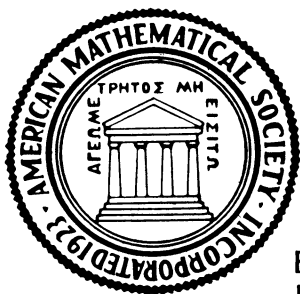


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October 1982

Volume 39, Number 160, Pages 309–775

**Published by the American Mathematical Society
Providence, Rhode Island USA**

ISSN 0025-5718

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MATHEMATICS OF COMPUTATION is published quarterly by the American Mathematical Society, 201 Charles Street, Providence, RI 02904. Second-class postage is paid at Providence, Rhode Island, and additional mailing offices. Postmaster: Send address changes to Mathematics of Computation, American Mathematical Society, P. O. Box 6248, Providence, RI 02940.

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