285489472561E+01
R • 0.60 L • 12 N • 7 ROOT • 4.985489472561E+01
R • 0.60 L • 12 N • 8 ROOT • 5.732317587142E+01
R • 0.60 L • 12 N • 9 ROOT • 6.52317587142E+01
R • 0.60 L • 12 N • 10 ROOT • 7.32317587142E+01
R • 0.60 L • 12 N • 11 ROOT • 8.028067858924E+01
R • 0.60 L • 12 N • 12 ROOT • 8.635014646172E+01
R • 0.60 L • 12 N • 13 ROOT • 9.5635014646172E+01
R • 0.60 L • 12 N • 14 ROOT • 1.03847738759E+02
R • 0.60 L • 12 N • 15 ROOT • 1.1182196553330E+02
R • 0.60 L • 12 N • 16 ROOT • 1.1892196553330E+02
R • 0.60 L • 12 N • 17 ROOT • 1.267879451598E+02
R • 0.60 L • 12 N • 18 ROOT • 1.34688777959E+02
R • 0.60 L • 12 N • 19 ROOT • 1.42588777959E+02
R • 0.60 L • 12 N • 20 ROOT • 1.5018565919893E+02
R • 0.60 L • 12 N • 21 ROOT • 1.579168343345E+02
R • 0.60 L • 12 N • 22 ROOT • 1.656343345E+02
R • 0.60 L • 12 N • 23 ROOT • 1.735482459986E+02
R • 0.60 L • 12 N • 24 ROOT • 1.813626658395E+02
R • 0.60 L • 12 N • 25 ROOT • 1.891918268952E+02
R • 0.60 L • 12 N • 26 ROOT • 1.9701918268952E+02
R • 0.60 L • 12 N • 27 ROOT • 2.048477614932E+02
R • 0.60 L • 12 N • 28 ROOT • 2.126785243590E+02
R • 0.60 L • 12 N • 29 ROOT • 2.2056954827972E+02
R • 0.60 L • 12 N • 30 ROOT • 2.2834295033620E+02

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1 ROOTS OF EQUATION 3
R • 0.60 L • 13 N • 1 ROOT • 1.53059599303150E+01
R • 0.60 L • 13 N • 2 ROOT • 2.01229947319280E+01
R • 0.60 L • 13 N • 3 ROOT • 2.46221965653330E+01
R • 0.60 L • 13 N • 4 ROOT • 2.9512507107576E+01
R • 0.60 L • 13 N • 5 ROOT • 3.4412507107576E+01
R • 0.60 L • 13 N • 6 ROOT • 4.303054275876E+01
R • 0.60 L • 13 N • 7 ROOT • 5.0291577533208E+01
R • 0.60 L • 13 N • 8 ROOT • 5.732317587142E+01
R • 0.60 L • 13 N • 9 ROOT • 6.5234635658631E+01
R • 0.60 L • 13 N • 10 ROOT • 7.26284049886839E+01
R • 0.60 L • 13 N • 11 ROOT • 8.0136266583952E+01
R • 0.60 L • 13 N • 12 ROOT • 8.8153568349550E+01
R • 0.60 L • 13 N • 13 ROOT • 9.5863279829601E+01
R • 0.60 L • 13 N • 14 ROOT • 1.038477614932E+02
R • 0.60 L • 13 N • 15 ROOT • 1.143615456895E+02
R • 0.60 L • 13 N • 16 ROOT • 1.1910537858395E+02
R • 0.60 L • 13 N • 17 ROOT • 1.2687126259645E+02
R • 0.60 L • 13 N • 18 ROOT • 1.346343345E+02
R • 0.60 L • 13 N • 19 ROOT • 1.4245286025631E+02
R • 0.60 L • 13 N • 20 ROOT • 1.5025926549218E+02
R • 0.60 L • 13 N • 21 ROOT • 1.5805663265905E+02
R • 0.60 L • 13 N • 22 ROOT • 1.6586112267516E+02
R • 0.60 L • 13 N • 23 ROOT • 1.7361312627890E+02
R • 0.60 L • 13 N • 24 ROOT • 1.8140608480501E+02
R • 0.60 L • 13 N • 25 ROOT • 1.893075980132E+02
R • 0.60 L • 13 N • 26 ROOT • 1.9712917885147E+02
R • 0.60 L • 13 N • 27 ROOT • 2.0491985147E+02
R • 0.60 L • 13 N • 28 ROOT • 2.12775955959568E+02
R • 0.60 L • 13 N • 29 ROOT • 2.2060792243590E+02
R • 0.60 L • 13 N • 30 ROOT • 2.2843785283587E+02

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1 ROOTS OF EQUATION 3
R • 0.68 L • 14 N • 1 ROOT • 1.635766297207E+01
R • 0.68 L • 14 N • 2 ROOT • 2.1102852525887E+01
R • 0.68 L • 14 N • 3 ROOT • 3.1102852525887E+01
R • 0.68 L • 14 N • 4 ROOT • 3.0335361631963E+01
R • 0.68 L • 14 N • 5 ROOT • 3.6599239129879E+01
R • 0.68 L • 14 N • 6 ROOT • 4.15921360527E+01
R • 0.68 L • 14 N • 7 ROOT • 5.0759184103636E+01
R • 0.68 L • 14 N • 8 ROOT • 5.817395687665E+01
R • 0.68 L • 14 N • 9 ROOT • 6.55912360527E+01
R • 0.68 L • 14 N • 10 ROOT • 7.31494959586243E+01
R • 0.68 L • 14 N • 11 ROOT • 8.076309530425E+01
R • 0.68 L • 14 N • 12 ROOT • 8.83809530425E+01
R • 0.68 L • 14 N • 13 ROOT • 9.6106989533631E+01
R • 0.68 L • 14 N • 14 ROOT • 1.0381997989946E+02
R • 0.68 L • 14 N • 15 ROOT • 1.1138141592893E+02
R • 0.68 L • 14 N • 16 ROOT • 1.1938141592893E+02
R • 0.68 L • 14 N • 17 ROOT • 1.2706395172769E+02
R • 0.68 L • 14 N • 18 ROOT • 1.3474173679262E+02
R • 0.68 L • 14 N • 19 ROOT • 1.4261673679262E+02
R • 0.68 L • 14 N • 20 ROOT • 1.5048563085767E+02
R • 0.68 L • 14 N • 21 ROOT • 1.5835333085767E+02
R • 0.68 L • 14 N • 22 ROOT • 1.66201851719191E+02
R • 0.68 L • 14 N • 23 ROOT • 1.7398752148093E+02
R • 0.68 L • 14 N • 24 ROOT • 1.817652148093E+02
R • 0.68 L • 14 N • 25 ROOT • 1.8943685801829E+02
R • 0.68 L • 14 N • 26 ROOT • 1.9724757395923E+02
R • 0.68 L • 14 N • 27 ROOT • 2.050571401284E+02
R • 0.68 L • 14 N • 28 ROOT • 2.128877171284E+02
R • 0.68 L • 14 N • 29 ROOT • 2.2071361160799E+02
R • 0.68 L • 14 N • 30 ROOT • 2.2854061375324E+02

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1 ROOTS OF EQUATION 3
R • 0.68 L • 15 N • 1 ROOT • 1.748620463135495E+01
R • 0.68 L • 15 N • 2 ROOT • 2.2499545144235E+01
R • 0.68 L • 15 N • 3 ROOT • 2.6219524316498E+01
R • 0.68 L • 15 N • 4 ROOT • 3.1199358298729E+01
R • 0.68 L • 15 N • 5 ROOT • 3.6019358298729E+01
R • 0.68 L • 15 N • 6 ROOT • 4.4157541231872E+01
R • 0.68 L • 15 N • 7 ROOT • 5.1253965972494E+01
R • 0.68 L • 15 N • 8 ROOT • 5.8038529528177E+01
R • 0.68 L • 15 N • 9 ROOT • 6.5975716694296E+01
R • 0.68 L • 15 N • 10 ROOT • 7.3492165977673E+01
R • 0.68 L • 15 N • 11 ROOT • 8.0267859528917E+01
R • 0.68 L • 15 N • 12 ROOT • 8.7020959528917E+01
R • 0.68 L • 15 N • 13 ROOT • 9.6367429314417E+01
R • 0.68 L • 15 N • 14 ROOT • 1.04087429314417E+02
R • 0.68 L • 15 N • 15 ROOT • 1.1277707128394E+02
R • 0.68 L • 15 N • 16 ROOT • 1.1951113859886E+02
R • 0.68 L • 15 N • 17 ROOT • 1.2524441333614E+02
R • 0.68 L • 15 N • 18 ROOT • 1.346289333614E+02
R • 0.68 L • 15 N • 19 ROOT • 1.4279212922693E+02
R • 0.68 L • 15 N • 20 ROOT • 1.5057193812946E+02
R • 0.68 L • 15 N • 21 ROOT • 1.5835333085767E+02
R • 0.68 L • 15 N • 22 ROOT • 1.6615251336487E+02
R • 0.68 L • 15 N • 23 ROOT • 1.7395141157274E+02
R • 0.68 L • 15 N • 24 ROOT • 1.817652148093E+02
R • 0.68 L • 15 N • 25 ROOT • 1.8956289732768E+02
R • 0.68 L • 15 N • 26 ROOT • 1.9737433394357E+02
R • 0.68 L • 15 N • 27 ROOT • 2.050571401284E+02
R • 0.68 L • 15 N • 28 ROOT • 2.128877171284E+02
R • 0.68 L • 15 N • 29 ROOT • 2.2071361160799E+02
R • 0.68 L • 15 N • 30 ROOT • 2.2854061375324E+02

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1 ROOTS OF EQUATION 3

```

R = 0.79 L = 1 N = 1      ROOT = 1.65436817091666E+00
R = 0.79 L = 1 N = 2      ROOT = 1.6744564491242E+01
R = 0.79 L = 1 N = 3      ROOT = 1.694561016590E+01
R = 0.79 L = 1 N = 4      ROOT = 3.1596881016590E+01
R = 0.79 L = 1 N = 5      ROOT = 4.19561547563E+01
R = 0.79 L = 1 N = 6      ROOT = 5.00000000000E+01
R = 0.79 L = 1 N = 7      ROOT = 6.2877327244641E+01
R = 0.79 L = 1 N = 8      ROOT = 7.3342896156398E+01
R = 0.79 L = 1 N = 9      ROOT = 8.2387852459350E+01
R = 0.79 L = 1 N = 10     ROOT = 9.4278895245935E+01
R = 0.79 L = 1 N = 11     ROOT = 1.0474783912273E+02
R = 0.79 L = 1 N = 12     ROOT = 1.16600000000E+02
R = 0.79 L = 1 N = 13     ROOT = 1.256844273788E+02
R = 0.79 L = 1 N = 14     ROOT = 1.3615665925768E+02
R = 0.79 L = 1 N = 15     ROOT = 1.47166666666E+02
R = 0.79 L = 1 N = 16     ROOT = 1.5785782195136E+02
R = 0.79 L = 1 N = 17     ROOT = 1.6756866666688E+02
R = 0.79 L = 1 N = 18     ROOT = 1.7736866666688E+02
R = 0.79 L = 1 N = 19     ROOT = 1.881687168035E+02
R = 0.79 L = 1 N = 20     ROOT = 1.9898189461681E+02
R = 0.79 L = 1 N = 21     ROOT = 2.097981521594E+02
R = 0.79 L = 1 N = 22     ROOT = 2.205981521594E+02
R = 0.79 L = 1 N = 23     ROOT = 2.30359586297562E+02
R = 0.79 L = 1 N = 24     ROOT = 2.40136769519366E+02
R = 0.79 L = 1 N = 25     ROOT = 2.50136769519366E+02
R = 0.79 L = 1 N = 26     ROOT = 2.6181030130039E+02
R = 0.79 L = 1 N = 27     ROOT = 2.7228185706851E+02
R = 0.79 L = 1 N = 28     ROOT = 2.8275886666666E+02
R = 0.79 L = 1 N = 29     ROOT = 2.9322505852988E+02
R = 0.79 L = 1 N = 30     PCOT = 3.0369669603345E+02

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1 ROOTS OF EQUATION 3

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R = 0.79 L = 2 N = 1      ROOT = 2.8625462453961E+00
R = 0.79 L = 2 N = 2      ROOT = 1.1819185754292E+01
R = 0.79 L = 2 N = 3      ROOT = 2.1217123672742E+01
R = 0.79 L = 2 N = 4      ROOT = 3.1597925295897E+01
R = 0.79 L = 2 N = 5      ROOT = 4.19561547563E+01
R = 0.79 L = 2 N = 6      ROOT = 5.00000000000E+01
R = 0.79 L = 2 N = 7      ROOT = 6.2922812777598E+01
R = 0.79 L = 2 N = 8      ROOT = 7.3342896156398E+01
R = 0.79 L = 2 N = 9      ROOT = 8.2387852459350E+01
R = 0.79 L = 2 N = 10     ROOT = 9.4278895245935E+01
R = 0.79 L = 2 N = 11     ROOT = 1.0474783912273E+02
R = 0.79 L = 2 N = 12     ROOT = 1.16600000000E+02
R = 0.79 L = 2 N = 13     ROOT = 1.256844273788E+02
R = 0.79 L = 2 N = 14     ROOT = 1.3615665925768E+02
R = 0.79 L = 2 N = 15     ROOT = 1.47166666666E+02
R = 0.79 L = 2 N = 16     ROOT = 1.5785782195136E+02
R = 0.79 L = 2 N = 17     ROOT = 1.6756866666688E+02
R = 0.79 L = 2 N = 18     ROOT = 1.7736866666688E+02
R = 0.79 L = 2 N = 19     ROOT = 1.881687168035E+02
R = 0.79 L = 2 N = 20     ROOT = 1.9898189461681E+02
R = 0.79 L = 2 N = 21     ROOT = 2.097981521594E+02
R = 0.79 L = 2 N = 22     ROOT = 2.205981521594E+02
R = 0.79 L = 2 N = 23     ROOT = 2.30359586297562E+02
R = 0.79 L = 2 N = 24     ROOT = 2.40136769519366E+02
R = 0.79 L = 2 N = 25     ROOT = 2.50136769519366E+02
R = 0.79 L = 2 N = 26     ROOT = 2.6181030130039E+02
R = 0.79 L = 2 N = 27     ROOT = 2.7228185706851E+02
R = 0.79 L = 2 N = 28     ROOT = 2.8275886666666E+02
R = 0.79 L = 2 N = 29     ROOT = 2.9322505852988E+02
R = 0.79 L = 2 N = 30     ROOT = 3.0369669603345E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 3 N = 1          ROOT = 1.8421619871989E+00
A = 0.70 L = 3 N = 2          ROOT = 1.141988085293E+01
A = 0.70 L = 3 N = 3          ROOT = 2.1429783821585E+01
A = 0.70 L = 3 N = 4          ROOT = 3.1429783821585E+01
A = 0.70 L = 3 N = 5          ROOT = 4.2126547567482E+01
A = 0.70 L = 3 N = 6          ROOT = 5.2556819895668E+01
A = 0.70 L = 3 N = 7          ROOT = 6.2986159895668E+01
A = 0.70 L = 3 N = 8          ROOT = 7.3446238950327E+01
A = 0.70 L = 3 N = 9          ROOT = 8.3895159483183E+01
A = 0.70 L = 3 N = 10         ROOT = 9.4335285442477E+01
A = 0.70 L = 3 N = 11         ROOT = 1.048152424773E+02
A = 0.70 L = 3 N = 12         ROOT = 1.1527853829586E+02
A = 0.70 L = 3 N = 13         ROOT = 1.257000000000E+02
A = 0.70 L = 3 N = 14         ROOT = 1.3628913526316E+02
A = 0.70 L = 3 N = 15         ROOT = 1.4667586441131E+02
A = 0.70 L = 3 N = 16         ROOT = 1.571289394362E+02
A = 0.70 L = 3 N = 17         ROOT = 1.6761289394362E+02
A = 0.70 L = 3 N = 18         ROOT = 1.7807975490565E+02
A = 0.70 L = 3 N = 19         ROOT = 1.8854679337688E+02
A = 0.70 L = 3 N = 20         ROOT = 1.989179337688E+02
A = 0.70 L = 3 N = 21         ROOT = 2.0948725603034E+02
A = 0.70 L = 3 N = 22         ROOT = 2.1995655745035E+02
A = 0.70 L = 3 N = 23         ROOT = 2.2946328563593E+02
A = 0.70 L = 3 N = 24         ROOT = 2.40896395500110E+02
A = 0.70 L = 3 N = 25         ROOT = 2.513674555256E+02
A = 0.70 L = 3 N = 26         ROOT = 2.618362155256E+02
A = 0.70 L = 3 N = 27         ROOT = 2.7230899105399E+02
A = 0.70 L = 3 N = 28         ROOT = 2.8277970630701E+02
A = 0.70 L = 3 N = 29         ROOT = 2.9224770630701E+02
A = 0.70 L = 3 N = 30         ROOT = 3.0372021822899E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 4 N = 1          ROOT = 5.2081018927458E+00
A = 0.70 L = 4 N = 2          ROOT = 2.1935653997537E+01
A = 0.70 L = 4 N = 3          ROOT = 3.1914649993784E+01
A = 0.70 L = 4 N = 4          ROOT = 4.2262423514493E+01
A = 0.70 L = 4 N = 5          ROOT = 5.2591745932381E+01
A = 0.70 L = 4 N = 6          ROOT = 6.291745932381E+01
A = 0.70 L = 4 N = 7          ROOT = 7.35180832956255E+01
A = 0.70 L = 4 N = 8          ROOT = 8.3961892913535E+01
A = 0.70 L = 4 N = 9          ROOT = 9.440448939353E+01
A = 0.70 L = 4 N = 10         ROOT = 1.0486977476052E+02
A = 0.70 L = 4 N = 11         ROOT = 1.15328177328674E+02
A = 0.70 L = 4 N = 12         ROOT = 1.258677408274E+02
A = 0.70 L = 4 N = 13         ROOT = 1.3625199415594E+02
A = 0.70 L = 4 N = 14         ROOT = 1.467356884547E+02
A = 0.70 L = 4 N = 15         ROOT = 1.571289394362E+02
A = 0.70 L = 4 N = 16         ROOT = 1.6761289394362E+02
A = 0.70 L = 4 N = 17         ROOT = 1.7807975490565E+02
A = 0.70 L = 4 N = 18         ROOT = 1.8854679337688E+02
A = 0.70 L = 4 N = 19         ROOT = 1.989179337688E+02
A = 0.70 L = 4 N = 20         ROOT = 2.0948725603034E+02
A = 0.70 L = 4 N = 21         ROOT = 2.1995655745035E+02
A = 0.70 L = 4 N = 22         ROOT = 2.2946328563593E+02
A = 0.70 L = 4 N = 23         ROOT = 2.40896395500110E+02
A = 0.70 L = 4 N = 24         ROOT = 2.4092067706264E+02
A = 0.70 L = 4 N = 25         ROOT = 2.513674555256E+02
A = 0.70 L = 4 N = 26         ROOT = 2.618362155256E+02
A = 0.70 L = 4 N = 27         ROOT = 2.7232997651882E+02
A = 0.70 L = 4 N = 28         ROOT = 2.8277970630701E+02
A = 0.70 L = 4 N = 29         ROOT = 2.9224770630701E+02
A = 0.70 L = 4 N = 30         ROOT = 3.0372021822899E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 5 N = 1      ROOT = 6.363184980759E+00
A = 0.70 L = 5 N = 2      ROOT = 1.255396761325E+01
A = 0.70 L = 5 N = 3      ROOT = 2.1398017390E+01
A = 0.70 L = 5 N = 4      ROOT = 3.21398017390E+01
A = 0.70 L = 5 N = 5      ROOT = 4.243168795978E+01
A = 0.70 L = 5 N = 6      ROOT = 5.27546818801E+01
A = 0.70 L = 5 N = 7      ROOT = 6.3195078334248E+01
A = 0.70 L = 5 N = 8      ROOT = 7.361520943963E+01
A = 0.70 L = 5 N = 9      ROOT = 8.419613307394E+01
A = 0.70 L = 5 N = 10     ROOT = 9.49613307394E+01
A = 0.70 L = 5 N = 11     ROOT = 1.0493790193718E+02
A = 0.70 L = 5 N = 12     ROOT = 1.1493790193718E+02
A = 0.70 L = 5 N = 13     ROOT = 1.248552636339E+02
A = 0.70 L = 5 N = 14     ROOT = 1.3630352540114E+02
A = 0.70 L = 5 N = 15     ROOT = 1.4722510931605E+02
A = 0.70 L = 5 N = 16     ROOT = 1.5722510931605E+02
A = 0.70 L = 5 N = 17     ROOT = 1.6768795667162E+02
A = 0.70 L = 5 N = 18     ROOT = 1.7815195667162E+02
A = 0.70 L = 5 N = 19     ROOT = 1.886173991517E+02
A = 0.70 L = 5 N = 20     ROOT = 1.9986239553633E+02
A = 0.70 L = 5 N = 21     ROOT = 2.110454087711E+02
A = 0.70 L = 5 N = 22     ROOT = 2.222454087711E+02
A = 0.70 L = 5 N = 23     ROOT = 2.334826317103E+02
A = 0.70 L = 5 N = 24     ROOT = 2.4495180989610E+02
A = 0.70 L = 5 N = 25     ROOT = 2.5642831898439E+02
A = 0.70 L = 5 N = 26     ROOT = 2.610866877247E+02
A = 0.70 L = 5 N = 27     ROOT = 2.72355316460E+02
A = 0.70 L = 5 N = 28     ROOT = 2.83522677130E+02
A = 0.70 L = 5 N = 29     ROOT = 2.9329326216632E+02
A = 0.70 L = 5 N = 30     ROOT = 3.0376255018903E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 6 N = 1      ROOT = 7.5078135337444E+00
A = 0.70 L = 6 N = 2      ROOT = 1.326229113993E+01
A = 0.70 L = 6 N = 3      ROOT = 2.0464513522E+01
A = 0.70 L = 6 N = 4      ROOT = 3.2406464513522E+01
A = 0.70 L = 6 N = 5      ROOT = 4.2633963810649E+01
A = 0.70 L = 6 N = 6      ROOT = 5.285000000000E+01
A = 0.70 L = 6 N = 7      ROOT = 6.333078665568E+01
A = 0.70 L = 6 N = 8      ROOT = 7.3731768079643E+01
A = 0.70 L = 6 N = 9      ROOT = 8.419613307394E+01
A = 0.70 L = 6 N = 10     ROOT = 9.49613307394E+01
A = 0.70 L = 6 N = 11     ROOT = 1.0493790193718E+02
A = 0.70 L = 6 N = 12     ROOT = 1.1493790193718E+02
A = 0.70 L = 6 N = 13     ROOT = 1.248552636339E+02
A = 0.70 L = 6 N = 14     ROOT = 1.3630352540114E+02
A = 0.70 L = 6 N = 15     ROOT = 1.4685180989610E+02
A = 0.70 L = 6 N = 16     ROOT = 1.5642831898439E+02
A = 0.70 L = 6 N = 17     ROOT = 1.6773911584829E+02
A = 0.70 L = 6 N = 18     ROOT = 1.7828865816526E+02
A = 0.70 L = 6 N = 19     ROOT = 1.886173991517E+02
A = 0.70 L = 6 N = 20     ROOT = 1.9986239553633E+02
A = 0.70 L = 6 N = 21     ROOT = 2.110454087711E+02
A = 0.70 L = 6 N = 22     ROOT = 2.222454087711E+02
A = 0.70 L = 6 N = 23     ROOT = 2.334826317103E+02
A = 0.70 L = 6 N = 24     ROOT = 2.4495180989610E+02
A = 0.70 L = 6 N = 25     ROOT = 2.5642831898439E+02
A = 0.70 L = 6 N = 26     ROOT = 2.6191941830604E+02
A = 0.70 L = 6 N = 27     ROOT = 2.7238677855602E+02
A = 0.70 L = 6 N = 28     ROOT = 2.83522677130E+02
A = 0.70 L = 6 N = 29     ROOT = 2.9329326216632E+02
A = 0.70 L = 6 N = 30     ROOT = 3.0379076835961E+02

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ROOTS OF EQUATION 3

```

R = 0.70 L = ? N = 1
ROOT = 0.5418252372863E+00
R = 0.70 L = ? N = 2
ROOT = 0.48672351725E+00
R = 0.70 L = ? N = 3
ROOT = 2.2862315917726E+01
R = 0.70 L = ? N = 4
ROOT = 3.215159133279E+01
R = 0.70 L = ? N = 5
ROOT = 2.6889515479E+01
R = 0.70 L = ? N = 6
ROOT = 3.146897982339E+01
R = 0.70 L = ? N = 7
ROOT = 6.348975985955E+01
R = 0.70 L = ? N = 8
ROOT = 3.096899298959E+01
R = 0.70 L = ? N = 9
ROOT = 8.4269281703052E+01
R = 0.70 L = ? N = 10
ROOT = 9.46864218132E+01
R = 0.70 L = ? N = 11
ROOT = 1.034873588529E+02
R = 0.70 L = ? N = 12
ROOT = 1.1555097811275E+02
R = 0.70 L = ? N = 13
ROOT = 1.2599307469348E+02
R = 0.70 L = ? N = 14
ROOT = 1.3648904340632E+02
R = 0.70 L = ? N = 15
ROOT = 1.4689004340632E+02
R = 0.70 L = ? N = 16
ROOT = 1.5734321657305E+02
R = 0.70 L = ? N = 17
ROOT = 1.6781527527769E+02
R = 0.70 L = ? N = 18
ROOT = 1.7825618866869E+02
R = 0.70 L = ? N = 19
ROOT = 1.8871522527769E+02
R = 0.70 L = ? N = 20
ROOT = 1.992861527769E+02
R = 0.70 L = ? N = 21
ROOT = 2.0983725012956E+02
R = 0.70 L = ? N = 22
ROOT = 2.208998153798E+02
R = 0.70 L = ? N = 23
ROOT = 2.3146864218132E+02
R = 0.70 L = ? N = 24
ROOT = 2.410273965292E+02
R = 0.70 L = ? N = 25
ROOT = 2.5149221256615E+02
R = 0.70 L = ? N = 26
ROOT = 2.6195751313525E+02
R = 0.70 L = ? N = 27
ROOT = 2.72522951313525E+02
R = 0.70 L = ? N = 28
ROOT = 2.8288983518764E+02
R = 0.70 L = ? N = 29
ROOT = 2.93355895271E+02
R = 0.70 L = ? N = 30
ROOT = 3.0382369638871E+02

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ROOTS OF EQUATION 3

```

R = 0.70 L = 8 N = 1
ROOT = 9.7650553276311E+00
R = 0.70 L = 8 N = 2
ROOT = 1.4982531744768E+01
R = 0.70 L = 8 N = 3
ROOT = 2.3166261598684E+01
R = 0.70 L = 8 N = 4
ROOT = 3.1366261598684E+01
R = 0.70 L = 8 N = 5
ROOT = 4.3135720769864E+01
R = 0.70 L = 8 N = 6
ROOT = 5.3162863616986E+01
R = 0.70 L = 8 N = 7
ROOT = 6.3162863616986E+01
R = 0.70 L = 8 N = 8
ROOT = 7.4022289541776E+01
R = 0.70 L = 8 N = 9
ROOT = 8.448491354236E+01
R = 0.70 L = 8 N = 10
ROOT = 9.49523591108E+01
R = 0.70 L = 8 N = 11
ROOT = 1.05223397573110E+02
R = 0.70 L = 8 N = 12
ROOT = 1.1564969584090E+02
R = 0.70 L = 8 N = 13
ROOT = 1.261766484913E+02
R = 0.70 L = 8 N = 14
ROOT = 1.3652352635306E+02
R = 0.70 L = 8 N = 15
ROOT = 1.4696765266445E+02
R = 0.70 L = 8 N = 16
ROOT = 1.5734321657305E+02
R = 0.70 L = 8 N = 17
ROOT = 1.6781527527769E+02
R = 0.70 L = 8 N = 18
ROOT = 1.7825618866869E+02
R = 0.70 L = 8 N = 19
ROOT = 1.8871522527769E+02
R = 0.70 L = 8 N = 20
ROOT = 1.992861527769E+02
R = 0.70 L = 8 N = 21
ROOT = 2.0983725012956E+02
R = 0.70 L = 8 N = 22
ROOT = 2.208998153798E+02
R = 0.70 L = 8 N = 23
ROOT = 2.3146864218132E+02
R = 0.70 L = 8 N = 24
ROOT = 2.410273965292E+02
R = 0.70 L = 8 N = 25
ROOT = 2.5153756520767E+02
R = 0.70 L = 8 N = 26
ROOT = 2.6195751313525E+02
R = 0.70 L = 8 N = 27
ROOT = 2.7246544429395E+02
R = 0.70 L = 8 N = 28
ROOT = 2.8293025333359E+02
R = 0.70 L = 8 N = 29
ROOT = 2.93355895271E+02
R = 0.70 L = 8 N = 30
ROOT = 3.0382369638871E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 9 N = 1      ROOT = 1.8977547682564E+01
A = 0.70 L = 9 N = 2      ROOT = 1.5913856842464E+01
A = 0.70 L = 9 N = 3      ROOT = 2.3921630233153E+01
A = 0.70 L = 9 N = 4      ROOT = 2.054140579313E+01
A = 0.70 L = 9 N = 5      ROOT = 4.3434140579313E+01
A = 0.70 L = 9 N = 6      ROOT = 5.3682186191719E+01
A = 0.70 L = 9 N = 7      ROOT = 6.1782186191719E+01
A = 0.70 L = 9 N = 8      ROOT = 6.195953885204E+01
A = 0.70 L = 9 N = 9      ROOT = 8.4557293686910E+01
A = 0.70 L = 9 N = 10     ROOT = 9.0000000000000E+01
A = 0.70 L = 9 N = 11     ROOT = 9.03578074577E+02
A = 0.70 L = 9 N = 12     ROOT = 1.1576180081846E+02
A = 0.70 L = 9 N = 13     ROOT = 1.3621770877193E+02
A = 0.70 L = 9 N = 14     ROOT = 1.3621770877193E+02
A = 0.70 L = 9 N = 15     ROOT = 1.4785534101947E+02
A = 0.70 L = 9 N = 16     ROOT = 1.5745143670323E+02
A = 0.70 L = 9 N = 17     ROOT = 1.6714143670323E+02
A = 0.70 L = 9 N = 18     ROOT = 1.7839240949899E+02
A = 0.70 L = 9 N = 19     ROOT = 1.888439757752E+02
A = 0.70 L = 9 N = 20     ROOT = 1.988439757752E+02
A = 0.70 L = 9 N = 21     ROOT = 2.0975308437155E+02
A = 0.70 L = 9 N = 22     ROOT = 2.2021816022122E+02
A = 0.70 L = 9 N = 23     ROOT = 2.3077815934222E+02
A = 0.70 L = 9 N = 24     ROOT = 2.4112814964355E+02
A = 0.70 L = 9 N = 25     ROOT = 2.515877101342E+02
A = 0.70 L = 9 N = 26     ROOT = 2.6204563332103E+02
A = 0.70 L = 9 N = 27     ROOT = 2.7251263331040E+02
A = 0.70 L = 9 N = 28     ROOT = 2.8297567090837E+02
A = 0.70 L = 9 N = 29     ROOT = 3.3162815934222E+02
A = 0.70 L = 9 N = 30     ROOT = 3.0393031596618E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 10 N = 1      ROOT = 1.1979623406572E+01
A = 0.70 L = 10 N = 2      ROOT = 1.6774065930519E+01
A = 0.70 L = 10 N = 3      ROOT = 2.054140579313E+01
A = 0.70 L = 10 N = 4      ROOT = 2.38841493775732E+01
A = 0.70 L = 10 N = 5      ROOT = 3.3763462437363E+01
A = 0.70 L = 10 N = 6      ROOT = 3.8098613673133E+01
A = 0.70 L = 10 N = 7      ROOT = 4.0293613673133E+01
A = 0.70 L = 10 N = 8      ROOT = 7.438954937003E+01
A = 0.70 L = 10 N = 9      ROOT = 8.4262275850958E+01
A = 0.70 L = 10 N = 10     ROOT = 8.6951405410390E+01
A = 0.70 L = 10 N = 11     ROOT = 1.05461405453309E+02
A = 0.70 L = 10 N = 12     ROOT = 1.1584140531192E+02
A = 0.70 L = 10 N = 13     ROOT = 1.3073891561592E+02
A = 0.70 L = 10 N = 14     ROOT = 1.3672228315192E+02
A = 0.70 L = 10 N = 15     ROOT = 1.4745249196573E+02
A = 0.70 L = 10 N = 16     ROOT = 1.575249196573E+02
A = 0.70 L = 10 N = 17     ROOT = 1.6802851818366E+02
A = 0.70 L = 10 N = 18     ROOT = 1.7847249794574E+02
A = 0.70 L = 10 N = 19     ROOT = 1.888439757752E+02
A = 0.70 L = 10 N = 20     ROOT = 1.99369273934895E+02
A = 0.70 L = 10 N = 21     ROOT = 2.0982119358212E+02
A = 0.70 L = 10 N = 22     ROOT = 2.2021816022122E+02
A = 0.70 L = 10 N = 23     ROOT = 2.3077815934222E+02
A = 0.70 L = 10 N = 24     ROOT = 2.41187396415239E+02
A = 0.70 L = 10 N = 25     ROOT = 2.5158771013422E+02
A = 0.70 L = 10 N = 26     ROOT = 2.6204563332103E+02
A = 0.70 L = 10 N = 27     ROOT = 2.7256595638139E+02
A = 0.70 L = 10 N = 28     ROOT = 2.8297567090837E+02
A = 0.70 L = 10 N = 29     ROOT = 3.3162815934222E+02
A = 0.70 L = 10 N = 30     ROOT = 3.0393031596618E+02

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ROOTS OF EQUATION 3

```

R • 0.70 L • 11 N • 1      ROOT • 1.3871878488469E+01
R • 0.70 L • 11 N • 2      ROOT • 1.7775473580469E+01
R • 0.70 L • 11 N • 3      ROOT • 2.5174357146948E+01
R • 0.70 L • 11 N • 4      ROOT • 3.2562128126120E+01
R • 0.70 L • 11 N • 5      ROOT • 4.4123034647373E+01
R • 0.70 L • 11 N • 6      ROOT • 5.4161794388365E+01
R • 0.70 L • 11 N • 7      ROOT • 6.4199884388365E+01
R • 0.70 L • 11 N • 8      ROOT • 7.4599866909324E+01
R • 0.70 L • 11 N • 9      ROOT • 8.4911785731143E+01
R • 0.70 L • 11 N • 10     ROOT • 9.4911785731143E+01
R • 0.70 L • 11 N • 11     ROOT • 1.0563940056247E+02
R • 0.70 L • 11 N • 12     ROOT • 1.160281153883E+02
R • 0.70 L • 11 N • 13     ROOT • 1.263381153883E+02
R • 0.70 L • 11 N • 14     ROOT • 1.368172672232E+02
R • 0.70 L • 11 N • 15     ROOT • 1.4725929722228E+02
R • 0.70 L • 11 N • 16     ROOT • 1.57638222357524E+02
R • 0.70 L • 11 N • 17     ROOT • 1.6812283575244E+02
R • 0.70 L • 11 N • 18     ROOT • 1.7856854595766E+02
R • 0.70 L • 11 N • 19     ROOT • 1.8906855959813E+02
R • 0.70 L • 11 N • 20     ROOT • 1.9956860280124E+02
R • 0.70 L • 11 N • 21     ROOT • 2.0989689293286E+02
R • 0.70 L • 11 N • 22     ROOT • 2.2094636801885E+02
R • 0.70 L • 11 N • 23     ROOT • 2.3199637397382E+02
R • 0.70 L • 11 N • 24     ROOT • 2.4125255156546E+02
R • 0.70 L • 11 N • 25     ROOT • 2.5176886335195E+02
R • 0.70 L • 11 N • 26     ROOT • 2.6222710611723E+02
R • 0.70 L • 11 N • 27     ROOT • 2.7262271061196E+02
R • 0.70 L • 11 N • 28     ROOT • 2.830816574223E+02
R • 0.70 L • 11 N • 29     ROOT • 2.9355984052342E+02
R • 0.70 L • 11 N • 30     ROOT • 3.0400232474246E+02

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ROOTS OF EQUATION 3

```

R • 0.70 L • 12 N • 1      ROOT • 1.4155097129639E+01
R • 0.70 L • 12 N • 2      ROOT • 1.881124652613E+01
R • 0.70 L • 12 N • 3      ROOT • 2.5865871736563E+01
R • 0.70 L • 12 N • 4      ROOT • 3.381124652613E+01
R • 0.70 L • 12 N • 5      ROOT • 4.4512170825666E+01
R • 0.70 L • 12 N • 6      ROOT • 5.447858666463E+01
R • 0.70 L • 12 N • 7      ROOT • 6.4444444444444E+01
R • 0.70 L • 12 N • 8      ROOT • 7.48237275703259E+01
R • 0.70 L • 12 N • 9      ROOT • 8.5113720224963E+01
R • 0.70 L • 12 N • 10     ROOT • 9.5402335111111E+01
R • 0.70 L • 12 N • 11     ROOT • 10.579323973572E+02
R • 0.70 L • 12 N • 12     ROOT • 1.1616788017682E+02
R • 0.70 L • 12 N • 13     ROOT • 1.2655983653994E+02
R • 0.70 L • 12 N • 14     ROOT • 1.3695086069632E+02
R • 0.70 L • 12 N • 15     ROOT • 1.4737578674935E+02
R • 0.70 L • 12 N • 16     ROOT • 1.5773668727369E+02
R • 0.70 L • 12 N • 17     ROOT • 1.681124652613E+02
R • 0.70 L • 12 N • 18     ROOT • 1.7865655456813E+02
R • 0.70 L • 12 N • 19     ROOT • 1.8909346405839E+02
R • 0.70 L • 12 N • 20     ROOT • 1.9955984052342E+02
R • 0.70 L • 12 N • 21     ROOT • 2.099776455886E+02
R • 0.70 L • 12 N • 22     ROOT • 2.2042416179706E+02
R • 0.70 L • 12 N • 23     ROOT • 2.308708080808E+02
R • 0.70 L • 12 N • 24     ROOT • 2.4132361071555E+02
R • 0.70 L • 12 N • 25     ROOT • 2.5177618972399E+02
R • 0.70 L • 12 N • 26     ROOT • 2.6222710611723E+02
R • 0.70 L • 12 N • 27     ROOT • 2.6268539378484E+02
R • 0.70 L • 12 N • 28     ROOT • 2.8314242560696E+02
R • 0.70 L • 12 N • 29     ROOT • 2.9355984052342E+02
R • 0.70 L • 12 N • 30     ROOT • 3.0400232474246E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 13 N = 1          ROOT = 1.532024313213E+01
A = 0.70 L = 13 N = 2          ROOT = 1.9875342432908E+01
A = 0.70 L = 13 N = 3          ROOT = 2.6597028576199E+01
A = 0.70 L = 13 N = 4          ROOT = 3.4897285730151E+01
A = 0.70 L = 13 N = 5          ROOT = 4.493015885730E+01
A = 0.70 L = 13 N = 6          ROOT = 5.4819762851932E+01
A = 0.70 L = 13 N = 7          ROOT = 6.4708382851931E+01
A = 0.70 L = 13 N = 8          ROOT = 7.4597799365733E+01
A = 0.70 L = 13 N = 9          ROOT = 8.533196829559E+01
A = 0.70 L = 13 N = 10         ROOT = 9.60704829559E+01
A = 0.70 L = 13 N = 11         ROOT = 1.059682147898E+02
A = 0.70 L = 13 N = 12         ROOT = 1.1632772727295E+02
A = 0.70 L = 13 N = 13         ROOT = 1.26682147898E+02
A = 0.70 L = 13 N = 14         ROOT = 1.3709811949791E+02
A = 0.70 L = 13 N = 15         ROOT = 1.4750172876892E+02
A = 0.70 L = 13 N = 16         ROOT = 1.5791438778798E+02
A = 0.70 L = 13 N = 17         ROOT = 1.683270285730E+02
A = 0.70 L = 13 N = 18         ROOT = 1.787605921890E+02
A = 0.70 L = 13 N = 19         ROOT = 1.891916895181E+02
A = 0.70 L = 13 N = 20         ROOT = 1.99621817948E+02
A = 0.70 L = 13 N = 21         ROOT = 2.1066521181595E+02
A = 0.70 L = 13 N = 22         ROOT = 2.2050841710259E+02
A = 0.70 L = 13 N = 23         ROOT = 2.3035181710259E+02
A = 0.70 L = 13 N = 24         ROOT = 2.4140856887827E+02
A = 0.70 L = 13 N = 25         ROOT = 2.5180987283673E+02
A = 0.70 L = 13 N = 26         ROOT = 2.622208285730E+02
A = 0.70 L = 13 N = 27         ROOT = 2.7375363961014E+02
A = 0.70 L = 13 N = 28         ROOT = 2.83207879784814E+02
A = 0.70 L = 13 N = 29         ROOT = 2.9366524257978E+02
A = 0.70 L = 13 N = 30         ROOT = 3.04119731214085E+02

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1 ROOTS OF EQUATION 3
A = 0.70 L = 14 N = 1          ROOT = 1.6298197881697E+01
A = 0.70 L = 14 N = 2          ROOT = 2.0952445718896E+01
A = 0.70 L = 14 N = 3          ROOT = 2.561411816199E+01
A = 0.70 L = 14 N = 4          ROOT = 3.15954328173151E+01
A = 0.70 L = 14 N = 5          ROOT = 4.5376231520936E+01
A = 0.70 L = 14 N = 6          ROOT = 5.9165248156199E+01
A = 0.70 L = 14 N = 7          ROOT = 7.5262476149881E+01
A = 0.70 L = 14 N = 8          ROOT = 7.53444871915635E+01
A = 0.70 L = 14 N = 9          ROOT = 8.25684115314295E+01
A = 0.70 L = 14 N = 10         ROOT = 9.038026115314295E+01
A = 0.70 L = 14 N = 11         ROOT = 1.0615784227057E+02
A = 0.70 L = 14 N = 12         ROOT = 1.168972161938E+02
A = 0.70 L = 14 N = 13         ROOT = 1.2864818811938E+02
A = 0.70 L = 14 N = 14         ROOT = 1.3724401239463E+02
A = 0.70 L = 14 N = 15         ROOT = 1.4633132148454E+02
A = 0.70 L = 14 N = 16         ROOT = 1.5540640625954E+02
A = 0.70 L = 14 N = 17         ROOT = 1.6845322625689E+02
A = 0.70 L = 14 N = 18         ROOT = 1.7882139575634E+02
A = 0.70 L = 14 N = 19         ROOT = 1.891916895181E+02
A = 0.70 L = 14 N = 20         ROOT = 1.9972731758454E+02
A = 0.70 L = 14 N = 21         ROOT = 2.1016142286732E+02
A = 0.70 L = 14 N = 22         ROOT = 2.206054286732E+02
A = 0.70 L = 14 N = 23         ROOT = 2.3163991936899E+02
A = 0.70 L = 14 N = 24         ROOT = 2.4148342065878E+02
A = 0.70 L = 14 N = 25         ROOT = 2.5222723553737E+02
A = 0.70 L = 14 N = 26         ROOT = 2.6237723553737E+02
A = 0.70 L = 14 N = 27         ROOT = 2.7282792716191E+02
A = 0.70 L = 14 N = 28         ROOT = 2.83207879784814E+02
A = 0.70 L = 14 N = 29         ROOT = 2.9371135225147E+02
A = 0.70 L = 14 N = 30         ROOT = 3.0418555971049E+02

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104

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1 ROOTS OF EQUATION 3
A = 0.70 L = 13 N = 1          ROOT = 1.53282013213E+01
A = 0.70 L = 13 N = 2          ROOT = 1.9875342432908E+01
A = 0.70 L = 13 N = 3          ROOT = 2.6597828576199E+01
A = 0.70 L = 13 N = 4          ROOT = 3.46204885738E+01
A = 0.70 L = 13 N = 5          ROOT = 4.493015885738E+01
A = 0.70 L = 13 N = 6          ROOT = 5.4819762851932E+01
A = 0.70 L = 13 N = 7          ROOT = 6.4708528517931E+01
A = 0.70 L = 13 N = 8          ROOT = 7.4597593657331E+01
A = 0.70 L = 13 N = 9          ROOT = 8.5331968295598E+01
A = 0.70 L = 13 N = 10         ROOT = 9.6178528517931E+01
A = 0.70 L = 13 N = 11         ROOT = 1.0596282147898E+02
A = 0.70 L = 13 N = 12         ROOT = 1.1632777272795E+02
A = 0.70 L = 13 N = 13         ROOT = 1.2668282147898E+02
A = 0.70 L = 13 N = 14         ROOT = 1.3705011949791E+02
A = 0.70 L = 13 N = 15         ROOT = 1.4750172876892E+02
A = 0.70 L = 13 N = 16         ROOT = 1.5795143877819E+02
A = 0.70 L = 13 N = 17         ROOT = 1.6831438808958E+02
A = 0.70 L = 13 N = 18         ROOT = 1.7876059218988E+02
A = 0.70 L = 13 N = 19         ROOT = 1.8919168851891E+02
A = 0.70 L = 13 N = 20         ROOT = 1.9952048217947E+02
A = 0.70 L = 13 N = 21         ROOT = 2.106662181585E+02
A = 0.70 L = 13 N = 22         ROOT = 2.20936471710259E+02
A = 0.70 L = 13 N = 23         ROOT = 2.31207181585E+02
A = 0.70 L = 13 N = 24         ROOT = 2.4140856887827E+02
A = 0.70 L = 13 N = 25         ROOT = 2.5167987283673E+02
A = 0.70 L = 13 N = 26         ROOT = 2.6195087283673E+02
A = 0.70 L = 13 N = 27         ROOT = 2.7237363961014E+02
A = 0.70 L = 13 N = 28         ROOT = 2.8220781784814E+02
A = 0.70 L = 13 N = 29         ROOT = 2.9366524257878E+02
A = 0.70 L = 13 N = 30         ROOT = 3.0411973214065E+02

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103

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1 ROOTS OF EQUATION 3
A = 0.70 L = 14 N = 1          ROOT = 1.6298197881697E+01
A = 0.70 L = 14 N = 2          ROOT = 2.0962445718896E+01
A = 0.70 L = 14 N = 3          ROOT = 2.5635228178131E+01
A = 0.70 L = 14 N = 4          ROOT = 3.5594328173131E+01
A = 0.70 L = 14 N = 5          ROOT = 4.5376231520936E+01
A = 0.70 L = 14 N = 6          ROOT = 5.5158231520936E+01
A = 0.70 L = 14 N = 7          ROOT = 6.502476181585E+01
A = 0.70 L = 14 N = 8          ROOT = 7.5344487915635E+01
A = 0.70 L = 14 N = 9          ROOT = 8.5568118991498E+01
A = 0.70 L = 14 N = 10         ROOT = 9.5792380542958E+01
A = 0.70 L = 14 N = 11         ROOT = 1.06157042627057E+02
A = 0.70 L = 14 N = 12         ROOT = 1.1648972161938E+02
A = 0.70 L = 14 N = 13         ROOT = 1.2682281811498E+02
A = 0.70 L = 14 N = 14         ROOT = 1.3724401239463E+02
A = 0.70 L = 14 N = 15         ROOT = 1.4837132784545E+02
A = 0.70 L = 14 N = 16         ROOT = 1.586032784545E+02
A = 0.70 L = 14 N = 17         ROOT = 1.6845322625689E+02
A = 0.70 L = 14 N = 18         ROOT = 1.7862339576384E+02
A = 0.70 L = 14 N = 19         ROOT = 1.8880447286732E+02
A = 0.70 L = 14 N = 20         ROOT = 1.9912731758454E+02
A = 0.70 L = 14 N = 21         ROOT = 2.1016142286732E+02
A = 0.70 L = 14 N = 22         ROOT = 2.21203614228673E+02
A = 0.70 L = 14 N = 23         ROOT = 2.3163991936899E+02
A = 0.70 L = 14 N = 24         ROOT = 2.4148342065878E+02
A = 0.70 L = 14 N = 25         ROOT = 2.5132287235537E+02
A = 0.70 L = 14 N = 26         ROOT = 2.6237723553737E+02
A = 0.70 L = 14 N = 27         ROOT = 2.7282792716191E+02
A = 0.70 L = 14 N = 28         ROOT = 2.8336624257878E+02
A = 0.70 L = 14 N = 29         ROOT = 2.937113223147E+02
A = 0.70 L = 14 N = 30         ROOT = 3.0418555971049E+02

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104

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1 ROOTS OF EQUATION 3
A = 0.20 L = 12 N = 1      ROOT = 1.4259349813425E+01
A = 0.20 L = 12 N = 2      ROOT = 1.927023748124E+01
A = 0.20 L = 12 N = 3      ROOT = 2.382751789409E+01
A = 0.20 L = 12 N = 4      ROOT = 3.03339508662646E+01
A = 0.20 L = 12 N = 5      ROOT = 3.3758938413442E+01
A = 0.20 L = 12 N = 6      ROOT = 3.6283244413442E+01
A = 0.20 L = 12 N = 7      ROOT = 4.04339037149726E+01
A = 0.20 L = 12 N = 8      ROOT = 4.37274993138406E+01
A = 0.20 L = 12 N = 9      ROOT = 4.60613849813442E+01
A = 0.20 L = 12 N = 10     ROOT = 5.0282048228276E+01
A = 0.20 L = 12 N = 11     ROOT = 5.1365483668873E+01
A = 0.20 L = 12 N = 12     ROOT = 5.250000000000E+01
A = 0.20 L = 12 N = 13     ROOT = 5.3566828564735E+01
A = 0.20 L = 12 N = 14     ROOT = 6.2729411926460E+01
A = 0.20 L = 12 N = 15     ROOT = 6.382751789409E+01
A = 0.20 L = 12 N = 16     ROOT = 6.339917588888E+01
A = 0.20 L = 12 N = 17     ROOT = 7.28789321787525E+01
A = 0.20 L = 12 N = 18     ROOT = 7.322329808954E+01
A = 0.20 L = 12 N = 19     ROOT = 8.0022817881494E+01
A = 0.20 L = 12 N = 20     ROOT = 8.0022817881494E+01
A = 0.20 L = 12 N = 21     ROOT = 8.3660047484341E+01
A = 0.20 L = 12 N = 22     ROOT = 8.356667790843E+01
A = 0.20 L = 12 N = 23     ROOT = 8.356667790843E+01
A = 0.20 L = 12 N = 24     ROOT = 9.472999219265E+01
A = 0.20 L = 12 N = 25     ROOT = 9.806238668025E+01
A = 0.20 L = 12 N = 26     ROOT = 9.822329808954E+01
A = 0.20 L = 12 N = 27     ROOT = 1.0600084832533E+02
A = 0.20 L = 12 N = 28     ROOT = 1.0600084832533E+02
A = 0.20 L = 12 N = 29     ROOT = 1.1356667790843E+02
A = 0.20 L = 12 N = 30     ROOT = 1.17378613153899E+02

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27

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1 ROOTS OF EQUATION 3
A = 0.20 L = 13 N = 1      ROOT = 1.53169738371BE+01
A = 0.20 L = 13 N = 2      ROOT = 1.448955202224E+01
A = 0.20 L = 13 N = 3      ROOT = 2.436261752268E+01
A = 0.20 L = 13 N = 4      ROOT = 2.8962136644515E+01
A = 0.20 L = 13 N = 5      ROOT = 3.174323230997E+01
A = 0.20 L = 13 N = 6      ROOT = 3.5035875699882E+01
A = 0.20 L = 13 N = 7      ROOT = 3.8417901558175E+01
A = 0.20 L = 13 N = 8      ROOT = 4.1751128800295E+01
A = 0.20 L = 13 N = 9      ROOT = 5.1594338229568E+01
A = 0.20 L = 13 N = 10     ROOT = 4.8343123230997E+01
A = 0.20 L = 13 N = 11     ROOT = 5.1594338229568E+01
A = 0.20 L = 13 N = 12     ROOT = 5.1594338229568E+01
A = 0.20 L = 13 N = 13     ROOT = 5.7973423832610E+01
A = 0.20 L = 13 N = 14     ROOT = 6.18813989748480E+01
A = 0.20 L = 13 N = 15     ROOT = 6.17474747474747E+01
A = 0.20 L = 13 N = 16     ROOT = 6.73286862336461E+01
A = 0.20 L = 13 N = 17     ROOT = 7.05956950541561E+01
A = 0.20 L = 13 N = 18     ROOT = 7.05956950541561E+01
A = 0.20 L = 13 N = 19     ROOT = 7.7428763999170E+01
A = 0.20 L = 13 N = 20     ROOT = 8.0949357986593E+01
A = 0.20 L = 13 N = 21     ROOT = 8.0949357986593E+01
A = 0.20 L = 13 N = 22     ROOT = 8.6148044594024E+01
A = 0.20 L = 13 N = 23     ROOT = 9.1881134736671E+01
A = 0.20 L = 13 N = 24     ROOT = 9.1881134736671E+01
A = 0.20 L = 13 N = 25     ROOT = 9.9184579769532E+01
A = 0.20 L = 13 N = 26     ROOT = 1.02967383384181E+02
A = 0.20 L = 13 N = 27     ROOT = 1.0600084832533E+02
A = 0.20 L = 13 N = 28     ROOT = 1.10461313018143E+02
A = 0.20 L = 13 N = 29     ROOT = 1.1416871908259E+02
A = 0.20 L = 13 N = 30     ROOT = 1.1794762446162E+02

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28

Robert L. Pexton and Arno D. Steiger, Degenerate Roots of Three Transcendental Equations Involving Spherical Bessel Functions, p. 1041

PAGE 1

```
61 80 X=X
62 81 ITOL=ITOL0
63 82 CALL INVOL(FUNC,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)
64 83 N=N+1
65 84 X=X1+N*DX
66 85 IF(N.EQ.10) 10,16
67 86 WRITE(15,10) N,X1,DX
68 87 10 WRITE(15,10) N,X1,DX
69 88 GO TO 17
70 89 17 WRITE(15,10) N,X1,DX,E20.13,E20.13
71 90 FORMAT(15A,12A,E20.13,12X,E20.13)
72 91 12X,E20.13
73 92 X=X1
74 93 X=X1+(N-30)*4,1
75 94 CONTINUE
76 95 4 WRITE(*,*)"ANSWER"
77 96 WRITE(*,*)"ADENO"
78 97 FORMAT(15A,12A,E20.13)
79 98 2 CALL EXIT
80 99 END
```

```

61      99 X2X
62      1 TOL=1E-10
63      2 N=MPL=MVPPOL(FUNC,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)
64      3 N=MPL=MVPPOL(FUNC,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)
65      4 F(M,EQD)=15,16
66      5 F(M,EQD)=15,16
67      10 WRITE(5,37) N,X1,ALF
68      11 READ(5,38) N,X2,ALF
69      12 GO TO 13
70      13 WRITE(5,39) N,X1,ALF
71      14 READ(5,40) N,X2,ALF
72      15 FORMA=(X1+X2)/2.0
73      16 E25=(X1-X2)/2.0
74      17 F1=F2
75      18 IF(F1.EQ.30) 4,1,1
76      19 PAENO=PAENO+1
77      20 PAENO=PAENO+1
78      21 PAENO=PAENO+1
79      22 CONTINUE
80      23 EXIT
81      END

```

```

91 C
92 C
93 C
94 C
95 C
96 C
97 C
98 C
99 C
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101 C
102 C
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141 C
142 C
143 C
144 C
145 C
146 C
147 C
148 C
149 C
150 C

SUBROUTINE NVPOL(FUN,X1,X2,XTOL,YTOL,ITOL,Y1,Y2)

      A STABLE METHOD OF INVERSE INTERPOLATION
      J.M.BLATT

      THE AUSTRALIAN COMPUTER JOURNAL
      VOL. 7 #2 JULY, 1975    PP 51-57

      METHOD
      AT EVERY STAGE OF THE ITERATION AT LEAST ONE ROOT
      IS GUARANTEED TO LIE WITHIN THE INTERVAL (X1,X2).
      IF CERTAIN CONDITIONS HOLD THE ROUTINE CALCULATES THE
      NEXT APPROXIMATION USING MULLER'S QUADRATIC POLYNOMIAL
      APPROXIMATION. OTHERWISE A LINEAR APPROXIMATION IS USED.
      "REDUCED VARIABLES" ARE USED FOR THE MULLER APPROXIMATION.

      INVERSE INTERPOLATION BY MODIFIED MULLER METHOD

      INPUT REQUIREMENTS
      FUN+FUNCTION NAME. WE WANT TO FIND X SUCH THAT F(X)=0
      NOTE THE ACTUAL NAME MUST BE DECLARED EXTERNAL IN THE
      CALLING PROGRAM.
      X1=X-VALUE AT ONE END OF INTERVAL
      X2=X-VALUE AT OTHER END OF INTERVAL
      BY ASSUMPTION, Y1 AND Y2 HAVE OPPOSITE SIGNS. ROUTINE
      CHECKS THIS, RETURNS WITH ITOL=-1 IF UNTRUE.
      XTOL=TOLERANCE ON ROOT, I.E. ON ABS(X1-X2) AT THE END
      YTOL=OPTIONAL TOLERANCE ON ABS(Y1), IGNORED IF =0
      ITOL=MAX NO. OF ITERATIONS. IF ITOL LE. 0, ITOL=60.

```

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151 C
152 C
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168 C
169 C
170 C
171 C
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173 C
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191 C
192 C
193 C
194 C
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196 C
197 C
198 C
199 C
200 C
201 C
202 C
203 C
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205 C
206 C
207 C
208 C
209 C
210 C

AFTER RETURN FROM ROUTINE
(X1,Y1) AND (X2,Y2) ARE THE BEST POINTS FOUND
ABS(Y1).LE.ABS(Y2)
(IF(Y1.NE.0) THEN Y1 AND Y2 HAVE OPPOSITE SIGNS
ITOL IS THE ACTUAL NO. OF ITERATIONS USED. IF THE
INITIAL POINTS WERE CHOSEN SO BADLY THAT Y1 AND Y2
HAD THE SAME SIGN, THEN ITOL IS SET TO -1, AND WE
EXIT IMMEDIATELY.
USER MUST SUPPLY
1. AN ACTUAL FUNCTION NAME TO REPLACE THE NOMINAL "FUN"
2. VALUES OF X1,X2,XTOL
3. OPTIONALY: VALUES OF YTOL,ITOL
4. FUNCTION SUBPROGRAM, OF DECLARED NAME, TO EVALUATE
FX(X).
5. WITHIN THE CALLING PROGRAM, AN "EXTERNAL" DECLARATION
FOR THAT FUNCTION NAME.
DIMENSION X(3),Y(3)
ITOL=1 SNTCH=1 SITER=0 SHULLER=0
YTOL=ABS(YTOL) SIF(ITOL.LE.0),ITOL=60
X(1)=X1 Y(1)=Y1 FUN=X(FUN,X,Y,ITOL)
X(2)=X2 Y(2)=Y2 SIFY1(Y1)YY(2)) 1100,9000,1050
1050,9000,1050
1100,IF(ABS(Y1)>YTOL.OR.ABS(X(1)-X(2)).LE.XTOL.OR.(ITER.GE.ITOL))
C GO TO 9000
TO DISPLAY INTERMEDIATE VALUES REMOVE THE "C" IN
COLUMN 1 OF THE FOLLOWING CARDS

```

```

211 C
212 C          DEBUG PRINTING
213 C
214 C      WRITE(3,223) I,K,ITER,MULLER,ITCH,NOTCH,MILLER,JJ
215 C
216 C      223 FORMAT(1X,I,K,ITER,MULLER,ITCH,NOTCH,MILLER,JJ
217 C     ,1X,(3.2424) X(1),X(2),X(3),XNEW
218 C     ,1X,(3.2424) Y(1),Y(2),Y(3),YNEW
219 C     ,1X,(3.2424) P(1),P(2),P(3),PNEW
220 C     ,1X,244 FORMAT(1X,4E26.13)
221 C
222 C      ITER=ITER+1 $MILLER=1 $ITCH(LE,0) GO TO 1150
223 C
224 C      1150 MILLER=2 $ITCH(MILLER-1,0) GO TO 2000
225 C      IF(ALPHA.LE.1.0) GO TO 1550 $IF(ALPHA.GE.1000.0) GO TO 2000
226 C      IF(BALPHA.LE.1.0) GO TO 1550 $IF(BALPHA.GE.1000.0) GO TO 2000
227 C      D1=ALPHA-1.0 $GAMMA=ALPHA/(ALPHA-BETA)/ALPHA/(ALPHA-1.0)
228 C      IF(BALPHA.GE.1.0) D1=BALPHA/(ALPHA-BETA)/ALPHA/(BALPHA-1.0)
229 C      IF(BALPHA.LT.1.0) D1=BALPHA/(ALPHA-BETA)/ALPHA/(ALPHA-1.0)
230 C      IF(BALPHA.EQ.1.0) D1=BALPHA/(ALPHA-BETA)/ALPHA/(ALPHA-1.0)
231 C      MILLER=MILLER-1 $MILLER=MILLER-1 GO TO 2000
232 C
233 C      1550 P1=ALPHA(1,1)-0.5*(ALPHA(1,1)-0.5)
234 C
235 C      PATH=REJOIN
236 C
237 C      2000 XNEW=X(1)+P1*(X(2)-X(1)) $YNEW=Y(1)+P1*(Y(2)-Y(1)) GO TO 9000
238 C      YNEW=Y(1)+P1*(Y(2)-Y(1))
239 C      XNEW=X(1)+P1*(X(2)-X(1))
240 C      C 0 TO 2010
241 C
242 C          A MULLER-TYPE ITERATION HAS PROVED UNSUCCESSFUL
243 C          INHIBIT MULLER-TYPE ITERATIONS FOR A FEW TIMES.
244 C          AND INHIBIT NUMBER OF INHIBITIONS FOR THE NEXT
245 C          SUCH OCCURRENCE.
246 C
247 C      ITCH=NOTCH
248 C      NOTCH=NOTCH1
249 C      IF(MILLER.EQ.1 OR ABS(Y(1)).GT.ABS(Y(1))) GO TO 2040
250 C
251 C      DISCARD POINT I
252 C
253 C      X(I)=XNEW   SY(I)=YNEW    900 TO 2060
254 C
255 C      PREPARE FOR SWITCHING LABELS I AND K.
256 C
257 C      2030 JJ=2
258 C
259 C      DISCARD POINT K
260 C
261 C      2040 X(K)=X(2)   SY(K)=Y(2)   SX(2)=XNEW   SY(2)=YNEW
262 C
263 C      TEST FOR PRECISE ROOT.
264 C
265 C      2060 IF(Y(2).EQ.0.0) GO TO 6000    900 TO (1100,2100),JJ
266 C
267 C      INTERCHANGE LABELS I AND K
268 C
269 C      2100 JJ=1   S1*K   SK-JJ    900 TO 1100

```

```

271 C      FINISHED
272 C      Y(2) WAS EXACTLY ZERO. SELECT THE BEST OTHER ONE.
273 C
274 C      8000 IF(ABS(Y(K)) LT ABS(Y(1))) I+K
275 C
276 C      REPORT NO. OF ITERATIONS USED.
277 C
278 C      9000 ITOL=ITER
279 C
280 C      REPORT THE TWO BEST POINTS FOUND.
281 C
282 C
283 C      9100 IF(ABS(Y(2)) LE ABS(Y(1))) GO TO 9200
284 C      9200 I1=2          I2=1
285 C      9200 I1=2          I2=1
286 C      9300 I1=Y(1)      SY1=Y(1)
287 C      9300 I2=Y(2)      SX2=X(I2)
288 C      RETURN
289 C      END

```

```

290 SUBROUTINE SJYMC(X,J,Y,MN,NOUT)
291 C          SJYMC(YSUBK)           SPHERICAL BESSSEL FUNCTIONS
292 C          FOR USE IN SJYMC
293 C          JSUBD(J,1), JSUB (0,1)   FOR ALL N>0, J>0
294 C          JSUBD(J,0), JSUB (0,0)   FOR ALL N>0, J=0
295 C          Y SUB N (X)*J SUB (-N+1) (X)  FOR ALL N>0, J>0
296 C          Y SUB N (X)*J SUB (-N+1) (X)  FOR ALL N>0, J=0
297 C          MN = MAXIMUM NUMBER OF TERMS COMPUTED
298 C          NOUT = MAXIMUM SUBSCRIPT OF DESIRED BESSEL FUNCTIONS
299 C          RECOMMENDED MAX. OF COMPS. BESSEL FUNCTIONS
300 C          REC'D. FROM HANDBOOK OF COMPS. BESSEL FUNCTIONS, VOL. 22 NO. 101 JAN. 1968
301 C          REC'D. FROM HANDBOOK OF COMPS. BESSEL FUNCTIONS, VOL. 22 NO. 101 JAN. 1968
302 C          DIMENSION J(0,900), Y(0,900)
303 C          THE DIMENSION OF AND M MAY BE VARIED TO SUIT THE USERS NEEDS
304 C          DATA MN/1000/, NMAXD/1000/, NMAXD/1000/
305 C          BOUND = MAX ALPHAL MNAD0 MAY BE VARIED
306 C          S1=MN/1000.0, S2=MN/1000.0, S3=MN/1000.0
307 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
308 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
309 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
310 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
311 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
312 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
313 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
314 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
315 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
316 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
317 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
318 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
319 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
320 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
321 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
322 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
323 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
324 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
325 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
326 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
327 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
328 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
329 C          MMN=1, S1=0.0, S2=1.0, S3=1.0, X=1.0
330 C          END

```

INPUT PARAMETERS  
LMIN \*1  
LMAX \*15  
DELX \*1.0  
XB \*1.0  
XTOL \*1.0E-12  
YTOL \*1.0  
IMIN \*1  
ITMAX \*7000  
ITOLG \*50  
END

L	H	MU <sub>MIN</sub>	ALPHA(MU <sub>MIN</sub> )
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L	H	MU <sub>MIN</sub>	ALPHA( MU <sub>MIN</sub> )
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L	N	MU MIN	ALPHAC ( MU ) MIN
1			
2		3.464101615137E+00	1.00000000000000E+00
3		6.259125000000E+00	4.199525926762E-01
4		1.136351250000E+01	2.365248266725E-01
5		1.4951883839379E+01	2.3168328936360E-01
6		1.89186163355E+01	1.8955919680354E-01
7		2.13790168800E+01	1.628205000000E-01
8		2.4563389747161E+01	1.4162705996219E-01
9		2.7378935817874E+01	1.248869467399E-01
10		3.030000000000E+01	1.120000000000E-01
11		3.4968245414779E+01	1.0168109353786E-01
12		3.7227419364840E+01	9.2052446352981E-02
13		4.000000000000E+01	8.377393283477E-02
14		4.353795367159E+01	7.9565092728738E-02
15		4.690419458895E+01	7.41929537474566E-02
16		5.020000000000E+01	6.959000000000E-02
17		5.3991497379836E+01	6.5370894952645E-02
18		5.6149515397026E+01	6.1784129195183E-02
19		5.832000000000E+01	5.842000000000E-02
20		6.2436256273112E+01	5.4621765864993E-02
21		6.559327656217E+01	5.2819892136715E-02
22		7.1875819128173E+01	4.8195647119658E-02
23		7.5821590164527E+01	4.6174784662274E-02
24		7.816100000000E+01	4.431274462222E-02
25		8.1311911277167E+01	4.2682674235578E-02
26		8.4456712323731E+01	4.1016397174419E-02
27		8.757000000000E+01	3.950000000000E-02
28		9.0745646366509E+01	3.8173743926539E-02
29		9.3889824345461E+01	3.69549281816E-02
30		9.7034934253148E+01	3.5623353407670E-02

L	N	MU MIN	ALPHA( MU MIN )
1	2	4.4721359549396E+00	4.00000000000000E+00
2	9	9.4781976654249E+00	4.7181400398887E-01
3	1	1.2958171568693E+01	3.451209932677E-01
4	1	1.6058171568693E+01	2.458639932677E-01
5	1	1.9538375156604E+01	2.20895399326583E-01
6	2	2.2761299915211E+01	1.9647981317670E-01
7	2	2.5161299915211E+01	1.7224775681752E-01
8	2	2.75161299915211E+01	1.5323888027569E-01
9	3	3.23709825735660E+01	1.39232888027569E-01
10	3	3.55031259562656E+01	1.2596456884171E-01
11	3	3.80215000000000E+01	1.153622888027569E-01
12	4	4.1833471609331E+01	1.06903129495628E-01
13	4	4.49936173405966E+01	9.9394896860734E-02
14	4	4.81620000000000E+01	9.2602888027569E-02
15	5	5.130629917835E+01	8.7164347385238E-02
16	5	5.4461046426702E+01	8.2116232581364E-02
17	5	5.75300000000000E+01	7.7623888027569E-02
18	6	6.065241961533E+01	7.3596542542541E-02
19	6	6.391577521421E+01	6.9969203198224E-02
20	6	6.727546421421E+01	6.6883139403897E-02
21	7	7.062149963598E+01	6.4035053905485E-02
22	7	7.3362756393986E+01	6.0959213307495E-02
23	7	7.61620000000000E+01	5.8451249582142E-02
24	7	7.89578988600000E+01	5.61412000000000E-02
25	8	8.2804656214597E+01	5.4008266677835E-02
26	8	8.5951117776520E+01	5.2031157513848E-02
27	8	8.91600000000000E+01	5.01316600000000E-02
28	9	9.224304264632E+01	4.8482095287643E-02
29	9	9.5388578535454E+01	4.688372677398E-02
30	9	9.9333847377662E+01	4.5386733027795E-02

L	N	MU	MIN	ALPHAC ( MU / MIN )
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L	N	HU	MIN	ALPHA(HU, MIN)
1	6	6.4897465384675E+00	1.6888680808359E+00	
2	1	1.1851781741945E+01	5.4651934231053E-01	
3	1	1.5471105805866E+01	4.1089317530653E-01	
4	1	1.8884251311760E+01	3.4318229467565E-01	
5	1	2.2120351111111E+01	2.9102050000000E-01	
6	1	2.54789653996106E+01	2.5435652326360E-01	
7	1	2.8720864399464E+01	2.256524967151E-01	
8	1	3.2000000000000E+01	2.0200000000000E-01	
9	1	3.5145315382438E+01	1.84398422037397E-01	
10	1	3.8339638399580E+01	1.6903503323450E-01	
11	1	4.1533333333333E+01	1.5600000000000E-01	
12	1	4.4705232223961E+01	1.4496607235110E-01	
13	1	4.7874663669526E+01	1.3535476654846E-01	
14	1	5.1043333333333E+01	1.2600000000000E-01	
15	1	5.4216857297414E+01	1.1913368415520E-01	
16	1	5.7384929891871E+01	1.1294241485759E-01	
17	1	6.0557575757576E+01	1.0700000000000E-01	
18	1	6.37031105481E+01	1.0173478129394E-01	
19	1	6.6869270595918E+01	9.6929520601796E-02	
20	1	7.0036666666667E+01	9.2949000594968E-02	
21	1	7.3171925471684E+01	8.8356670000000E-02	
22	1	7.6325971556570E+01	8.4906721975491E-02	
23	1	7.9479822222222E+01	8.1545253496757E-02	
24	1	8.2633011701333E+01	7.8200000000000E-02	
25	1	8.5783594598244E+01	7.5049434140532E-02	
26	1	8.8936813321518E+01	7.2971932263274E-02	
27	1	9.2087368133215E+01	7.0900000000000E-02	
28	1	9.5232866397760E+01	6.885513119175E-02	
29	1	9.8381665175299E+01	6.5973326215765E-02	
30	1	1.0153046235656E+02	6.3035142850987E-02	

L	N	MU	MIN	ALPHA(MU)	MIN
1		7.4613147735479E+00		1.00000000000000E+00	
2		1.2918495915693E+01		5.74695365374E-01	
3		1.6704189051383E+01		4.47398365374E-01	
4		2.6161987891912E+01		3.7115957085510E-01	
5		2.5111111111111E+01		3.18065360742E-01	
6		6.8152853424091E+01		2.70865360742E-01	
7		3.0876912381547E+01		2.408059511734E-01	
8		3.1311111111111E+01		2.408059511734E-01	
9		1.6533417591332E+01		2.408059511734E-01	
10		3.5739871252634E+01		2.408059511734E-01	
11		4.2428571428571E+01		1.8832747402212E-01	
12		4.6125891259546E+01		1.7428646872478E-01	
13		4.3307592759392E+01		1.6218646872478E-01	
14		2.2628571428571E+01		1.5176881143421E-01	
15		3.6583128931832E+01		1.44596271149E-01	
16		5.882811619801E+01		1.34596271149E-01	
17		1.299190361422E+01		1.2729635680545E-01	
18		4.5346458333333E+01		1.2070326186802E-01	
19		6.9321737479449E+01		1.1408561943750E-01	
20		1.1861111111111E+01		1.0951651034159E-01	
21		4.0931651569034E+01		1.080865365374E-01	
22		7.779839528053E+01		9.6168549283209E-02	
23		6.69152614341E+01		9.243845676865E-02	
24		4.1095621428571E+01		8.8993845676865E-02	
25		8.7263712861522E+01		8.5755172776376E-02	
26		9.0416921426901E+01		8.2764538489690E-02	
27		9.7370063971536E-02		7.9310063971536E-02	
28		9.6721054747668E+01		7.7370063971536E-02	
29		9.9672124576533E+01		7.4928561194415E-02	
30		1.0302261275985E+02		7.2637594534627E-02	

L	N	MU	MIN	ALPHR( MU, MIN )
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L	N	MU MIN	ALPHA( MU MIN )
1		9.48603290051E+00	1.69660000000000E+00
2		1.332151467073E+01	6.191615441721E-01
3		1.9133229617683E+01	4.9583019542004E-01
4		2.5713229617683E+01	4.16200000000000E-01
5		3.6998835544975E+01	3.6349625182646E-01
6		2.9449432182122E+01	3.2215656979386E-01
7		3.7232059081947E+01	2.989545623811E-01
8		3.6924422859098E+01	2.63130000000000E-01
9		3.9273728542659E+01	2.155671025737E-01
10		4.2203728542659E+01	2.318597102538E-01
11		4.57246374095771E+01	2.07000000000000E-01
12		4.8933952948786E+01	1.9367371950766E-01
13		2.4123591961852E+01	1.8137188508319E-01
14		3.3255917619630E+01	1.77000000000000E-01
15		5.8513210276761E+01	1.6213147314313E-01
16		6.1593536757427E+01	1.5376624689395E-01
17		6.46438536757427E+01	1.46200000000000E-01
18		6.80408987040877E+01	1.3941199874684E-01
19		7.12207625844232E+01	1.3320319220005E-01
20		7.43400000000000E+01	1.27300000000000E-01
21		7.75569706102989E+01	1.2232082352511E-01
22		8.0721917101271E+01	1.1752487206917E-01
23		8.3936665678951E+01	1.13800000000000E-01
24		8.7046665678951E+01	1.0899559553759E-01
25		9.0206933468421E+01	1.0516756454673E-01
26		9.3366665678951E+01	1.01000000000000E-01
27		9.6523492880018E+01	9.5295223300000E-02
28		9.9680218624680E+01	9.512674291830E-02
29		1.0283580553925E+02	9.2252652763986E-02
30		1.0599059454547E+02	9.398666594675E-02

L	N	MU MIN	ALPHA(MU MIN)
1	1	1.0408889849171E+01	1.000000000000E+00
2	1	1.6467729438165E+01	6.3715459613566E-01
3	2	2.0332114908595E+01	5.1503854059722E-01
4	2	2.3332114908595E+01	4.3636854059528E-01
5	2	2.737198861534E+01	3.8316877948100E-01
6	3	3.6747430419442E+01	3.411045210819E-01
7	3	4.0047430419442E+01	3.0781153772748E-01
8	3	4.3625252118232E+01	2.801000000000E-01
9	4	4.8627312989315E+01	2.501536143507E-01
10	4	4.3013648016149E+01	2.339517237137E-01
11	4	7.013214616149E+01	2.227029981392E-01
12	5	5.83219542648296E+01	2.0041978528141E-01
13	5	2.253219542648296E+01	1.9500233388171E-01
14	5	2.253219542648296E+01	1.9486233388171E-01
15	5	5.3927089980747E+01	1.7501437974414E-01
16	5	5.1695728059595E+01	1.661984646214E-01
17	5	6.33685728059595E+01	1.591984646214E-01
18	6	5.9481279849764E+01	1.50948406559705E-01
19	6	1.2545371859615E+01	1.44346803963961E-01
20	7	7.0933769984153E+00	1.39364832337139E-01
21	7	7.9083769984153E+01	1.3275427848323E-01
22	8	2.172832981545E+01	1.2763450037139E-01
23	8	5.37332981545E+01	1.2236450037139E-01
24	8	8.05649891668395E+01	1.1850275386217E-01
25	9	1.1668583085969E+01	1.1441321869321E-01
26	9	3.483085969E+01	1.10864832337139E-01
27	9	7.791244717655E+01	1.023389113481E-01
28	10	1.0115874486669E+02	1.0366770388715E-01
29	10	1.043015128548E+02	1.0054811445864E-01
30	10	1.0746250176917E+02	9.7291370711234E-02

L	N	MU MIN	ALPHAC(MU MIN)
1		1.469125293075E+01	1.0669600032600E+00
2		1.753591359135E+01	6.559489523623E-01
3		2.1522124707610E+01	3.338265810140E-01
4		2.5149592872795E+01	4.568243925837E-01
5		2.869312405100E+01	4.010126250000E-01
6		3.2036803298239E+01	3.5863166781735E-01
7		3.538240318911E+01	3.2471296628956E-01
8		3.868510308000E+01	2.965410000000E-01
9		4.197071359135E+01	2.7674100021769E-01
10		4.529735791369E+01	2.5401707736282E-01
11		4.842408100000E+01	2.337410000000E-01
12		5.1791403568413E+01	2.2222076141735E-01
13		5.4919561782279E+01	2.0919761995871E-01
14		5.8116661782279E+01	1.976426860000E-01
15		6.1132132305535E+01	1.874630000000E-01
16		6.4528350793298E+01	1.7604771315932E-01
17		6.77490397617E+01	1.695510000000E-01
18		7.094200000000E+01	1.632000000000E-01
19		7.4088164627861E+01	1.5507369255467E-01
20		7.726748953942E+01	1.4663344264283E-01
21		8.044626347250E+01	1.420252800000E-01
22		8.3616626389867E+01	1.3740241161933E-01
23		8.678764082812E+01	1.323985376564E-01
24		9.000000000000E+01	1.278534930000E-01
25		9.3123959426059E+01	1.2337501987674E-01
26		9.6268536315992E+01	1.1931926628867E-01
27		9.940300000000E+01	1.15321158562E-01
28		1.0261518163394E+02	1.1195321158562E-01
29		1.05767635415637E+02	1.0861714212698E-01
30		1.0893638015358E+02	1.0546637658493E-01

I	L	N	MU	MIN	ALPHA( MU )	MIN
1			1.24999599677E+01		1.08898999999999E+00	
2			1.8719291949984E+01		6.6722597245416E-01	
3			2.2784186752287E+01		5.5811862495906E-01	
4			2.5313621866610E+01		4.7452081717170E-01	
5			2.9988430719627E+01		4.1789712171765E-01	
6			3.314952818170E+01		3.74996169865946E-01	
7			3.6606214815000E+01		3.4686787663646E-01	
8			4.0698521481506E+01		3.1781908863646E-01	
9			4.3394753559256E+01		2.8842090804876E-01	
10			4.5537500000000E+01		2.6815716516346E-01	
11			4.9821989054043E+01		2.5000000000000E-01	
12			5.2671918612461E+01		2.3534095475237E-01	
13			5.3830618650000E+01		2.1846659865532E-01	
14			5.95186606500193E+01		2.0999999999999E-01	
15			6.2728531359433E+01		1.9911061336310E-01	
16			6.5852232741610E+01		1.8943545398171E-01	
17			6.91299132327416E+01		1.8089999999999E-01	
18			7.3222392569360E+01		1.7269887727137E-01	
19			7.5518420198360E+01		1.6540746537156E-01	
20			7.8652640198360E+01		1.5920000000000E-01	
21			8.1875567504576E+01		1.5254951265805E-01	
22			8.409882367670E+01		1.4684891048105E-01	
23			8.6228652367670E+01		1.4120000000000E-01	
24			9.1481492802955E+01		1.3664989312436E-01	
25			9.4572234625252E+01		1.3206935414713E-01	
26			9.7711893246252E+01		1.2747777777777E-01	
27			1.0099808295137E+02		1.237752147325E-01	
28			1.0407358631816E+02		1.2001120013985E-01	
29			1.07234718668E+02		1.1647023762355E-01	
30			1.1048043718668E+02		1.131317359825E-01	

L	N	MU_MIN	ALPHR( MU_MIN )
1	2	1.3490737563232E+01	1.49898000000000E+00
3	1.9840075472633E+01	6.7997410507095E-01	
4	2.3879866798254E+01	5.6496638677893E-01	
5	2.7179866798254E+01	4.9999999999999E-01	
6	3.113390128349E+01	4.3332654432298E-01	
7	3.4585144559203E+01	3.9867318707396E-01	
8	3.7712656250000E+01	3.552629611331E-01	
9	4.1316276638259E+01	3.2028053632983E-01	
10	4.4629898489254E+01	3.0228053632983E-01	
11	4.7714866798254E+01	2.8124807765595E-01	
12	5.1101826404521E+01	2.6323606281111E-01	
13	5.4431953936802E+01	2.4793681117295E-01	
14	5.7712100000000E+01	2.3352100000000E-01	
15	6.0893151945520E+01	2.2105134210000E-01	
16	6.4117765566596E+01	2.1046560980158E-01	
17	6.733927288618E+01	2.0337160296596E-01	
18	7.3731653022570E+01	1.9312000000000E-01	
19	7.62952542681E+01	1.8257077328513E-01	
20	8.0115161163175E+01	1.737449344431E-01	
21	8.3808951163175E+01	1.6395178296110E-01	
22	8.687469326714E+01	1.5592909590164E-01	
23	9.0000000000000E+01	1.5000000000000E-01	
24	9.283994591396E+01	1.4531177954336E-01	
25	9.6014465364295E+01	1.4050731524571E-01	
26	9.9190000000000E+01	1.3636363636363E-01	
27	1.0235735013907E+02	1.3198037328927E-01	
28	1.055260593395E+02	1.2784271444624E-01	
29	1.08688837636E+02	1.24156245592E-01	
30	1.118588837636E+02	1.20605054451E-01	

L	N	MU <sub>MIN</sub>	ALPHA(MU <sub>MIN</sub> )
1			
2		1.4491376745189E+01	1.000000000000000E+00
3		2.8935981174632E+01	6.9151586796219E-01
4		2.5847492460015E+01	5.7055598796259E-01
5		2.8704526596501E+01	5.6323277300943E-01
6		3.1704538852054E+01	4.4632277300943E-01
7		3.5847125957254E+01	4.0425491191689E-01
8		3.9256941529540E+01	3.6914173467155E-01
9		4.2120514778254E+01	3.4046339052054E-01
10		4.5946633936592E+01	3.1539579314345E-01
11		4.9246332618135E+01	2.9425947523603E-01
12		5.2379542475376E+01	2.7710591754337E-01
13		5.57879512475376E+01	2.5975817543377E-01
14		5.9835946320544E+01	2.4546760187554E-01
15		6.422086472707E+01	2.3124581656279E-01
16		6.549986472707E+01	2.2124581656279E-01
17		6.67115229632E+01	2.1068348032594E-01
18		7.1320514778254E+01	2.010000000000000E+00
19		7.5133752152641E+01	1.928439174959E-01
20		7.833353948251E+01	1.8495951222443E-01
21		8.15012965217E+01	1.7710591754337E-01
22		8.4719612695217E+01	1.705162647038E-01
23		8.7386320679630E+01	1.6484969986C45E-01
24		9.1000000000000E+01	1.593000000000000E+00
25		9.4272086002016E+01	1.5371863889997E-01
26		9.7459581359116E+01	1.4879487732439E-01
27		1.006666666666666E+02	1.440112500000000E-01
28		1.038006616509E+02	1.395411250000000E-01
29		1.0697271554632E+02	1.3546797117293E-01
30		1.1014296701515E+02	1.3155878780719E-01
		1.1331153535393E+02	1.276096180345E-01

L	N	MU MIN	ALPHA( MU MIN )
1			
2		1.5421933384839E+01	1.66909606233979E+00
3		2.209991640522E+01	7.8528262333972E-01
4		2.6209991640542E+01	5.9106597761828E-01
5		2.9953133246059E+01	5.1651605674292E-01
6		3.32530133246059E+01	4.6161605674292E-01
7		3.7101526532979E+01	4.175512501405E-01
8		4.853219931443E+01	3.8221299142492E-01
9		4.4129931443E+01	3.9221299142492E-01
10		4.725662199729E+01	3.2763273651566E-01
11		5.0569791001176E+01	3.06340758574489E-01
12		5.390301176E+01	2.697140529497232E-01
13		5.7134330119308E+01	2.71140529497232E-01
14		6.0392396499268E+01	2.5652129817759E-01
15		6.35386499268E+01	2.4349868016681E-01
16		6.6972917252295E+01	2.311666666666666E-01
17		7.095096531267E+01	2.2100897504626E-01
18		7.211666666666666E+01	2.1129983904626E-01
19		7.42093460522E+01	2.0242093460522E-01
20		7.573481028090E+01	1.9429132436081E-01
21		8.0255575721308E+01	1.9679471111608E-01
22		8.9323998739140E+01	1.7953161114352E-01
23		9.2512649652752E+01	1.7343528731584E-01
24		9.5393649652752E+01	1.6749646162017E-01
25		9.8880665446206E+01	1.6889646162017E-01
26		1.02686653071817E+02	1.5667302921012E-01
27		1.06086653071817E+02	1.5179547214578E-01
28		1.0841369795499E+02	1.471086653071817E-01
29		1.115820182862E+02	1.4289545752386E-01
30		1.1475891530649E+02	1.3883252856925E-01