

Rational Chebyshev Approximations for the Bessel Functions $J_0(x)$, $J_1(x)$, $Y_0(x)$, $Y_1(x)$ *

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Abstract. This report presents near-minimax rational approximations for the Bessel functions $J_0(x)$, $J_1(x)$, $Y_0(x)$, and $Y_1(x)$ for the complete range of x , with relative errors ranging down to 10^{-23} . The first thirty zeros of each function are listed to 35D. The tabulated zeros and the McMahon asymptotic formulae may be used to construct an algorithm which retains relative accuracy in the neighborhood of zeros.

1. Introduction. The Bessel functions of the first and second kinds $J_0(x)$, $J_1(x)$, $Y_0(x)$, and $Y_1(x)$ are among the most commonly used functions in scientific computations, and efficient approximations have wide applicability.

Chebyshev series expansion coefficients are given to 20D in [3] for the ranges $|x| \leq 8$ and $x \geq 8$; in [10] for the ranges $|x| \leq 8$ and $x \geq 5$; and to 15D in [14] for $|x| \leq 5$. [7] contains rational minimax approximations for $|x| \leq 8$ and $x \geq 8$ with absolute errors ranging down to 10^{-25} . [4] contains unpublished rational minimax approximations to $J_0(x)$ and $J_1(x)$ for $|x| \leq 4$ and $4 \leq x \leq 8$, and to $Y_\nu(x)$ for $0 \leq \nu \leq 1$ [5]. A number of other approximations are listed in [10].

The present report gives rational minimax approximations to $J_0(x)$, $J_1(x)$, $Y_0(x)$, and $Y_1(x)$ for small values of x , and to the modulus and phase for larger arguments. An advantage of using the modulus and phase is that fewer function evaluations are necessary. For example, the computation of $J_0(x)$ for $x \geq 8$ by the formulae in [7] involves the computation of $P(x)$, $Q(x)$, $\sin \chi$ and $\cos \chi$, whereas the modulus-phase approach involves the computation of $M(x)$, $\theta(x)$ and $\cos \theta$.

Following Cody [4] we have factored the zeros of the function out of the rational approximation wherever possible, thereby providing a form which retains relative accuracy in the neighborhood of zeros. For the remaining ranges, accurate zeros are either listed in the report or are obtainable by the McMahon asymptotic formulae, and a Taylor expansion about each zero provides full relative accuracy in a neighborhood containing the zero. Thus the methods described here provide $J_0(x)$, $J_1(x)$, $Y_0(x)$, and $Y_1(x)$ with full relative accuracy for the complete range of the argument.

2. Functional Properties. $J_n(x)$ and $Y_n(x)$ are linearly independent solutions of the differential equation

$$x^2 y'' + xy' + (x^2 - n^2)y = 0.$$

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Ascending series, given in [1], are

$$(1) \quad J_n(x) = (x/2)^n \sum_{k=0}^{\infty} \frac{(-x^2/4)^k}{k!(n+k)!},$$

$$(2) \quad Y_n(x) = -\frac{(x/2)^{-n}}{\pi} \sum_{k=0}^{n-1} \frac{(n-k-1)!}{k!} (x^2/4)^k + \frac{2}{\pi} \ln(x/2)J_n(x) \\ - \frac{(x/2)^n}{\pi} \sum_{k=0}^{\infty} [\psi(k+1) + \psi(n+k+1)] \frac{(-x^2/4)^k}{k!(n+k)!},$$

where $\psi(n) = -\gamma + \sum_{k=1}^{n-1} k^{-1}$ and γ is Euler's constant.

The modulus and phase are defined in [1] as

$$(3) \quad M_n(x) = [J_n^2(x) + Y_n^2(x)]^{1/2},$$

$$(4) \quad \theta_n(x) = \arctan[Y_n(x)/J_n(x)],$$

so that $J_n(x) = M_n \cos \theta_n$ and $Y_n(x) = M_n \sin \theta_n$.

An asymptotic formula for M_n for large argument is given in [1];

$$(5) \quad M_n^2 \sim \frac{2}{\pi x} \left(1 + \sum_{k=1}^{\infty} a_k x^{-2k} \right),$$

where

$$a_k = \frac{1 \cdot 3 \cdot 5 \cdots (2k-1)}{2 \cdot 4 \cdot 6 \cdots 2k} \frac{(\mu-1^2)(\mu-3^2) \cdots [\mu-(2k-1)^2]}{2^{2k}} \quad \text{and} \\ \mu = 4n^2.$$

The corresponding asymptotic formula for θ_n is

$$(6) \quad \theta_n \sim x - (n/2 + 1/4)\pi + \sum_{k=1}^{\infty} b_k x^{-2k+1}.$$

An explicit formula for b_k is not known, but a recursive formula can be developed by substituting (5) and (6) in the identity $M_n^2 \theta'_n = 2/(\pi x)$.

The resulting formula is

$$(7) \quad b_k = \left[a_k - \sum_{n=1}^{k-1} (2n-1)a_{k-n}b_n \right] / (2k-1).$$

If \mathcal{C} denotes either J or Y , the derivatives with respect to x are given by

$$(8) \quad \mathcal{C}'_0 = -\mathcal{C}_1, \quad x\mathcal{C}'_1 = x\mathcal{C}_0 - \mathcal{C}_1.$$

Repeated differentiation gives the following formulae for the k th derivatives

$$(9) \quad \mathcal{C}_0^{(k)} = -\mathcal{C}_1^{(k-1)}, \quad \mathcal{C}_1^{(k)} = -\frac{k}{x}\mathcal{C}_1^{(k-1)} + \mathcal{C}_0^{(k-1)} + \frac{(k-1)}{x}\mathcal{C}_0^{(k-2)},$$

for $k = 1, 2, 3, \dots$

The Wronskian

$$(10) \quad J_1(x)Y_0(x) - J_0(x)Y_1(x) = 2/(\pi x)$$

is often used for checking computations.

The McMahon asymptotic expansions for the zeros of $J_n(x)$ and $Y_n(x)$ are [1]

$$(11) \quad j_{n,s}, y_{n,s} \sim \beta + \sum_{k=1}^{\infty} c_k \beta^{-2k+1},$$

where $\beta = (s + n/2 - 1/4)\pi$ for $j_{n,s}$, $\beta = (s + n/2 - 3/4)\pi$ for $y_{n,s}$.

Expressions for c_1, c_2, \dots, c_7 are listed in [13], but a general formula for c_k is not known. The c_k may be computed in terms of the b_k by the following algorithm

$$(12) \quad c_k = -b_k - \sum_{l=1}^{k-1} b_{k-l} \times \sum_{i=1}^l \frac{(-2k + 2l + 1)(-2k + 2l) \cdots (-2k + 2l + 2 - i)}{i!} c_{i,l},$$

for $k = 1, 2, 3, \dots$, where $c_{1,k} \equiv c_k$ and

$$c_{k+1,l} = \sum_{i=1}^{l-k} c_i c_{k,l-i}, \quad l = k + 1, k + 2, k + 3, \dots, k = 1, 2, 3, \dots$$

(7) and (12) are particular cases of the algorithm in [6].

The derivatives of J_n and Y_n at the zeros may be computed from the formulae

$$J'_n(j_{n,s}) = (-1)^s 2 / [\pi j_{n,s} M_n(j_{n,s})],$$

$$Y'_n(y_{n,s}) = (-1)^{s-1} 2 / [\pi y_{n,s} M_n(y_{n,s})],$$

and (9).

3. Generation of Approximations. Rational minimax approximations to $J_n(x)$, $Y_n(x)$, $M_n(x)$, and $\theta_n(x)$ were computed in 29S arithmetic on a CDC 6600/CYBER 170 Model 175 computer system using a version of the second algorithm of Remes due to Ralston [9]. The error of the approximations was levelled to three digits in most cases.

The approximation forms and intervals are:

$$(13) \quad \begin{aligned} J_0(x) &\simeq (x^2 - j_{0,1}^2)(x^2 - j_{0,2}^2)(x^2 - j_{0,3}^2)(x^2 - j_{0,4}^2)R_{lm}(x^2), & 0 \leq x \leq 14, \\ &= M_0(x)\cos \theta_0(x), & x \geq 14, \\ Y_0(x) &\simeq (x^2 - j_{0,1}^2)\ln \frac{x}{y_{0,1}} R_{lm}(x^2) + (x^2 - y_{0,1}^2)S_{lm}(x^2), & 0 < x \leq 3.5, \\ &= M_0(x)\sin \theta_0(x), & x \geq 3.5, \\ M_0(x) &\simeq x^{-1/2}R_{lm}(1/x^2), & 3.5 \leq x \leq 14 \text{ and } x \geq 14, \\ \theta_0(x) &\simeq x - \frac{\pi}{4} + x^{-1}S_{lm}(1/x^2), & 3.5 \leq x \leq 14 \text{ and } x \geq 14, \\ J_1(x) &\simeq x(x^2 - j_{1,1}^2)(x^2 - j_{1,2}^2)(x^2 - j_{1,3}^2)(x^2 - j_{1,4}^2)R_{lm}(x^2), & 0 \leq x \leq 14, \\ &= M_1(x)\cos \theta_1(x), & x \geq 14, \\ Y_1(x) &\simeq x(x^2 - j_{1,1}^2)\ln \frac{x}{y_{1,1}} R_{lm}(x^2) + \frac{(x^2 - y_{1,1}^2)}{xy_{1,1}^2} S_{lm}(x^2), & 0 < x \leq 5, \\ &= M_1(x)\sin \theta_1(x), & x \geq 5, \\ M_1(x) &\simeq x^{-1/2}R_{lm}(1/x^2), & 5 \leq x \leq 14 \text{ and } x \geq 14, \\ \theta_1(x) &\simeq x - \frac{3\pi}{4} + x^{-1}S_{lm}(1/x^2), & 5 \leq x \leq 14 \text{ and } x \geq 14, \end{aligned}$$

where $R_{lm}(x)$ and $S_{lm}(x)$ are rational functions of degree l in the numerator and m in the denominator. The above forms are the most efficient of a number of different alternatives that were tested.

For the low range of x an approximation to $J_n(x)$ of the form

$$x^n \prod_{i=1}^4 (x - j_{n,i}) R_{lm}(x)$$

was tried, but was discarded because of slow convergence in the Walsh array.

In the approximation to $Y_n(x)$ in the low range, the two terms in the formula cancel more and more as $x \rightarrow y_{n,2}$, and the breakpoint between the two lower ranges had to be somewhat smaller than $y_{n,2}$. For the value chosen, the maximum cancellation is between one and two bits for $Y_0(x)$ and about one bit for $Y_1(x)$. Other forms of approximation to $Y_n(x)$ in the ranges [3.5, 14] and [5, 14], involving the factors $(x - y_{n,i})$, were tested but were discarded because of slow convergence in the Walsh array.

In addition to the approximation to $M_n(x)$ on the previous page, we tested the form $[x^{-1}R_{lm}(1/x^2)]^{1/2}$, since both forms involve the same amount of computation. The latter form proved to be less accurate, for a given degree, and was discarded.

For the rational functions $R_{lm}(x)$ and $S_{lm}(x)$ the relative error of the approximation was minimized.

The master routines are based on the ascending series (1) and (2) for $0 \leq x \leq 6$, and on the asymptotic series (5) and (6) for $x \geq 40$. For the intermediate range $6 \leq x \leq 40$, $J_n(x)$ and $Y_n(x)$ are computed by Taylor series expansions of the form

$$(14) \quad \mathcal{C}_n(x_0 + h) = \mathcal{C}_n(x_0) + \sum_{m=1}^N \frac{h^m}{m!} \mathcal{C}_n^{(m)}(x_0),$$

where $\mathcal{C}_n(x_0)$ is the closest of a set of reference values, and where the derivatives $\mathcal{C}_n^{(m)}(x_0)$ are computed by (9). The table of reference values is constructed by using the Hankel asymptotic expansion at $x = 40$, and then using (14) repeatedly with negative values of h . For $x < 40$, M_n and θ_n are computed directly from (3) and (4).

The zeros $j_{n,1}, j_{n,2}, j_{n,3}, j_{n,4}$, and $y_{n,1}$ were obtained from [11].

For the lowest range of the argument each auxiliary function is computed from the corresponding value of J_n or Y_n if the argument is not close to a zero, and, if the argument is close to a zero, from a Taylor expansion about that zero.

The accuracy of the master routines was established by comparison with values in [8] and [7], with values computed by Brent's multiple-precision package [2], with values computed at the range boundaries, and by differencing. We conclude that the master routines are accurate to at least 26D for $0 < x \leq 14$, and to at least 26S for $x \geq 14$.

As a check of the zeros $j_{0,s}, j_{1,s}, y_{0,s}$, and $y_{1,s}$ in [11], we recomputed them with Brent's MP package and found agreement to all digits quoted in [11]. The formulae

$$\sum_{s=1}^{\infty} 1/[j_{0,s} J_1(j_{0,s})] = 1/2$$

and

$$\sum_{s=1}^{\infty} 1/[j_{1,s}^2 J_0(j_{1,s})] = -1/8,$$

combined with the Euler transformation applied to the $j_{0,s}$ and $j_{1,s}$ for $s = 1, 2, \dots, 50$, gave agreement to 35D.

$y_{0,s}$ and $y_{1,s}$, $s = 1, 2, \dots, 50$, were substituted in the Wronskian (10), and gave agreement to at least 40D.

The tests also indicate that the McMahon expansions (11) are accurate to 29S for $j_{0,11}, y_{0,12}, j_{1,12}, y_{1,11}$ and larger zeros.

4. Results. The details of the approximations are given in Tables 1–146, in a format similar to that used in [7]. Tables 1–14 summarize the best approximations in the L_∞ Walsh arrays of the functions, and Tables 19–146 give the coefficients of selected approximations. The precision is defined as

$$-\log_{10} \max_x \left| \frac{f(x) - R_{lm}(x)}{f(x)} \right|,$$

where $f(x)$ is the function being approximated, and the maximum is taken over the appropriate interval. Tables 1–146 are in the microfiche supplement attached to the end of this issue.

For completeness we have also listed in Tables 15–18 the zeros $j_{n,s}$ and $y_{n,s}$ to 35D for $s = 1, 2, \dots, 30$.

For the lowest range of each function the rational approximations are ill-conditioned, those pertaining to $J_0(x)$ and $J_1(x)$ losing up to four significant digits by cancellation, and those pertaining to $Y_0(x)$ and $Y_1(x)$ about one digit. To eliminate the cancellation each numerator was converted to minimal Newton form [12], and the resulting coefficients rounded off by an algorithm similar to that used in [7]. The cancellation also necessitated a modification to the Remes algorithm for certain cases. In particular, the error curve for the last entry in Tables 1 and 8 was levelled to only one digit.

The approximations in Tables 19–146 were verified by comparing them with the master routine for 5000 pseudo random values of the argument in each interval. The resulting precision agreed to three digits with the computed value in the Walsh array, even for the cases in which the error curve was levelled to one digit. In addition J_n and Y_n values computed by (13) were compared with values in [8] and with values computed by the MP package, and in all cases the agreement was as expected.

5. Design of a Subroutine. For the low range of x relative accuracy may be retained in the computation of J_n and Y_n if the terms $(x^2 - c^2)$ and $\ln x/c$ in (13) are evaluated carefully, where c denotes a zero.

In the formula for J_n , let c denote the zero closest to x . Then the difference $(x^2 - c^2)$ should be computed as $(x - c)(x + c)$, and the factor $(x - c)$ computed in double-precision arithmetic, with c accurate to double precision. All other operations may be performed in single precision.

In the formula for Y_n , $(x^2 - c^2)$ should be evaluated in the same manner, where c denotes the closer of $j_{n,1}$ and $y_{n,1}$. If x is close to $y_{n,1}$, $\ln x/y_{n,1}$ may be computed accurately from the series expansion of $\ln[1 + (x - y_{n,1})/y_{n,1}]$. Again, $x - y_{n,1}$ should be computed in double-precision arithmetic.

For the remaining ranges of x , the formulae (13) are not capable of retaining complete accuracy in the neighborhood of zeros, and an alternative formulation is necessary there. We can assess the accuracy attainable with (13) by the following

approximate analysis, which pertains to a binary computer with t binary digits in the mantissa of floating-point numbers.

Consider the evaluation of $Y_0(x) = M_0(x)\sin \theta_0(x)$, where

$$\theta_0(x) \simeq x - \pi/4 + x^{-1}S(1/x^2).$$

If x is reduced to the range $[0, \pi)$ by a double-precision range reduction, then the error in the reduced argument is $O(2^{-2t+1}x)$. If the subtraction of $\pi/4$ is again done in double precision, the error in the resulting value is $O(2^{-2t+1}x)$. $x^{-1}S(1/x^2)$ may now be added in single precision, introducing a further error $O(2^{-t-2}/x)$, if $S(1/x^2)$ is accurate to approximately single precision. Thus the total error in the reduced argument $\theta_0(x)$ is $O(2^{-2t+1}x) + O(2^{-t-2}/x)$, and, since the reduced $\theta_0(x)$ is approximately zero, the error in $\sin \theta_0(x)$ is $O(2^{-2t+1}x) + O(2^{-t-2}/x)$.

Let $\delta x = x - c$ be the minimum difference between x and the closest zero c of $Y_0(x)$ for which $\sin \theta_0(x)$, as computed above, gives single-precision accuracy. For this argument x , $\sin \theta_0(x) \simeq \pm \sin \delta x \simeq \pm \delta x$ (assuming $|\delta x| < 1$), and so, by the definition of δx ,

$$\left| \frac{2^{-t-2}}{x \delta x} \right| = O(2^{-t}), \quad \therefore |\delta x| = O(1/4x).$$

Thus, if $|\delta x| > O(1/4x)$, $\sin \theta_0(x)$ is accurate to single precision. Now, for a general argument x , the minimum δx possible for a single precision argument is $O(2^{-t+1}x)$, and so it follows that, for $x > O(2^{t/2})$, the above algorithm gives single-precision accuracy at zeros.

We have shown, therefore, that if $x > O(2^{t/2})$, or if $x < O(2^{t/2})$ and $|x - c| > O(1/4x)$, then $\sin \theta_0(x)$ as evaluated above, and hence $Y_0(x)$, is accurate to single precision.

For $x < O(2^{t/2})$ and $|x - c| < O(1/4x)$, $J_n(x)$ and $Y_n(x)$ can be computed accurately by using a Taylor expansion about c . Let $s = [x/\pi - n/2 + 1/4]$ or $s = [x/\pi - n/2 + 3/4]$ in the case of $J_n(x)$ and $Y_n(x)$, respectively (where $[\]$ denotes "integral part"), and compute

$$\beta = (s + n/2 - 1/4)\pi \quad \text{or} \quad \beta = (s + n/2 - 3/4)\pi.$$

The expansion should be based on $j_{n,s}$ or $y_{n,s}$ if $x - (\beta \pm c_1/\beta) < O(1/4x)$, and $j_{n,s+1}$ or $y_{n,s+1}$ if $x - (\beta + c_1/\beta) > \pi - O(1/4x)$. A typical expansion is

$$J_n(x) = hJ'_n(j_{n,s}) + h^2J''_n(j_{n,s})/2! + h^3J'''_n(j_{n,s})/3! + \dots,$$

where $h = x - j_{n,s}$. h should be computed in double-precision arithmetic, with $j_{n,s}$ accurate to double precision, but all other operations may be performed in single precision.

Double-precision values of $j_{n,s}$ and $y_{n,s}$ may be obtained from a table of values, or computed by (11).

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1. M. ABRAMOWITZ & I. A. STEGUN (Editors), *Handbook of Mathematical Functions*, Nat. Bur. Standards, Appl. Math. Series No. 55, U. S. Government Printing Office, Washington, D. C., 1965.
2. R. P. BRENT, "A FORTRAN Multiple-Precision Arithmetic Package," *ACM Trans. Math. Software*, v. 4, 1978, pp. 57–70.
3. C. W. CLENSHAW & SUSAN M. PICKEN, *Chebyshev Series for Bessel Functions of Fractional Order*, Nat. Phys. Lab. Math. Tables, v. 8, Her Majesty's Stationery Office, London, 1956.
4. W. J. CODY, "The FUNPACK Package of Special Function Subroutines," *ACM Trans. Math. Software*, v. 1, 1975, pp. 13–25.
5. W. J. CODY, R. M. MOTLEY & L. W. FULLERTON, "Coefficients for the approximation of $Y_\nu(x)$," *AMD Technical Memorandum #284*, Argonne National Laboratory. (In preparation.)
6. D. DÖRING, "Über die McMahon-Entwicklungen," *Z. Angew. Math. Phys.*, v. 18, 1967, pp. 461–473.
7. J. F. HART, ET AL., *Computer Approximations*, Wiley, New York, 1968.
8. K. HAYASHI, *Tafeln der Besselschen, Theta, Kugel—und anderer Funktionen*, Springer-Verlag, Berlin, 1930.
9. J. H. JOHNSON & J. M. BLAIR, *REMES2: A FORTRAN Program to Calculate Rational Minimax Approximations to a Given Function*, Atomic Energy of Canada Limited, Report AECL-4210, Chalk River, Ontario, 1973.
10. Y. L. LUKE, *Mathematical Functions and Their Approximations*, Academic Press, New York, 1975.
11. S. MAKINOCHI, *Zeros of Bessel Functions $J_\nu(x)$ and $Y_\nu(x)$ Accurate to Twenty-Nine Significant Digits*, Osaka University Technology Report No. 685, 1965.
12. C. MESZTENYI & C. WITZGALL, "Stable evaluation of polynomials," *J. Res. Nat. Bur. Standards Sect. B*, v. 71B, 1967, pp. 11–17.
13. F. W. J. OLVER (Ed.), *Bessel Functions, Part III. Zeros and Associated Values*, Royal Society Mathematical Tables, v. 7, Cambridge Univ. Press, Cambridge, 1960.
14. J. WIMP, "Polynomial expansions of Bessel functions and some associated functions," *Math. Comp.*, v. 16, 1962, pp. 446–458.

Table 1

$$J_0(x) = \prod_{s=1}^4 (x^2 - j_{0,s}^2) \sum_{j=0}^{\ell} p_j (x^2 - 196)^j / \sum_{j=0}^m q_j x^{2j}$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0, 14]	2.72	3	2	19
	4.95	5	2	20
	8.86	7	3	21
	11.79	8	4	22
	14.92	10	4	23
	16.56	10	5	24
	18.26	11	5	25
	21.74	12	6	26
	23.51	13	6	27

Table 2

$$Y_0(x) = (x^2 - y_{0,1}^2) \ln \frac{x}{y_{0,1}} \sum_{j=0}^{\ell} p_j (x^2 + 12.25)^j / \sum_{j=0}^m q_j x^{2j} + (x^2 - y_{0,1}^2) S(x^2)$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0, 3.5]	2.61	1	1	28
	4.26	2	1	29
	7.92	4	1	30
	12.15	5	2	31
	14.38	6	2	32
	16.69	6	3	33
	19.13	7	3	34
	24.14	9	3	35

Table 3

$$Y_0(x) = (x^2 - y_{0,1}^2)^{l_n} \frac{x}{y_{0,1}} R(x^2) + (x^2 - y_{0,1}^2) \sum_{j=0}^l p_j (x^2 - 12.25)^j / \sum_{j=0}^m q_j x^{2j}$$

RANGE	PRECISION	l	m	TABLE OF COEFFICIENTS
[0, 3.5]	2.35	1	1	36
	3.99	2	1	37
	7.61	4	1	38
	11.79	5	2	39
	14.02	6	2	40
	16.31	6	3	41
	18.73	7	3	42
	23.74	9	3	43

Table 4

$$M_0(x) = x^{-1/2} \sum_{j=0}^l p_j z^j / \sum_{j=0}^m q_j z^j, \quad z = 1/x^2$$

RANGE	PRECISION	l	m	TABLE OF COEFFICIENTS
[3.5, 14]	2.67	0	0	44
	5.80	1	1	45
	8.27	2	2	46
	10.49	3	3	47
	12.55	4	4	48
	14.53	5	5	49
	16.44	6	6	50
	18.31	7	7	51
	20.14	8	8	52
	23.71	10	10	53

Table 5

$$M_0(x) = x^{-1/2} \frac{\sum_{j=0}^{\ell} p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
$(0, 1/196]_z$	3.80	0	0	54
	6.51	0	1	55
	8.86	1	1	56
	12.82	2	2	57
	14.55	2	3	58
	16.20	3	3	59
	17.74	3	4	60
	20.64	4	5	61
	24.63	6	6	62

Table 6

$$\theta_0(x) = x - \pi/4 + x^{-1} \frac{\sum_{j=0}^{\ell} p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
$(3.5, 14]$	3.28	0	1	63
	5.83	1	2	64
	8.07	2	3	65
	10.15	3	4	66
	12.13	4	5	67
	14.04	5	6	68
	15.91	6	7	69
	18.64	8	8	70
	20.42	9	9	71
	23.90	11	11	72

Table 7

$$\theta_0(x) = x - \pi/4 + x^{-1} \frac{\sum_{j=0}^{\ell} p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0, 1/196] _z	2.88	0	0	73
	5.37	0	1	74
	7.56	1	1	75
	9.52	1	2	76
	11.34	2	2	77
	13.01	2	3	78
	14.61	3	3	79
	16.11	3	4	80
	18.95	4	5	81
	22.83	6	6	82

Table 8

$$J_1(x) = x \prod_{s=1}^4 (x^2 - j_{1,s}^2) \frac{\sum_{j=0}^{\ell} p_j (x^2 - 196)^j}{\sum_{j=0}^m q_j x^{2j}}$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0, 14]	3.15	3	2	83
	5.44	5	2	84
	8.07	6	3	85
	12.45	8	4	86
	14.02	9	4	87
	17.30	10	5	88
	20.75	12	5	89
	24.29	13	6	90

Table 9

$$Y_1(x) = x(x^2 - j_{1,1}^2) \ln \frac{x}{y_{1,1}} \sum_{j=0}^{\ell} p_j (x^2 - 25)^j / \sum_{j=0}^m q_j x^{2j} + \frac{(x^2 - y_{1,1}^2)}{xy_{1,1}^2} S(x^2)$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0,5]	2.00	1	1	91
	4.92	3	1	92
	8.36	4	2	93
	12.21	6	2	94
	14.26	6	3	95
	16.41	7	3	96
	18.61	8	3	97
	20.86	9	3	98
	23.19	9	4	99

Table 10

$$Y_1(x) = x(x^2 - j_{1,1}^2) \ln \frac{x}{y_{1,1}} R(x^2) + \frac{(x^2 - y_{1,1}^2)}{xy_{1,1}^2} x$$

$$x [p_0 + p_1(x^2 - 25) + x^2 \sum_{j=2}^{\ell} p_j (x^2 - 25)^{j-1}] / \sum_{j=0}^m q_j x^{2j}$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0,5]	2.12	3	0	100
	4.96	4	1	101
	8.33	5	2	102
	12.16	7	2	103
	14.18	7	3	104
	16.32	8	3	105
	18.51	9	3	106
	20.75	10	3	107
	23.07	10	4	108

Table 11

$$M_1(x) = x^{-1/2} \frac{\sum_{j=0}^l p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	l	m	TABLE OF COEFFICIENTS
[5,14]	2.50	0	0	109
	4.63	1	0	110
	7.89	2	1	111
	11.89	3	3	112
	14.29	4	4	113
	16.57	5	5	114
	18.78	6	6	115
	20.94	7	7	116
	24.08	9	8	117

Table 12

$$M_1(x) = x^{-1/2} \frac{\sum_{j=0}^l p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	l	m	TABLE OF COEFFICIENTS
[0, 1/196] _z	3.32	0	0	118
	6.21	1	0	119
	8.64	1	1	120
	12.66	2	2	121
	14.41	3	2	122
	16.07	3	3	123
	17.62	4	3	124
	20.54	5	4	125
	24.53	6	6	126

Table 13

$$\theta_1(x) = x - 3\pi/4 + x^{-1} \frac{\sum_{j=0}^{\ell} p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[5, 14)	2.15	0	0	127
	4.07	0	1	128
	8.44	2	2	129
	10.99	3	3	130
	12.14	3	4	131
	14.44	4	5	132
	16.65	5	6	133
	19.87	7	7	134
	21.96	8	8	135
	24.00	9	9	136

Table 14

$$\theta_1(x) = x - 3\pi/4 + x^{-1} \frac{\sum_{j=0}^{\ell} p_j z^j}{\sum_{j=0}^m q_j z^j}, \quad z = 1/x^2$$

RANGE	PRECISION	ℓ	m	TABLE OF COEFFICIENTS
[0, 1/196] _z	2.96	0	0	137
	5.61	0	1	138
	9.84	1	2	139
	11.66	2	2	140
	13.36	2	3	141
	14.96	3	3	142
	16.48	3	4	143
	17.93	4	4	144
	20.67	5	5	145
	23.23	6	6	146

TABLE 1

2

1	100	100	100	100	100	100	100
2	95	95	95	95	95	95	95
3	90	90	90	90	90	90	90
4	85	85	85	85	85	85	85
5	80	80	80	80	80	80	80
6	75	75	75	75	75	75	75
7	70	70	70	70	70	70	70
8	65	65	65	65	65	65	65
9	60	60	60	60	60	60	60
10	55	55	55	55	55	55	55
11	50	50	50	50	50	50	50
12	45	45	45	45	45	45	45
13	40	40	40	40	40	40	40
14	35	35	35	35	35	35	35
15	30	30	30	30	30	30	30
16	25	25	25	25	25	25	25
17	20	20	20	20	20	20	20
18	15	15	15	15	15	15	15
19	10	10	10	10	10	10	10
20	5	5	5	5	5	5	5
21	0	0	0	0	0	0	0
22	0	0	0	0	0	0	0
23	0	0	0	0	0	0	0
24	0	0	0	0	0	0	0
25	0	0	0	0	0	0	0
26	0	0	0	0	0	0	0
27	0	0	0	0	0	0	0
28	0	0	0	0	0	0	0
29	0	0	0	0	0	0	0
30	0	0	0	0	0	0	0

Table 1

1980	1	1	1	1	1
1981	1	1	1	1	1
1982	1	1	1	1	1
1983	1	1	1	1	1
1984	1	1	1	1	1
1985	1	1	1	1	1
1986	1	1	1	1	1
1987	1	1	1	1	1
1988	1	1	1	1	1
1989	1	1	1	1	1
1990	1	1	1	1	1

Table 2

1980	1	1	1	1	1
1981	1	1	1	1	1
1982	1	1	1	1	1
1983	1	1	1	1	1
1984	1	1	1	1	1
1985	1	1	1	1	1
1986	1	1	1	1	1
1987	1	1	1	1	1
1988	1	1	1	1	1
1989	1	1	1	1	1
1990	1	1	1	1	1

Table 21

0110	(01)	0101010	0120101	0101010	
0101	(10)	0101010	0101010	0101010	
0100	(11)	0101010	0101010	0101010	0
0010	(02)	0101010	0101010	0101010	0
0011	(03)	0101010	0101010	0101010	0
0001	(10)	0101010	0101010	0101010	0
0000	(11)	0101010	0101010	0101010	0

0110	(01)	0101010	0101010	0101010	0101010	010
0101	(10)	0101010	0101010	0101010	0101010	010
0100	(11)	0101010	0101010	0101010	0101010	010
0010	(02)	0101010	0101010	0101010	0101010	010

Table 22

0110	(03)	0101010	0101010	0101010	010
0101	(10)	0101010	0101010	0101010	010
0100	(11)	0101010	0101010	0101010	010
0010	(02)	0101010	0101010	0101010	010
0011	(03)	0101010	0101010	0101010	010
0001	(10)	0101010	0101010	0101010	010
0000	(11)	0101010	0101010	0101010	010

0110	(03)	0101010	0101010	0101010	0101010	0101010	0
0101	(10)	0101010	0101010	0101010	0101010	0101010	0
0100	(11)	0101010	0101010	0101010	0101010	0101010	0
0010	(02)	0101010	0101010	0101010	0101010	0101010	0
0011	(03)	0101010	0101010	0101010	0101010	0101010	0

Table 25

P00	(7)	.14948	20928	41185	68341	2950	
P01	(5)	-.91733	61524	22568	06504	1408	
P02	(4)	.17162	53409	77032	29069	29426	
P03	(2)	-.15940	61530	98339	41464	58215	2
P04	(-1)	.88539	86594	44178	58984	71317	
P05	(-3)	-.32339	99701	99288	23077	89804	
P06	(-6)	.81928	32866	42628	89726	4517	
P07	(-8)	-.14800	59097	24065	08996	77224	
P08	(-11)	.19191	18099	64071	31913	6376	
P09	(-14)	-.17515	28892	91554	72140	342	
P10	(-17)	.10508	16620	52276	98909	154	
P11	(-21)	-.33317	09529	58821	28527	5	

Q00	(15)	.91295	37239	25383	20937	02887	5708
Q01	(13)	.35398	49753	12015	84478	23398	2936
Q02	(10)	.62112	85298	92583	91068	05675	6736
Q03	(7)	.52338	79824	34563	45429	63795	4020
Q04	(4)	.36297	72957	26149	51985	25299	7264
Q05	(0)	.99999	99999	99999	99999	99999	998

Table 26

P00	(10)	.38876	80391	09585	90908	67879	71
P01	(9)	-.23844	91990	96843	76179	46648	247
P02	(7)	.44564	04112	85398	97857	34281	292
P03	(5)	-.41354	37059	97827	49467	71803	7902
P04	(3)	.22973	13838	24143	14590	71016	3332
P05	(0)	-.84125	12446	48252	99846	36720	418
P06	(-2)	.21465	47038	84939	42996	15275	9883
P07	(-5)	-.39394	59484	46374	97158	82747	740
P08	(-8)	.52732	03857	53655	32915	41337	83
P09	(-11)	-.51281	79885	12207	68095	08127	3
P10	(-14)	.35194	19585	25010	24678	98604	4
P11	(-17)	-.15737	94220	80423	71430	73432	
P12	(-21)	.36080	57427	05061	72922	084	

Q00	(19)	.23762	22951	10319	06416	42727	1910
Q01	(16)	.91149	47598	17359	70159	79295	0155
Q02	(14)	.16240	76775	90718	32628	81831	8391
Q03	(11)	.17341	63239	58500	68264	63034	8614
Q04	(8)	.11816	67428	14753	85628	13192	8966
Q05	(4)	.49308	16827	31625	71174	32560	9456
Q06	(0)	.99999	99999	99999	99999	99999	9981

Table 27

P00	(10)	.74775	60485	33535	87861	04089	449
P01	(9)	-.46117	99587	06010	57446	60207	6637
P02	(7)	.87287	13969	93645	90780	25092	4243
P03	(5)	-.82529	09593	60315	37158	57327	4078
P04	(3)	.47016	73272	62552	67854	99865	2557
P05	(1)	-.17798	20890	67089	18089	80982	5192
P06	(-2)	.47424	69337	68945	24133	16794	1155
P07	(-5)	-.92131	27869	04297	57671	50458	1377
P08	(-7)	.13307	89281	07574	23868	69983	3469
P09	(-10)	-.14380	48027	98487	56012	73693	3350
P10	(-13)	.11517	30013	82333	24287	09365	624
P11	(-17)	-.66139	32748	89986	67197	56551	3
P12	(-20)	.25062	68042	45088	43861	70311	2
P13	(-24)	-.49147	93069	58303	47642	3621	

Q00	(19)	.49003	89421	63381	17134	43608	7202
Q01	(17)	.16987	29197	95222	81756	40943	4357
Q02	(14)	.27190	00503	81405	20169	50694	3701
Q03	(11)	.25900	00151	26746	36336	68377	7594
Q04	(8)	.15613	56667	21344	59138	57766	5640
Q05	(4)	.57053	28308	89995	68868	42127	6217
Q06	(0)	.99999	99999	99999	99999	99999	9981

Table 28

P00	(1)	-.13937	06
P01	(0)	.11221	64

Q00	(2)	.25086	153
Q01	(1)	.10000	000

Table 29

P00	(1)	-.24295	5419
P01	(0)	.21242	3053
P02	(-2)	-.51087	885
Q00	(2)	.52670	76349
Q01	(1)	.10000	00000

Table 30

P00	(1)	-.54104	32960	08
P01	(0)	.51989	24163	77
P02	(-1)	-.15716	63731	32
P03	(-3)	.21590	56586	3
P04	(-5)	-.14529	35415	7
Q00	(3)	.13233	14915	4502
Q01	(1)	.10000	00000	000

Table 31

P00	(4)	-.16275	90279	93385	98
P01	(3)	.15389	93071	79208	44
P02	(1)	-.45080	07229	90244	9
P03	(-1)	.59822	36377	80690	
P04	(-3)	-.40199	58177	4675	
P05	(-5)	.12392	19260	537	
Q00	(5)	.39141	15394	29032	994
Q01	(3)	.34305	51303	57363	69
Q02	(1)	.10000	00000	00000	0

Table 32

P00	(4)	-.27390	65549	68637	7157
P01	(3)	.26405	53968	02596	4955
P02	(1)	-.80820	50323	09570	633
P03	(0)	.11634	14895	32709	724
P04	(-3)	-.91268	71527	03922	2
P05	(-5)	.40294	51091	89263	7
P06	(-8)	-.87222	60376	6295	
Q00	(5)	.67424	04913	08379	13053
Q01	(3)	.45887	13683	53649	2339
Q02	(1)	.10000	00000	00000	000

Table 33

P00	(6)	-.85852	78246	77332	25274	9
P01	(5)	.81119	10680	75168	56624	8
P02	(4)	-.23775	26245	62644	90177	8
P03	(2)	.31901	03319	95918	29594	
P04	(0)	-.22539	23551	84685	4475	
P05	(-3)	.85394	48389	51789	12	
P06	(-5)	-.14631	86785	70432	2	
Q00	(8)	.20648	15831	99978	80161	292
Q01	(6)	.17919	62526	75175	99979	53
Q02	(3)	.64672	57980	90501	20173	
Q03	(1)	.10000	00000	00000	0000	

Table 34

P00	(7)	-.16907	68886	10051	35420	7692
P01	(6)	.16243	10594	49623	64409	6653
P02	(4)	-.49403	46555	73593	32322	849
P03	(2)	.70728	69474	28936	01998	21
P04	(0)	-.55775	14063	27460	78786	8
P05	(-2)	.25763	31389	51770	69120	1
P06	(-5)	-.68415	46476	77247	6309	
P07	(-8)	.86251	15001	53368	09	
Q00	(8)	.41471	42544	79652	31830	64828
Q01	(6)	.29247	81603	25869	60684	2579
Q02	(3)	.83848	33679	91673	08957	29
Q03	(1)	.10000	00000	00000	00000	0

Table 35

P00	(7)	-.53901	96315	94916	81628	11732	2112
P01	(6)	.52901	63489	24645	01044	73639	3696
P02	(5)	-.16847	29093	00526	76958	82640	3049
P03	(3)	.26039	47862	81642	48594	41196	154
P04	(1)	-.23154	50667	58157	94135	20357	80
P05	(-1)	.12933	37567	58074	34656	94556	9
P06	(-4)	-.47373	01915	69395	45345	0221	
P07	(-6)	.11435	36521	97414	83584	518	
P08	(-9)	-.17277	93266	14738	91155	5	
P09	(-12)	.13204	13158	95607	3179		
Q00	(9)	.13565	75709	55594	63709	20178	0464
Q01	(6)	.66833	52593	63584	90504	46717	547
Q02	(4)	.12941	20177	15908	53519	06894	79
Q03	(1)	.10000	00000	00000	00000	00000	0

Table 36

P00	(1)	.14938	32
P01	(0)	-.18920	10
Q00	(2)	.20832	604
Q01	(1)	.10000	000

Table 37

P00	(1)	.26869	841
P01	(0)	-.35212	836
P02	(-1)	.10383	0382
Q00	(2)	.46983	5223
Q01	(1)	.10000	0000

Table 38

P00	(1)	.61922	38399	04
P01	(0)	-.87284	94601	03
P02	(-1)	.31757	97634	98
P03	(-3)	-.49133	72842	3
P04	(-5)	.36171	97028	
Q00	(3)	.12426	95426	845
Q01	(1)	.10000	00000	000

Table 39

P00	(4)	.17996	78635	79003	46
P01	(3)	-.25099	00214	02244	72
P02	(1)	.88760	19472	34476	8
P03	(0)	-.13293	47104	38737	5
P04	(-3)	.97548	67359	4387	
P05	(-5)	-.32232	95583	331	
Q00	(5)	.35540	44488	64782	36
Q01	(3)	.32545	25859	75531	7
Q02	(1)	.10000	00000	00000	0

Table 40

P00	(4)	.30708	09764	93299	6965
P01	(3)	-.43431	74756	89868	2167
P02	(2)	.16010	42187	34521	4062
P03	(0)	-.25968	01069	42937	304
P04	(-2)	.22213	95245	95699	10
P05	(-4)	-.10491	79827	99093	7
P06	(-7)	.24008	32736	9922	
Q00	(5)	.62171	16033	95044	5600
Q01	(3)	.43922	90661	40137	874
Q02	(1)	.10000	00000	00000	00

Table 41

P00	(6)	.92891	25554	24893	24497	1
P01	(6)	-.12955	86679	02750	59005	67
P02	(4)	.45890	29470	50285	03403	8
P03	(2)	-.69559	10718	92243	54847	
P04	(0)	.53704	13330	29036	4130	
P05	(-2)	-.21804	27168	33896	129	
P06	(-5)	.39537	50933	44849	3	
Q00	(8)	.18365	79030	43497	23301	09
Q01	(6)	.16483	45341	89213	30228	5
Q02	(3)	.61823	16717	42093	2983	
Q03	(1)	.10000	00000	00000	0000	

TABLE 16

Q117 (2) 73339 3

TABLE 17

Q118 (2) 50279 42222
Q119 (2) 73333 2222

Q120 (2) 31252 21222
Q121 (2) 21111 21111

TABLE 18

Q122 (2) 27222 22272 222
Q123 (2) 22272 22222 222
Q124 (2) 73333 22222 2

Q125 (2) 22222 22222 222
Q126 (2) 22222 22222 222
Q127 (2) 22222 22222 222

TABLE 19

Q128 (2) 22222 22222 22222
Q129 (2) 22222 22222 22222
Q130 (2) 22222 22222 22222
Q131 (2) 22222 22222 222

Q132 (2) 22222 22222 22222
Q133 (2) 22222 22222 22222
Q134 (2) 22222 22222 22222
Q135 (2) 22222 22222 22222

Table 51

0117	(20)	000000	000000	000000	000000	0
0118	(20)	000000	000000	000000	000000	0
0119	(20)	000000	000000	000000	000000	0
0120	(20)	000000	000000	000000	000000	0
0121	(20)	000000	000000	000000	000000	0
0122	(20)	000000	000000	000000	000000	0
0123	(20)	000000	000000	000000	000000	0

0124	(20)	000000	000000	000000	000000	0
0125	(20)	000000	000000	000000	000000	0
0126	(20)	000000	000000	000000	000000	0
0127	(20)	000000	000000	000000	000000	0
0128	(20)	000000	000000	000000	000000	0
0129	(20)	000000	000000	000000	000000	0
0130	(20)	000000	000000	000000	000000	0

Table 52

0131	(20)	000000	000000	000000	000000	0
0132	(20)	000000	000000	000000	000000	0
0133	(20)	000000	000000	000000	000000	0
0134	(20)	000000	000000	000000	000000	0
0135	(20)	000000	000000	000000	000000	0
0136	(20)	000000	000000	000000	000000	0
0137	(20)	000000	000000	000000	000000	0

0138	(20)	000000	000000	000000	000000	0
0139	(20)	000000	000000	000000	000000	0
0140	(20)	000000	000000	000000	000000	0
0141	(20)	000000	000000	000000	000000	0
0142	(20)	000000	000000	000000	000000	0
0143	(20)	000000	000000	000000	000000	0
0144	(20)	000000	000000	000000	000000	0

0000	(1)	0000	0000	0000	0000	0000	0000
0001	(2)	0001	0001	0001	0001	0001	0001
0002	(3)	0002	0002	0002	0002	0002	0002
0003	(4)	0003	0003	0003	0003	0003	0003
0004	(5)	0004	0004	0004	0004	0004	0004
0005	(6)	0005	0005	0005	0005	0005	0005
0006	(7)	0006	0006	0006	0006	0006	0006
0007	(8)	0007	0007	0007	0007	0007	0007
0008	(9)	0008	0008	0008	0008	0008	0008

0009	(10)	0009	0009	0009	0009	0009	0009
0010	(11)	0010	0010	0010	0010	0010	0010
0011	(12)	0011	0011	0011	0011	0011	0011
0012	(13)	0012	0012	0012	0012	0012	0012
0013	(14)	0013	0013	0013	0013	0013	0013
0014	(15)	0014	0014	0014	0014	0014	0014
0015	(16)	0015	0015	0015	0015	0015	0015
0016	(17)	0016	0016	0016	0016	0016	0016
0017	(18)	0017	0017	0017	0017	0017	0017
0018	(19)	0018	0018	0018	0018	0018	0018

0019	(20)	0019	0019	0019	0019	0019	0019
0020	(21)	0020	0020	0020	0020	0020	0020
0021	(22)	0021	0021	0021	0021	0021	0021
0022	(23)	0022	0022	0022	0022	0022	0022
0023	(24)	0023	0023	0023	0023	0023	0023
0024	(25)	0024	0024	0024	0024	0024	0024
0025	(26)	0025	0025	0025	0025	0025	0025
0026	(27)	0026	0026	0026	0026	0026	0026
0027	(28)	0027	0027	0027	0027	0027	0027
0028	(29)	0028	0028	0028	0028	0028	0028
0029	(30)	0029	0029	0029	0029	0029	0029

0030	(31)	0030	0030	0030	0030	0030	0030
0031	(32)	0031	0031	0031	0031	0031	0031
0032	(33)	0032	0032	0032	0032	0032	0032
0033	(34)	0033	0033	0033	0033	0033	0033
0034	(35)	0034	0034	0034	0034	0034	0034
0035	(36)	0035	0035	0035	0035	0035	0035
0036	(37)	0036	0036	0036	0036	0036	0036
0037	(38)	0037	0037	0037	0037	0037	0037
0038	(39)	0038	0038	0038	0038	0038	0038
0039	(40)	0039	0039	0039	0039	0039	0039

ANSWER 38

3188 (4) 72775 48

ANSWER 39

3188 (2) 22852 42772 7

3188 (2) 20227 70222 8

3188 (2) 28888 488

ANSWER 40

3188 (4) 22222 222 70 222

3188 (4) 70022 22222 7

3188 (4) 22222 22222 222

3188 (4) 28888 88888 88

ANSWER 41

3188 (2) 22222 22222 22222 22

3188 (2) 22222 22222 22222 2

3188 (2) 70000 22222 222

3188 (2) 22222 22222 22772 20

3188 (2) 22222 22772 22222 82

3188 (2) 28888 88888 88888

Table 38

0497	(4)	335544	343554	322442	73544
0498	(2)	335544	443554	44 772	447
0499	(2)	725 72	342555	443555	4
0497	(4)	4455 25	774552	342223	44552
0498	(2)	4424 42	742 72	3422 22	4525
0499	(2)	244445	445555	344444	5
0499	(5)	444444	444444	4444	

Table 39

0497	(2)	443442	342224	344422	444223	7
0498	(4)	344427	44 754	344447	444444	
0499	(2)	344443	472 74	44 744	34442	
0499	(4)	74242	44 522	344424	2	
0497	(2)	34442 2	44 744	24 744	344477	7
0498	(4)	24 24 2	44244	342244	24445	
0499	(2)	44445	34444	444424	4734	
0499	(2)	444444	444444	444444	444	

Table 40

0497	(2)	344422	42442	44 252	44424	445
0498	(2)	444444	24242	25544	34544	44
0499	(2)	444447	32244	44242	344447	4
0499	(2)	24445	74442	44447	4534	
0497	(2)	24244	34442	42554	444444	445
0498	(2)	44344	24244	34344	444444	44
0499	(2)	444425	34444	44444	27444	4
0499	(2)	344422	44444	444422	44 74	
0498	(2)	444444	444444	444444		

Table 61

P00	(-3)	.63858	31678	58121	11269	86258
P01	(-1)	.73640	77793	49140	23242	23910
P02	(1)	.22021	61368	19311	07752	5461
P03	(2)	.18214	94183	28523	80717	563
P04	(2)	.28833	09857	05081	48496	0
Q00	(-3)	.80034	53121	28300	35068	15378
Q01	(-1)	.92345	04965	07471	13836	55158
Q02	(1)	.27656	88692	76444	18663	0190
Q03	(2)	.22992	77496	20544	66161	399
Q04	(2)	.37333	13472	94684	52833	2
Q05	(1)	.10000	00000	00000	000	

Table 62

P00	(-6)	.10701	03603	20012	56843	69871	7926
P01	(-4)	.26271	24484	85997	43509	07643	3781
P02	(-2)	.20159	27500	01033	71888	84385	4185
P03	(-1)	.58242	72837	47137	75097	74312	877
P04	(0)	.60646	29982	88152	51588	81767	07
P05	(1)	.17997	00561	44264	61010	47463	
P06	(0)	.72409	97215	81098	09637	47	
Q00	(-6)	.13411	75974	28297	39160	25660	5921
Q01	(-4)	.32934	50492	34663	36130	74909	0780
Q02	(-2)	.25286	34958	85684	42350	80949	6823
Q03	(-1)	.73151	13812	22151	89098	88005	155
Q04	(0)	.76441	59363	90874	08599	37732	37
Q05	(1)	.22969	88239	29893	65985	70015	
Q06	(1)	.10000	00000	00000	00000	000	

Table 63

P00	(0)	-.28348	14
Q00	(1)	.22698	926
Q01	(1)	.10000	00

Table 64

P00	(-1)	-.99772	2674
P01	(0)	-.48290	1822
Q00	(0)	.79818	49411 3
Q01	(1)	.42773	70171
Q02	(1)	.10000	0000

Table 65

P00	(-1)	-.19261	84719	69
P01	(0)	-.30199	39712	42
P02	(0)	-.65926	31046	2
Q00	(0)	.15409	48098	0454
Q01	(1)	.24961	97461	1053
Q02	(1)	.63175	32603	48
Q03	(1)	.10000	00000	0

Table 66

P00	(-2)	-.26633	64804	31552
P01	(-1)	-.86952	45469	0106
P02	(0)	-.62001	44217	6719
P03	(0)	-.82525	43396	811
Q00	(-1)	.21306	91861	65299 8
Q01	(0)	.70671	68957	02842 9
Q02	(1)	.52924	95256	47962
Q03	(1)	.84503	79644	8168
Q04	(1)	.10000	00000	000

Table 67

P00	(-3)	-.29498	38954	95993	34
P01	(-1)	-.16430	52925	14899	71
P02	(0)	-.24469	78571	78998	31
P03	(1)	-.10688	01768	08973	06
P04	(0)	-.98557	70187	27502	

Q00	(-2)	..23598	71165	12026	143
Q01	(0)	.13267	33327	89317	547
Q02	(1)	.20227	27314	44266	657
Q03	(1)	.94123	66392	83702	36
Q04	(2)	.10696	19287	28938	54
Q05	(1)	.10000	00000	00000	

Table 68

P00	(-4)	-.27795	79066	37698	559
P01	(-2)	-.23545	28402	03787	4278
P02	(-1)	-.59979	13092	88994	4169
P03	(0)	-.54832	35595	49610	3130
P04	(1)	-.16637	90872	91700	0115
P05	(1)	-.11424	78521	78094	888

Q00	(-3)	.22236	63253	18108	57470
Q01	(-1)	.18952	04300	39591	33189
Q02	(0)	.48933	10947	23694	50408
Q03	(1)	.46125	87531	60577	33137
Q04	(2)	.15099	02046	47773	32688
Q05	(2)	.13063	50911	14922	8957
Q06	(1)	.10000	00000	00000	00

Table 69

P00	(-5)	-.23125	06761	18087	10342	
P01	(-3)	-.27638	35226	44865	22186	3
P02	(-1)	-.10735	07066	22251	84758	34
P03	(0)	-.16816	37969	04305	69514	84
P04	(1)	-.10695	27154	02689	40041	01
P05	(1)	-.24206	02553	96667	64922	8
P06	(1)	-.12971	98186	69122	48964	

Q00	(-4)	.18500	05408	95056	78395	3
Q01	(-2)	.22207	03625	93670	99035	69
Q02	(-1)	.87006	16530	14288	02843	36
Q03	(1)	.13871	45363	86924	92036	812
Q04	(1)	.91584	46243	94744	72555	37
Q05	(2)	.22611	30768	07861	73246	56
Q06	(2)	.15556	29964	98904	52539	2
Q07	(1)	.10000	00000	00000	0000	

Table 70

P00	(-8)	-.62785	23539	69707	00067	414
P01	(-5)	-.11449	13567	56603	45584	69131
P02	(-4)	-.73332	71636	69595	78227	38888
P03	(-2)	-.21073	72378	43309	36612	11207
P04	(-1)	-.28805	40216	16150	99401	28456
P05	(0)	-.18295	65065	94559	81692	33021
P06	(0)	-.48708	82841	67550	04239	5339
P07	(0)	-.42291	00124	36828	29899	817
P08	(-1)	-.54748	76936	45597	22995	4

Q00	(-7)	.50228	18831	75821	37616	5670
Q01	(-5)	.91854	69055	26970	47934	83469
Q02	(-3)	.59136	16187	09507	52068	75247 7
Q03	(-1)	.17152	23807	24558	28806	34012 4
Q04	(0)	.23849	61587	38669	69646	37635 6
Q05	(1)	.15653	51596	20516	54713	10814 9
Q06	(1)	.44580	68790	50105	84466	15741
Q07	(1)	.45327	01724	45777	01323	7001
Q08	(1)	.10000	00000	00000	00000	000

P00	(-9)	-.39545	33153	29009	82258	93454	
P01	(-7)	-.91328	43730	85233	48281	06070	1
P02	(-5)	-.76844	43911	39726	04464	82783	3
P03	(-3)	-.30406	97003	56627	67560	40852	57
P04	(-2)	-.60987	63616	42016	29252	00891	20
P05	(-1)	-.62323	82098	27715	61109	79174	31
P06	(0)	-.30953	02798	49467	57086	25128	26
P07	(0)	-.66532	35708	90317	73504	09285	7
P08	(0)	-.47776	47262	86506	71716	85813	
P09	(-1)	-.52121	25703	26227	39124	511	

Q00	(-8)	.31636	26522	63212	24941	54166	4
Q01	(-6)	.73227	52206	15324	85492	99992	13
Q02	(-4)	.61851	64061	77042	37271	36295	83
Q03	(-2)	.24635	85751	64099	14177	73551	247
Q04	(-1)	.49978	53036	46616	41786	60703	662
Q05	(0)	.52117	72659	57808	67515	67369	760
Q06	(1)	.26872	51819	97415	36811	54979	458
Q07	(1)	.62218	22223	93576	29102	86099	06
Q08	(1)	.52871	50223	58191	91366	96876	0
Q09	(1)	.10000	00000	00000	00000	00000	

Table 72

P00	(-11)	-.13260	98510	22249	27966	58278	139
P01	(-9)	-.45574	89339	63250	35315	87276	8532
P02	(-7)	-.60151	52467	54584	37504	19444	8304
P03	(-5)	-.39833	25153	24941	92045	27714	6247
P04	(-3)	-.14517	94386	67856	16156	70183	5646
P05	(-2)	-.30076	43544	80162	02303	69495	2288
P06	(-1)	-.35346	13522	70704	38380	44682	5733
P07	(0)	-.22837	02697	90105	80705	79565	3650
P08	(0)	-.75809	96049	20521	99868	27732	6354
P09	(1)	-.11368	00227	06142	36718	09328	5272
P10	(0)	-.58926	72329	19990	06948	16349	5228
P11	(-1)	-.47697	78082	78299	45345	15239	67

Q00	(-10)	.10608	78808	17799	45445	58165	6083
Q01	(-8)	.36515	16882	16525	73209	66758	1252
Q02	(-6)	.48309	62428	16865	68373	89222	5031
Q03	(-4)	.32112	23087	93369	52754	84655	1030
Q04	(-2)	.11773	96547	60994	75986	08714	4977
Q05	(-1)	.24626	22801	35109	49981	27377	6691
Q06	(0)	.29396	54864	77411	47170	75289	7908
Q07	(1)	.19497	98624	44123	69460	13449	5866
Q08	(1)	.67774	22648	74694	68899	18347	2137
Q09	(2)	.11082	45831	16824	83635	51092	9211
Q10	(1)	.69218	70906	30599	73647	23147	2350
Q11	(1)	.00000	00000	00000	00000	00000	0000

Table 73

P00 (0) -.12483 63

Table 74

P00 (0) -.24321 6949

Q00 (1) .19457 43965 9

Q01 (1) .10000 000

Table 75

P00 (-1) -.40128 61992 78

P01 (0) -.10410 36634

Q00 (0) .32102 89681 668

Q01 (1) .10000 00000 0

Table 76

P00 (-1) -.48043 54151 253

P01 (0) -.36944 16147 84

Q00 (0) .38434 83322 15775

Q01 (1) .31557 13581 926

Q02 (1) .10000 00000 0

Table 77

P00 (-2) -.40872 81668 20474

P01 (-1) -.68533 13978 4708

P02 (-1) -.95049 16397 56

Q00 (-1) .32698 25334 57890 3

Q01 (0) .56529 54569 85354

Q02 (1) .10000 00000 0000

Table 78

P00	(-2)	-.37798	02080	07502	52
P01	(0)	-.11249	14322	44983	85
P02	(0)	-.46009	13930	17871	
Q00	(-1)	.30238	41664	06031	245
Q01	(0)	.91568	06332	48822	99
Q02	(1)	.41069	51655	87901	5
Q03	(1)	.10000	00000	000	

Table 79

P00	(-3)	-.21736	85562	58149	3627
P01	(-1)	-.10432	01991	71354	8141
P02	(-1)	-.91799	92105	21894	78
P03	(-1)	-.89348	05307	6621	
Q00	(-2)	.17389	48450	06519	91969
Q01	(-1)	.84361	86165	47350	0166
Q02	(0)	.77542	23825	83396	881
Q03	(1)	.10000	00000	00000	0

Table 80

P00	(-3)	-.17131	98622	19550	32064	1
P01	(-1)	-.12165	72935	83560	25023	
P02	(0)	-.18755	81854	48566	3313	
P03	(0)	-.53423	69409	11398	14	
Q00	(-2)	.13705	58897	75640	26708	34
Q01	(-1)	.98039	66762	60933	39587	6
Q02	(1)	.15492	29982	83888	94633	
Q03	(1)	.49343	77014	83753	363	
Q04	(1)	.10000	00000	00000	0	

Table 81

P00	(-5)	-.53163	91840	76602	83929	034
P01	(-3)	-.71471	28252	57230	88810	905
P02	(-1)	-.25791	29837	58615	23563	823
P03	(0)	-.27165	94441	66338	19674	2
P04	(0)	-.59899	47737	41924	7092	
Q00	(-4)	.42531	13472	61282	27148	0469
Q01	(-2)	.57398	54234	72770	53348	2333
Q02	(0)	.20924	85883	15250	26531	0283
Q03	(1)	.22731	93319	11403	08435	14
Q04	(1)	.56923	25399	30122	65725	
Q05	(1)	.10000	00000	00000	000	

Table 82

P00	(-8)	-.37821	00773	38777	99893	23684	22
P01	(-5)	-.10421	17433	47611	87167	73307	528
P02	(-4)	-.91390	09970	07620	47110	08218	93
P03	(-2)	-.30942	15184	28176	11153	78538	5
P04	(-1)	-.39142	65981	83816	31215	60795	
P05	(0)	-.14859	68892	41177	93815	0180	
P06	(-1)	-.79097	79932	48585	16111	7	
Q00	(-7)	.30256	80618	71022	39914	58990	283
Q01	(-5)	.83526	98221	03139	88174	39892	004
Q02	(-3)	.73542	04338	36260	50064	55658	380
Q03	(-1)	.25123	14563	07348	45329	06465	38
Q04	(0)	.32509	70478	09407	61392	70655	6
Q05	(1)	.13241	74315	02616	66614	42746	
Q06	(1)	.10000	00000	00000	00000	000	

Table 83

P00	(-4)	.20299	176			
P01	(-6)	-.62769	0786			
P02	(-8)	.64080	9312			
P03	(-10)	-.51237	9953			

Q00	(5)	.20601	73206	16362	52	
Q01	(3)	.19379	37619	80724	71	
Q02	(1)	.10000	00000	00000	000	

Table 84

P00	(-4)	.44898	14054			
P01	(-5)	-.14594	95139	6		
P02	(-7)	.18465	15149	39		
P03	(-9)	-.12612	86344	74		
P04	(-12)	.47490	15174	9		
P05	(-14)	-.14889	80143	03		
Q00	(5)	.82890	01096	11519	4464	
Q01	(3)	.47496	66683	22594	0125	
Q02	(1)	.10000	00000	00000	0000	

Table 85

P00	(-1)	.38569	44034	491		
P01	(-2)	-.12308	44056	7225		
P02	(-4)	.15185	00575	19334		
P03	(-7)	-.99360	49263	1183		
P04	(-9)	.38782	93413	1570		
P05	(-12)	-.91857	62355	595		
P06	(-14)	.13076	54876	7235		
Q00	(8)	.67008	77958	96675	76769	11
Q01	(6)	.38048	43679	83080	45847	16
Q02	(3)	.91275	71468	76670	49575	0
Q03	(1)	.10000	00000	00000	00000	00

Table 86

P00	(2)	.84826	20109	19323	98		
P01	(1)	-.27432	32344	33912	366		
P02	(-1)	.34660	87159	36235	4302		
P03	(-3)	-.23637	88060	04651	0891		
P04	(-6)	.99185	99383	81542	647		
P05	(-8)	-.27215	70769	31295	9196		
P06	(-11)	.49643	65756	15462	900		
P07	(-14)	-.57986	70431	36691	38		
P08	(-17)	.36955	38273	55745	0		
Q00	(12)	.16832	00899	93005	40524	06537	00
Q01	(9)	.79913	72160	71670	12884	32535	2
Q02	(7)	.16769	01071	57409	34384	48726	1
Q03	(4)	.18882	35677	69859	37374	53914	0
Q04	(1)	.10000	00000	00000	00000	00000	0

Table 87

P00	(3)	.14733	65624	91392	3534		
P01	(1)	-.48403	16668	91031	24307		
P02	(-1)	.62707	78526	24984	85860		
P03	(-3)	-.44345	63477	37703	41328		
P04	(-5)	.19592	08707	39328	09441	8	
P05	(-8)	-.57907	66332	83208	36569		
P06	(-10)	.11818	44813	27759	24759		
P07	(-13)	-.16653	62193	82123	3350		
P08	(-16)	.15438	27144	62720	9573		
P09	(-20)	-.79209	96531	98236	77		
Q00	(12)	.32668	08396	34565	27909	15278	690
Q01	(10)	.13500	46013	40775	10408	73025	120
Q02	(7)	.24320	12558	04672	73220	26381	392
Q03	(4)	.23070	88173	24016	18054	94102	29
Q04	(1)	.10000	00000	00000	00000	00000	0

Table 88

P00	(6)	.29001	47709	98102	42530	27
P01	(4)	-.94966	90519	69751	00379	195
P02	(3)	.12250	18946	07943	86072	9088
P03	(0)	-.86253	60649	33020	96117	396
P04	(-2)	.38002	55604	71199	68408	4702
P05	(-4)	-.11252	75127	68698	79077	1041
P06	(-7)	.23246	27080	22246	89089	912
P07	(-10)	-.33918	02217	85585	52000	53
P08	(-13)	.34407	42671	70818	04416	33
P09	(-16)	-.22724	75441	36718	12037	4
P10	(-20)	.78744	27397	63408	1298	

Q00	(15)	.63717	05740	40533	69932	10003	2182
Q01	(13)	.26230	90563	65019	01674	32603	3140
Q02	(10)	.49093	25879	74359	01828	41919	6600
Q03	(7)	.52853	00187	40065	81960	03300	1593
Q04	(4)	.33253	42922	75896	11620	01663	6228
Q05	(0)	.99999	99999	99999	99999	99999	998

Table 89

P00	(6)	.93120	36319	14513	68868	71506	
P01	(5)	-.31177	92427	35663	77076	91157	80
P02	(3)	.41626	19277	53886	80718	83211	81
P03	(1)	-.30750	44187	57804	04514	50202	86
P04	(-1)	.14451	79583	21058	61004	58782	184
P05	(-4)	-.46637	44438	01798	29433	86963	78
P06	(-6)	.10816	36814	63618	95593	55130	27
P07	(-9)	-.18513	08184	39336	83021	03298	4
P08	(-12)	.23654	95366	51135	73527	27736	2
P09	(-15)	-.22466	79473	00219	43783	15968	
P10	(-18)	.15432	73980	13214	12705	0139	
P11	(-22)	-.71141	90603	23767	22478	982	
P12	(-25)	.17556	95004	80043	95761	31	
Q00	(16)	.23850	61753	12803	12263	92714	2798
Q01	(13)	.78483	32318	86301	31515	58102	2851
Q02	(11)	.11558	30025	70009	44027	40904	9189
Q03	(7)	.96068	50934	32748	29529	93880	0131
Q04	(4)	.45557	66612	64923	13473	93437	5886
Q05	(0)	.99999	99999	99999	99999	99999	9981

Table 90

P00	(10)	.26986	70038	11352	44316	15620	4964
P01	(8)	-.90176	75690	80037	33883	80979	9822
P02	(7)	.12007	20456	63397	43291	07669	5535
P03	(4)	-.88434	85474	33530	76915	56871	6418
P04	(2)	.41448	77690	04247	89867	34527	0330
P05	(0)	-.13355	06055	06029	36758	79335	2234
P06	(-3)	.31004	56751	37885	65556	98860	5205
P07	(-6)	-.53379	79988	16690	71517	76670	5530
P08	(-9)	.69224	30900	72402	14935	17154	2631
P09	(-12)	-.67844	76576	41606	51182	97457	757
P10	(-15)	.49683	23159	53018	57241	82233	71
P11	(-18)	-.26257	63531	59569	85512	02774	25
P12	(-22)	.92036	48356	03006	19197	98018	
P13	(-25)	-.16751	62799	21274	57170	0417	
Q00	(19)	.68573	00317	48900	22953	31374	1258
Q01	(17)	.22662	55663	71126	46000	15300	0006
Q02	(14)	.34492	39475	86812	85396	24864	8017
Q03	(11)	.31148	55341	78616	63294	36492	6292
Q04	(8)	.17739	07090	08663	98418	25548	1197
Q05	(4)	.60974	92038	27939	03967	29757	9980
Q06	(0)	.99999	99999	99999	99999	99999	9981

Table 91

P00	(0)	-.20607	1
P01	(-1)	.14968	33
Q00	(2)	.26497	890
Q01	(1)	.10000	0000

Table 92

P00	(0)	-.49253	3731		
P01	(-1)	.36707	01976		
P02	(-3)	-.86537	1815		
P03	(-5)	.95112	542		
Q00	(2)	.96846	09262	2	
Q01	(1)	.10000	00000	0	

Table 93

P00	(3)	-.13096	26454	741	
P01	(1)	.95515	69069	298	
P02	(0)	-.21866	93900	307	
P03	(-2)	.21908	80766	77	
P04	(-5)	-.95956	60178	6	
Q00	(5)	.25110	37428	88197	
Q01	(3)	.26650	39594	0456	
Q02	(1)	.10000	00000	0000	

Table 94

P00	(3)	-.37328	28672	18625	08
P01	(2)	.28658	53788	40984	86
P02	(0)	-.73435	86789	78936	34
P03	(-2)	.91354	16230	05872	9
P04	(-4)	-.63482	86598	73246	
P05	(-6)	.25426	14774	33927	
P06	(-9)	-.51910	48562	918	
Q00	(5)	.79282	44466	40072	382
Q01	(3)	.49746	03427	02346	787
Q02	(1)	.10000	00000	00000	00

Table 95

P00	(6)	-.13020	20114	56138	4990	
P01	(4)	.97628	93991	26582	5277	
P02	(3)	-.23858	66247	99477	8895	
P03	(1)	.27549	71430	36142	112	
P04	(-b)	-.17165	16215	53591	337	
P05	(-4)	.58647	23355	10818	2	
P06	(-7)	-.93139	50877	41343		
Q00	(8)	.26463	53567	18163	84971	8
Q01	(6)	.21166	22318	28460	45443	
Q02	(3)	.70254	20532	21274	3374	
Q03	(1)	.10000	00000	00000	000	

Table 96

P00	(6)	-.24760	17926	52527	41902	1
P01	(5)	.18907	22917	73495	97024	90
P02	(3)	-.47993	57093	78080	49092	7
P03	(1)	.59116	06052	53432	22151	
P04	(-1)	-.41022	37311	28822	53525	
P05	(-3)	.16991	56013	33390	3385	
P06	(-6)	-.41208	17107	40655	423	
P07	(-9)	.48574	49149	77159	6	
Q00	(8)	.52139	36987	01854	07142	563
Q01	(6)	.34125	44113	64408	75227	24
Q02	(3)	.90591	54921	41895	59421	5
Q03	(1)	.10000	00000	00000	00000	

Table 97

P00	(6)	-.44206	06316	64703	01796	451
P01	(5)	.34214	41074	34521	57626	3525
P02	(3)	-.89254	78599	57577	94209	378
P03	(2)	.11496	76166	69222	15233	861
P04	(-1)	-.85576	16184	35589	10704	68
P05	(-3)	.39672	39664	02055	75113	8
P06	(-5)	-.11721	10128	76047	61944	7
P07	(-8)	.21230	06490	96124	9958	
P08	(-11)	-.19314	70247	11626	33	

Q00	(8)	.95593	68378	23433	56718	38872
Q01	(6)	.52162	95697	57600	15285	3857
Q02	(4)	.11334	02547	03917	20534	6133
Q03	(1)	.10000	00000	00000	00000	00

Table 98

P00	(6)	-.74948	40835	52947	95013	54570
P01	(5)	.58607	36500	14057	65391	95188 5
P02	(4)	-.15604	24690	08402	27509	68823 4
P03	(2)	.20763	89722	59504	99903	04243
P04	(0)	-.16231	44956	84898	41305	45500
P05	(-3)	.81014	27767	72721	72414	021
P06	(-5)	-.26881	85626	13405	40798	431
P07	(-8)	.59527	64732	95516	84333	3
P08	(-11)	-.83610	84260	33883	2652	
P09	(-14)	.60496	10764	26828	470	

Q00	(9)	.16542	09156	28346	92850	90171 514
Q01	(6)	.76430	83123	49907	38342	71989 0
Q02	(4)	.13849	74248	88346	52281	39922 7
Q03	(1)	.10000	00000	00000	00000	0000

Table 99

P00	(9)	-.49021	69289	96935	89095	90583	099
P01	(8)	.37887	00099	71689	89776	47469	313
P02	(6)	-.98606	97420	47008	39755	11624	520
P03	(5)	.12679	19780	20370	47647	51433	354
P04	(2)	-.94542	09365	26442	76315	77261	3
P05	(0)	.44330	54923	37280	29789	19913	1
P06	(-2)	-.13563	95773	91295	59396	51633	
P07	(-5)	.27041	43017	90737	13920	6859	
P08	(-8)	-.33084	37294	51362	01058	36	
P09	(-11)	.19811	28563	28684	43769		
Q00	(12)	.10578	28193	09925	49776	07431	4239
Q01	(9)	.58334	85238	55804	31338	12775	7567
Q02	(7)	.14031	15784	39292	43805	18191	754
Q03	(4)	.17675	97280	84814	38454	77862	05
Q04	(1)	.10000	00000	00000	00000	00000	

Table 100

P00	(0)	.38499	26
P01	(-1)	-.10257	45
P02	(-3)	-.99144	1
P03	(-4)	.88653	3

Table 101

P00	(2)	.41030	25119
P01	(0)	-.45656	6286
P02	(0)	-.13721	56329
P03	(-2)	.48588	1125
P04	(-4)	-.64130	874
Q00	(2)	.82380	3953
Q01	(1)	.10000	00000

Table 102

P00	(5)	.10450	83687	0218
P01	(3)	-.11075	40638	660
P02	(2)	-.34640	97647	000
P03	(1)	.11944	57068	158
P04	(-1)	-.14611	16860	58
P05	(-4)	.72567	86922	3

Q00	(5)	.20765	43798	715
Q01	(3)	.23840	70518	719
Q02	(1)	.10000	00000	00

Table 103

P00	(5)	.31529	54135	59965	38
P01	(3)	-.52791	22787	04107	20
P02	(3)	-.10218	16964	28659	71
P03	(1)	.40436	55506	69910	3
P04	(-1)	-.61755	69053	96536	5
P05	(-3)	.48943	49415	00294	
P06	(-5)	-.21556	62247	7158	
P07	(-8)	.47269	10861	318	

Q00	(5)	.70257	55445	39365	43
Q01	(3)	.46530	36544	84571	8
Q02	(1)	.10000	00000	00000	

Table 104

P00	(8)	.10489	91483	58853	28361
P01	(6)	-.14945	09100	32166	8417
P02	(5)	-.34271	90179	56230	3015
P03	(4)	.12822	17142	21833	1849
P04	(2)	-.18175	28683	60134	052
P05	(0)	.12931	94178	37777	578
P06	(-3)	-.48672	42651	42390	5
P07	(-6)	.83271	64077	3054	
Q00	(8)	.22346	44320	54671	6901
Q01	(6)	.18722	06165	80078	6967
Q02	(3)	.65648	11592	66024	83
Q03	(1)	.10000	00000	00000	00

Table 105

P00	(8)	.20417	96894	49057	51578	30
P01	(6)	-.33393	06382	10082	53297	8
P02	(5)	-.66198	95967	02600	89168	5
P03	(4)	.25939	44637	98960	40804	0
P04	(2)	-.39267	47810	00176	45785	
P05	(0)	.31122	90776	17902	7349	
P06	(-2)	-.14203	94275	29152	7491	
P07	(-5)	.37145	39422	32842	39	
P08	(-8)	-.46512	66523	59789		
Q00	(8)	.45185	89611	68870	57499	3
Q01	(6)	.30793	62609	90701	83211	4
Q02	(3)	.85665	58332	22222	0197	
Q03	(1)	.10000	00000	00000	000	

Table 106

P00	(8)	.37108	72279	66610	48077	918
P01	(6)	-.66697	24732	75913	51646	374
P02	(6)	-.11955	04519	48597	50702	2065
P03	(4)	.48461	75629	79315	38342	683
P04	(2)	-.76785	72335	38729	03850	28
P05	(0)	.65286	01465	06453	20932	1
P06	(-2)	-.33347	72483	93308	96177	6
P07	(-4)	.10626	19263	89562	05928	
P08	(-7)	-.20462	91067	26072	814	
P09	(-10)	.19581	86247	96144	75	

Q00	(8)	.84482	19323	84230	25211	123
Q01	(6)	.47771	31520	03713	35445	42
Q02	(4)	.10810	07969	03112	20740	71
Q03	(1)	.10000	00000	00000	00000	

Table 107

P00	(8)	.63803	84658	30724	14808	61248	4
P01	(7)	-.12276	92737	99977	65279	65709	0
P02	(6)	-.20447	41359	43376	43633	46509	9
P03	(4)	.85048	79008	93395	49334	67056	
P04	(3)	-.13930	80736	47275	56335	72635	
P05	(1)	.12439	28622	88223	27378	7410	
P06	(-2)	-.68402	34491	90933	47396	676	
P07	(-4)	.24478	66706	47433	92551	90	
P08	(-7)	-.57642	15463	90718	64275		
P09	(-10)	.85224	09969	79882	2919		
P10	(-13)	-.64388	23327	29963	77		

Q00	(9)	.14843	42289	30145	72406	24265	1
Q01	(6)	.70794	40883	12729	54900	2266	
Q02	(4)	.13295	00361	48540	55562	6430	
Q03	(1)	.10000	00000	00000	00000	00	

Table 108

P00	(11)	.40489	63600	75052	76000	65719	626
P01	(9)	-.72471	90548	32039	57218	89482	59
P02	(9)	-.13043	31545	56085	90706	88819	191
P03	(7)	.52763	57996	93596	02603	59607	66
P04	(5)	-.83505	32867	18032	82749	54580	18
P05	(3)	.71172	62808	08521	64881	15549	0
P06	(1)	-.36799	08248	11944	01432	21538	
P07	(-1)	.12154	33144	52373	85343	81078	
P08	(-4)	-.25790	73771	05876	80888	348	
P09	(-7)	.33247	16339	10476	83287	5	
P10	(-10)	-.20814	07448	39659	67698		
Q00	(11)	.92060	62224	60625	96585	20822	080
Q01	(9)	.52261	91871	71925	27396	53776	10
Q02	(7)	.12982	20071	90860	34515	18822	1
Q03	(4)	.16958	26901	20732	33721	18141	
Q04	(1)	.10000	00000	00000	00000	000	

Table 109

P00 (0) .80114 1

Table 110

P00 (0) .79793 031
P01 (0) .14353 62

Table 111

P00 (0) .26171 86321 89
P01 (0) .84694 40441 3
P02 (0) .10026 59951

Q00 (0) .32801 56089 22
Q01 (1) .10000 00000 00

Table 112

P00	(-1)	.29768	08560	65044	9
P01	(0)	.64266	87693	51174	0
P02	(1)	.24092	62155	53313	3
P03	(1)	.11289	48920	7277	
Q00	(-1)	.37308	76252	13223	6
Q01	(0)	.79847	04670	22731	3
Q02	(1)	.28770	61761	21412	3
Q03	(1)	.10000	00000	0000	

Table 113

P00	(-2)	.29177	23301	03545	2698
P01	(0)	.12643	64421	28204	2419
P02	(1)	.13002	12267	53963	0771
P03	(1)	.31941	66311	56968	244
P04	(1)	.11880	13976	29480	7
Q00	(-2)	.36568	23861	93180	7169
Q01	(0)	.15777	89259	40426	6010
Q02	(1)	.16006	97941	23271	6622
Q03	(1)	.37307	27640	40664	179
Q04	(1)	.10000	00000	00000	0

Table 114

P00	(-3)	.22980	01486	24013	96508	0
P01	(-1)	.16707	75458	84828	84036	04
P02	(0)	.34080	28938	30209	45238	6
P03	(1)	.22320	60399	09037	91011	6
P04	(1)	.40303	37152	13244	86447	
P05	(1)	.12405	96523	19948	311	
Q00	(-3)	.28801	17750	27570	93582	3
Q01	(-1)	.20886	06282	08306	18706	65
Q02	(0)	.42327	26378	27814	35280	6
Q03	(1)	.27219	15826	73522	26423	8
Q04	(1)	.46081	70539	68621	26929	
Q05	(1)	.10000	00000	00000	000	

Table 115

P00	(-4)	.15426	46476	00407	32249	3139
P01	(-2)	.16891	89908	35378	88002	4701
P02	(-1)	.57569	13494	23021	95364	3144
P03	(0)	.74057	77017	02174	50336	082
P04	(1)	.34847	89909	83862	61862	544
P05	(1)	.49264	24082	52074	82083	30
P06	(1)	.12887	31078	30838	78760	

Q00	(-4)	.19334	20637	25579	84606	1064
Q01	(-2)	.21134	60429	05612	97880	2364
Q02	(-1)	.71759	67531	55483	36887	3148
Q03	(0)	.91511	46518	87836	75065	332
Q04	(1)	.42082	75526	89818	87006	379
Q05	(1)	.55182	58685	98997	09120	24
Q06	(1)	.10000	00000	00000	00000	

Table 116

P00	(-6)	.91542	73166	01801	35379	53168
P01	(-3)	.14050	23724	04361	82491	28906 71
P02	(-2)	.72029	91897	25919	28666	87355 8
P03	(0)	.15422	94860	24976	07058	23162 07
P04	(1)	.14134	55744	61436	77506	51769 9
P05	(1)	.51099	56996	33866	77131	83117
P06	(1)	.58880	28195	15982	13693	8904
P07	(1)	.13335	73488	24604	00300	79

Q00	(-5)	.11473	17997	58182	81171	90066 2
Q01	(-3)	.17587	84875	36209	90399	24282 15
Q02	(-2)	.89948	56204	08013	28665	63278 9
Q03	(0)	.19164	45435	10156	07157	85685 38
Q04	(1)	.17371	77200	47083	19589	29846 0
Q05	(1)	.61096	82370	19232	01646	10470
Q06	(1)	.64658	77938	52166	80188	3268
Q07	(1)	.10000	00000	00000	00000	00

Table 117

P00	(-8)	.31889	82066	31170	67677	07462	7421
P01	(-6)	.74015	51139	53709	60952	12019	4978
P02	(-4)	.61627	66651	50786	62771	16400	6352
P03	(-2)	.23579	19146	84851	97028	41896	0133
P04	(-1)	.44186	71777	76314	86434	30727	8616
P05	(0)	.40086	04754	91618	36898	66248	7139
P06	(1)	.16348	98988	36712	72553	49720	7647
P07	(1)	.25499	83597	63221	52136	76360	244
P08	(1)	.10770	34108	12787	39235	89097	5
P09	(-1)	.38287	23939	54369	12713	502	

Q00	(-8)	.39967	96307	35405	80071	44966	4561
Q01	(-6)	.92689	74688	16920	76335	96213	1532
Q02	(-4)	.77065	80523	57457	19272	62984	2557
Q03	(-2)	.29409	39568	61436	75684	65431	3069
Q04	(-1)	.54842	59780	55207	56751	45590	7765
Q05	(0)	.49263	43547	83712	99934	30654	0140
Q06	(1)	.19653	96658	71985	60644	89478	8772
Q07	(1)	.28937	84853	70369	72522	23957	200
Q08	(1)	.10000	00000	00000	00000	00000	0

Table 118

P00 (0) 79826 41

Table 119

P00 (0) .79788 50474
P01 (0) .14883 228

Table 120

P00 (0) .79160 47783 202
P01 (0) .94630 40026

Q00 (0) .99212 94575 874
Q01 (1) .10000 00000 0

Table 121

P00	(0)	.12157	43742	73508	886
P01	(1)	.13014	75578	01039	8
P02	(1)	.10141	30036	3672	
Q00	(0)	.15237	08820	12241	144
Q01	(1)	.16025	88201	25634	9
Q02	(1)	.10000	00000	0000	

Table 122

P00	(-1)	.17622	49333	50556	7422
P01	(0)	.36309	39137	55769	529
P02	(0)	.86193	76570	42028	0
P03	(-1)	.94223	76424	66	
Q00	(-1)	.22086	52003	15733	6961
Q01	(0)	.45092	95127	78684	908
Q02	(1)	.10000	00000	00000	00

Table 123

P00	(-2)	.82481	21435	11961	18371
P01	(0)	.29446	05096	13772	46280
P02	(1)	.17169	93925	97167	8786
P03	(1)	.10598	26665	24018	4
Q00	(-1)	.10337	48720	09304	21309 8
Q01	(0)	.36711	32407	29911	55930
Q02	(1)	.20850	97878	47086	0234
Q03	(1)	.10000	00000	00000	0

Table 124

P00	(-3)	.84595	73108	88274	00367	31
P01	(-1)	.46505	71664	06270	21781	67
P02	(0)	.50632	64376	25484	43572	
P03	(0)	.88294	16486	68464	950	
P04	(-1)	.84124	99827	58820		

Q00	(-2)	.10602	50257	30167	75779	115
Q01	(-1)	.58087	47520	84425	65274	6
Q02	(0)	.62389	96900	97812	36934	
Q03	(1)	.10000	00000	00000	00000	

Table 125

P00	(-4)	.27180	32012	00859	59381	45902
P01	(-2)	.30059	53731	79950	21313	25580
P02	(-1)	.84659	28489	77458	59615	2819
P03	(0)	.63992	21281	03093	52442	57
P04	(0)	.90096	22676	22894	82737	
P05	(-1)	.76918	53056	21486	88	

Q00	(-4)	.34065	47946	32646	68373	68951
Q01	(-2)	.37610	17030	78123	95073	65563
Q02	(0)	.10540	60748	03912	08805	71610
Q03	(0)	.78295	96059	51999	86753	85
Q04	(1)	.10000	00000	00000	00000	0

Table 126

P00	(-6)	.21661	27774	23535	11519	11641	6720
P01	(-4)	.51753	28326	48813	61731	93721	9217
P02	(-2)	.38320	13753	14743	64305	91107	4996
P03	(0)	.10544	46923	58985	37410	02893	1679
P04	(1)	.10248	03192	51418	24751	45179	07
P05	(1)	.27699	14641	93746	75055	22836	
P06	(1)	.11515	35887	56801	75997	948	

Q00	(-6)	.27148	38562	68092	38207	69719	2771
Q01	(-4)	.64812	21834	53192	32835	71746	7651
Q02	(-2)	.47906	17214	21613	48574	52526	9971
Q03	(0)	.13126	93963	35399	97828	43557	5346
Q04	(1)	.12606	63536	21396	88526	48028	81
Q05	(1)	.32571	88662	43734	76015	57534	
Q06	(1)	.10000	00000	00000	00000	000	

Table 127

P00 (0) .37153 0

Table 128

P00 (0) .91799 04

Q00 (1) .24484 9551

Q01 (1) .10000 00

Table 129

P00 (-1) .35669 13540 857

P01 (0) .35834 60148 90

P02 (0) .24641 74623 8

Q00 (-1) .95117 70607 919

Q01 (0) .99719 87212 38

Q02 (1) .10000 00000 00

Table 130

P00	(-2)	.39385	06567	45841	
P01	(0)	.10479	08570	67108	1
P02	(0)	.49719	52741	8047	
P03	(0)	.21946	39514	443	

Q00	(-1)	.10502	68420	85588	4
Q01	(0)	.28403	71931	37274	5
Q02	(1)	.14397	36572	77058	
Q03	(1)	.10000	00000	0000	

Table 131

P00	(-2)	.43854	62480	32497	7
P01	(0)	.16621	61732	22031	76
P02	(1)	.13531	74320	74168	58
P03	(1)	.19606	58746	53157	

Q00	(-1)	.11694	56661	99834	70
Q01	(0)	.44835	94975	57159	26
Q02	(1)	.37930	56623	80951	96
Q03	(1)	.65181	27362	09502	
Q04	(1)	.10000	00000	0000	

Table 132

P00	(-3)	.36093	15747	36395	4258
P01	(-1)	.23950	45846	35302	3802
P02	(0)	.42360	33418	62362	0769
P03	(1)	.21642	09003	15222	3141
P04	(1)	.22313	97735	87148	62

Q00	(-3)	.96248	41993	17764	8804
Q01	(-1)	.64288	97605	50296	1820
Q02	(1)	.11567	83388	82575	72521
Q03	(1)	.62198	10567	84424	8009
Q04	(1)	.78553	15333	79569	99
Q05	(1)	.10000	00000	00000	0

Table 133

P00	(-4)	.25008	39058	12557	32009	5
P01	(-2)	.25631	54934	15145	64229	59
P02	(-1)	.79248	95736	43978	86954	0
P03	(0)	.87668	28172	75923	80768	5
P04	(1)	.31735	44765	74155	62693	2
P05	(1)	.24894	22245	98367	4780	
Q00	(-4)	.66689	04155	00985	68419	1
Q01	(-2)	.68642	56279	99100	70826	98
Q02	(0)	.21426	77055	09815	09558	38
Q03	(1)	.24251	95142	18104	32784	80
Q04	(1)	.93498	12877	26198	72073	1
Q05	(1)	.92402	92424	90837	9926	
Q06	(1)	.10000	00000	00000	000	

Table 134

P00	(-7)	.73333	52319	74602	59305	9416
P01	(-4)	.12505	17156	34547	60692	84262 0
P02	(-3)	.71920	78244	98891	78985	03751
P03	(-1)	.17475	85404	59542	58171	34770 1
P04	(0)	.18400	02986	70065	26965	63356
P05	(0)	.76913	70830	15003	00582	9948
P06	(0)	.98586	82858	88468	79781	308
P07	(0)	.15977	08382	47871	79639	6
Q00	(-6)	.19555	60618	59899	11689	11339
Q01	(-4)	.33432	67994	62691	26989	13296 4
Q02	(-2)	.19323	20912	31100	52144	47035 3
Q03	(-1)	.47415	83644	32083	54175	53157 7
Q04	(0)	.50969	59770	13651	58821	59382
Q05	(1)	.22369	49501	40285	91912	37510
Q06	(1)	.32930	84754	59172	96936	6803
Q07	(1)	.10000	00000	00000	00000	00

Table 135

P00	(-8)	.36111	80301	32006	60827	40357	5
P01	(-6)	.81145	61281	87192	43783	87215	07
P02	(-4)	.64582	46121	25622	21539	81474	08
P03	(-2)	.23209	79894	61025	60507	53950	427
P04	(-1)	.39816	84579	49710	12131	58365	382
P05	(0)	.31711	38119	74933	88552	35142	15
P06	(1)	.10492	35401	39107	52789	58632	33
P07	(1)	.11002	45412	86154	21600	97987	
P08	(0)	.15038	01970	96227	06814	898	
Q00	(-8)	.96298	14136	85353	29239	89763	8
Q01	(-5)	.21680	96052	18401	43963	85979	941
Q02	(-3)	.17315	89141	01649	19693	62766	814
Q03	(-2)	.62629	53206	32515	50586	94285	656
Q04	(0)	.10875	99449	74536	61982	08240	8305
Q05	(0)	.88795	88123	81732	82127	37040	37
Q06	(1)	.31075	71887	54958	61560	12276	93
Q07	(1)	.37972	62346	54141	80108	92694	
Q08	(1)	.10000	00000	00000	00000	0000	

Table 136

P00	(-9)	.16531	34800	74504	54149	13540	2613
P01	(-7)	.47226	56937	08242	36902	35400	3351
P02	(-5)	.49599	48424	50523	61104	45213	5303
P03	(-3)	.24687	39670	48998	20217	88576	9539
P04	(-2)	.62650	67551	76413	59776	31899	7012
P05	(-1)	.81261	40206	98215	83157	61362	5263
P06	(0)	.51168	40555	76262	27316	90271	3923
P07	(1)	.13822	02042	00309	76875	94465	7754
P08	(1)	.12130	37213	65758	69809	24094	17
P09	(0)	.14218	24538	91217	62423	71204	
Q00	(-9)	.44083	59468	65345	55762	12489	8219
Q01	(-6)	.12613	03840	48951	33718	43496	4070
Q02	(-4)	.13281	27516	07318	81364	42223	8537
Q03	(-3)	.66401	91712	22370	37008	75465	8789
Q04	(-1)	.16984	98012	20044	54797	45432	9829
Q05	(0)	.22354	56354	40768	90747	03665	3726
Q06	(1)	.14488	00605	83911	49658	69750	4711
Q07	(1)	.41690	52260	10898	32492	16564	6470
Q08	(1)	.43213	47211	26016	20912	08723	37
Q09	(1)	.10000	00000	00000	00000	00000	0

Table 137

P00 (0) .37458 57

Table 138

P00 (0) .86491 9325

Q00 (1) .23064 57218

Q01 (1) .10000 000

Table 139

P00 (0) .18215 96605 0727

P01 (1) .11888 51398 733

Q00 (0) .48575 90947 5685

Q01 (1) .33827 89537 272

Q02 (1) .10000 00000 0

Table 140

P00 (-1) .18987 17407 19799 9

P01 (0) .27843 37349 36926

P02 (0) .26832 97608 813

Q00 (-1) .50632 46419 20575 4

Q01 (0) .76464 16617 64550

Q02 (1) .10000 00000 0000

Table 141

P00 (-1) .14702 09217 28495 543

P01 (0) .40140 35450 04122 70

P02 (1) .14029 77934 78162

Q00 (-1) .39205 57912 76005 192

Q01 (1) .10875 61894 18666 134

Q02 (1) .41783 06117 40593 2

Q03 (1) .10000 00000 000

Table 142

P00	(-2)	.10490	55786	90264	87075
P01	(-1)	.46757	15764	93703	1974
P02	(0)	.36133	93860	53303	67
P03	(0)	.24840	19545	88062	
Q00	(-2)	.27974	82098	40706	63015
Q01	(0)	.12590	96521	49642	23368
Q02	(1)	.10158	90284	54324	931
Q03	(1)	.10000	00000	00000	0

Table 143

P00	(-3)	.67527	82429	94108	22921	6
P01	(-1)	.45405	05075	71004	91445	
P02	(0)	.64276	59055	74611	8858	
P03	(1)	.15712	41437	68075	125	
Q00	(-2)	.18007	41981	31762	20046	63
Q01	(0)	.12186	79599	69092	74713	1
Q02	(1)	.17655	78600	99397	70151	
Q03	(1)	.48532	60560	01904	715	
Q04	(1)	.10000	00000	00000	0	

Table 144

P00	(-4)	.37040	56364	63070	33570	19
P01	(-2)	.35309	34949	66191	37899	37
P02	(-1)	.80701	01997	53211	36550	4
P03	(0)	.43133	69342	68374	39405	
P04	(0)	.23391	55386	51196	62	
Q00	(-4)	.98774	83639	01520	89637	52
Q01	(-2)	.94590	40523	35245	73955	64
Q02	(0)	.21924	33556	76564	53729	92
Q03	(1)	.12374	19308	85688	59614	8
Q04	(1)	.10000	00000	00000	000	

Table 145

P00	(-6)	.94930	79418	11991	57273	09831
P01	(-3)	.16075	43730	22251	27163	13694 0
P02	(-2)	.77335	28519	02406	91819	4463
P03	(0)	.11987	37733	29894	48244	2680
P04	(0)	.49341	54397	22331	85877	03
P05	(0)	.22250	44254	31231	5533	

Q00	(-5)	.25314	87844	83197	75272	88082 9
Q01	(-3)	.42978	58539	91450	71420	95957 3
Q02	(-1)	.20808	27022	88222	51244	85575
Q03	(0)	.32835	79236	38519	59384	8115
Q04	(1)	.14413	59242	72963	84304	987
Q05	(1)	.10000	00000	00000	00000	

Table 146

P00	(-7)	.19041	64201	49320	00401	66644 433
P01	(-5)	.51070	11742	18620	71543	49179 564
P02	(-3)	.43223	69476	12937	08590	35537 784
P03	(-1)	.13933	22107	43533	37539	78200 97
P04	(0)	.16386	94759	05001	86073	62037 3
P05	(0)	.55014	00927	31402	10367	1207
P06	(0)	.21306	67965	31005	17316	2

Q00	(-7)	.50777	71203	98186	67737	77747 479
Q01	(-4)	.13640	91322	81806	39745	37572 5758
Q02	(-2)	.11585	49537	50768	02094	73433 0894
Q03	(-1)	.37648	95073	87993	21602	21047 64
Q04	(0)	.45239	28490	81329	42891	96557 1
Q05	(1)	.16340	20412	61950	31413	44145
Q06	(1)	.10000	00000	00000	00000	00