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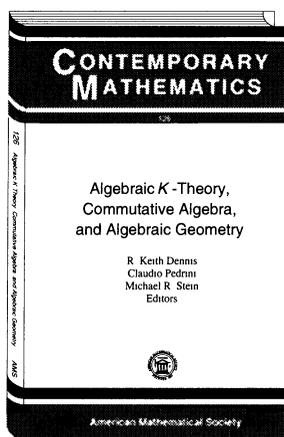
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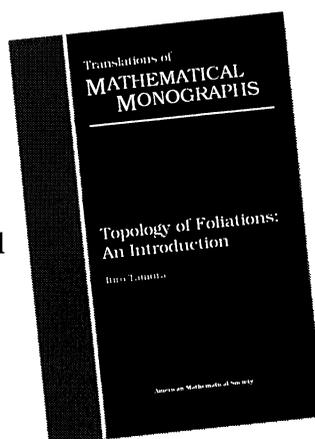
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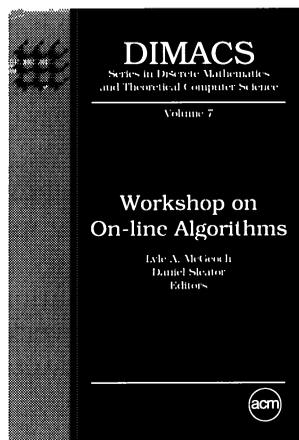
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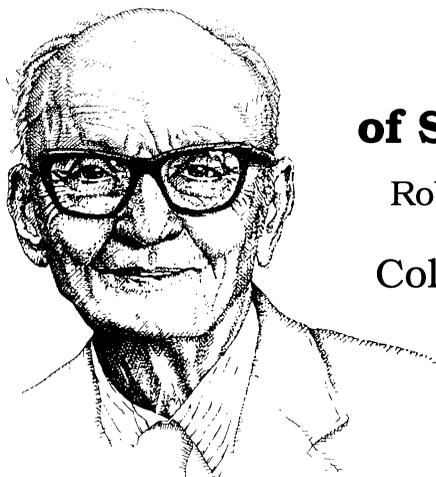
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(Continued from back cover)

|  |     |
|--|-----|
| <b>F. Gouvêa and B. Mazur</b> , Families of modular eigenforms .....   | 793 |
| <b>Dorian Goldfeld</b> , On the computational complexity of modular symbols .  | 807 |
| <b>R. Ernvall and T. Metsänkylä</b> , Computation of the zeros of $p$ -adic $L$ -<br>functions .....   | 815 |
| <b>Daniel C. Mayer</b> , Multiplicities of dihedral discriminants .....  | 831 |
| <b>Ilaria Del Corso</b> , Factorization of prime ideal extensions in number rings  | 849 |
| <b>Reviews and Descriptions of Tables and Books</b> .....  | 855 |
| Hämmerlin and Hoffmann <b>6</b> , Banks and Kunisch <b>7</b> , Roose, de Dier,<br>and Spence, Editors <b>8</b> , Dongarra, Duff, Sorensen, and van der Vorst<br><b>9</b> , Rivlin <b>10</b> , Nevai and Pinkus, Editors <b>11</b> , Wolfram <b>12</b> , Chudnovsky<br>and Jenks, Editors <b>13</b> |     |
| <b>Index to Volume 58</b> .....  | 865 |
| <b>Supplement to “Hierarchical bases for elliptic problems”</b> by <b>W. Dörfler</b> ..  | S29 |
| <b>Supplement to “Error estimates with smooth and nonsmooth data for a<br/>finite element method for the Cahn-Hilliard equation”</b> by <b>Charles M.<br/>Elliott and Stig Larsson</b> .....   | S33 |
| <b>Supplement to “Computation of the zeros of <math>p</math>-adic <math>L</math>-functions”</b> by <b>R.<br/>Ernvall and T. Metsänkylä</b> .....   | S37 |
| <b>Supplement to “Multiplicities of dihedral discriminants”</b> by <b>Daniel C.<br/>Mayer</b> .....  | S55 |

No microfiche supplement in this issue

# MATHEMATICS OF COMPUTATION

## TABLE OF CONTENTS

APRIL 1992

|   |     |
|---|-----|
| <b>L. Ridgway Scott and Shangyou Zhang</b> , Higher-dimensional nonnested multigrid methods .....   | 457 |
| <b>James H. Bramble and Joseph E. Pasciak</b> , The analysis of smoothers for multigrid algorithms .....  | 467 |
| <b>P. S. Vassilevski</b> , Hybrid $V$ -cycle algebraic multilevel preconditioners ...   | 489 |
| <b>W. Dörfler</b> , Hierarchical bases for elliptic problems .....  | 513 |
| <b>Guo Ben-yu and J. J. H. Miller</b> , Iterative and Petrov-Galerkin methods for solving a system of one-dimensional nonlinear elliptic equations                          | 531 |
| <b>Koichi Nijima</b> , A posteriori error bounds for piecewise linear approximate solutions of elliptic equations of monotone type .....                                    | 549 |
| <b>Ricardo Durán and Elsa Liberman</b> , On mixed finite element methods for the Reissner-Mindlin plate model .....   | 561 |
| <b>M. Costabel, F. Penzel, and R. Schneider</b> , Error analysis of a boundary element collocation method for a screen problem in $\mathbb{R}^3$ .....                      | 575 |
| <b>C. Chen, V. Thomée, and L. B. Wahlbin</b> , Finite element approximation of a parabolic integro-differential equation with a weakly singular kernel                      | 587 |
| <b>Charles M. Elliott and Stig Larsson</b> , Error estimates with smooth and nonsmooth data for a finite element method for the Cahn-Hilliard equation .....                | 603 |
| <b>Gerard R. Richter</b> , The discontinuous Galerkin method with diffusion ...   | 631 |
| <b>Anton Arnold and Francis Nier</b> , Numerical analysis of the deterministic particle method applied to the Wigner equation .....   | 645 |
| <b>Noel J. Walkington</b> , Convergence of nonconforming finite element approximations to first-order linear hyperbolic equations .....                                     | 671 |
| <b>G. Plonka and M. Tasche</b> , Efficient algorithms for periodic Hermite spline interpolation .....   | 693 |
| <b>Carl de Boor and Amos Ron</b> , Computational aspects of polynomial interpolation in several variables .....   | 705 |
| <b>Harvey Dubner</b> , Partitions approximated by finite cosine-series .....  | 729 |
| <b>M. Di Natale, L. Gotusso, R. Pavani, and D. Roux</b> , On the choice of parameter in a method for the inversion of Fourier series .....                                  | 737 |
| <b>Sotirios E. Notaris</b> , On Gauss-Kronrod quadrature formulae of Chebyshev type .....   | 745 |
| <b>N. M. Temme</b> , Asymptotic inversion of incomplete gamma functions ...   | 755 |
| <b>J. B. Keiper</b> , Power series expansions of Riemann's $\zeta$ function .....   | 765 |
| <b>Jürgen Eichenauer-Herrmann and Harald Niederreiter</b> , Lower bounds for the discrepancy of inversive congruential pseudorandom numbers with power of two modulus ..... | 775 |
| <b>Gerard van der Geer, René Schoof, and Marcel van der Vlugt</b> , Weight formulas for ternary Melas codes .....   | 781 |

(Continued on inside back cover)