

## The First Occurrence of Certain Large Prime Gaps

By Richard P. Brent

**Abstract.** The first occurrence of a string of  $2r - 1$  consecutive composite numbers between two primes (denoted by  $f(r)$  and  $f(r) + 2r$ ) is tabulated for  $f(r)$  in the range  $2.6 \times 10^{12} < f(r) \leq 4.444 \times 10^{12}$ . This extends earlier computations in the range  $f(r) \leq 2.6 \times 10^{12}$ .

Let  $p_1 = 2, p_2 = 3, \dots$  be the sequence of primes. For integer  $r \geq 1$ , define

$$f(r) = \begin{cases} p_j & \text{if } j \geq 1 \text{ is minimal such that } p_{j+1} - p_j = 2r, \\ \infty & \text{if no such } j \text{ exists.} \end{cases}$$

See [1] and [3] for a discussion of the asymptotic behavior of  $f(r)$ , and for additional references. All  $f(r) \leq 2.6 \times 10^{12}$  are tabulated in [1] and [2]. In Table 1 we give all eleven values of  $f(r)$  in the range  $2.6 \times 10^{12} < f(r) \leq 4.444 \times 10^{12}$ .

The maximal gap has  $r = 326$ , i.e.  $p_{j+1} - p_j \leq 652$  for all  $p_j \leq 4.444 \times 10^{12}$ , and  $p_{j+1} - p_j = 652$  for  $p_j = 2,614,941,710,599$ . The minimal  $r$  for which  $f(r)$  is still unknown is  $r = 268$ , and the next is  $r = 279$ .

The computation of Table 1 was performed over the period April 1973 to September 1978, on an IBM 360/50 computer with 256K bytes of memory. The method used was the same as that described in [1], except that the sieve size had to be reduced to fit into the 208K bytes available. About 61 seconds were required to sieve each block of 2,661,120 numbers near  $3 \times 10^{12}$ .

TABLE 1

$r$	$f(r)$	$r$	$f(r)$
271	2707053887651	285	4442109925217
272	2652427555639	287	3108794067079
274	3380058341279	296	3410069454097
277	3621153039299	309	4165633395149
278	4338624362173	326*	2614941710599
280	4260199366373		

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Department of Computer Science  
Australian National University  
Canberra, A.C.T. 2600, Australia

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