and of the arguments set out above. If  $X_1(r, r_{13}, r_{23}, z)$ were known exactly, then these arguments would be exact. However, no exact values of  $I_2$  appropriate to the square-mound potential are known so that any direct test of the success of our assumption that  $X_1$  is a function of *z* alone is not, at present, possible. Indirect evidence in support of our present arguments is, then, valuable and can be sought in two directions.

The first concerns the calculations of paper I for the temperature-independent case of hard spheres where a direct test shows that the value of  $I_2$  calculated on the assumption  $X_1$ = const is in error by about 2\%. The inherent similarity between the hard-sphere and squaremound-potential functions would make it plausible that *12* given by (20c) involves an error of a few percent. Because  $I_1$ , given by (18), is exact this would mean that  $K(n)$  computed from Eq. (21) is more accurate than our present calculated *h* itself.

The second indirect evidence suggesting a reasonable accuracy for our function  $I_2$  comes from the calculated data for the fourth virial coefficient. For hard spheres,

the value of *D* calculated under the assumption  $X_1$  $=$  const is found to be about  $\frac{1}{2}\%$  too high (see reference 3). For the present square-mound potential it has already been mentioned that the function *D<sup>M</sup>* resulting from the present approach is virtually the same as the approximate function derived by Hiroike<sup>6</sup> using entirely different arguments. It is possible that both sets of data are quite wrong but, in this case, there is the problem of explaining why they are so remarkably alike.

The present arguments take the calculation of *K* only as far as the cube term in *n,* although in paper I the quartic term was also determined for hard spheres. The formulas developed above could, after rather tedious although elementary calculation, be extended to include higher powers in *n*. However, such an extension would, in this case, be very doubtful in the absence of a direct check on the accuracy of  $I_2$  for the square-mound potential, which is, however, available for hard spheres. The inclusion of further terms must be associated with more information about the lower members of the set of functions  $X_i$ .

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# Electroelastic Properties of the Sulfides, Selenides, and Tellurides of Zinc and Cadmium\*

DON BERLINCOURT, HANS JAFFE, AND L. R. SHIOZAWA *Electronic Research Division, Clevite Corporation, Cleveland, Ohio*  (Received 11 September 1962)

A complete set of elastic, piezoelectric, and dielectric constants is presented for the sulfides, selenides, and tellurides of zinc and cadmium. The piezoelectric constants for the hexagonal crystals in this group are markedly higher than for the cubic crystals. An elementary model theory applied to these data leads to electric charges on the metal atom increasing from +0.066 *e* for ZnTe to +0.84 *e* for CdS. The elastic compliance increases regularly with increasing anion and cation weight, with no break between the cubic and hexagonal crystals. Pyroelectrie constants are given for CdS and CdSe. The quality factor of elastic resonances of CdS plates is measured as function of electric conductivity.

# **I. INTRODUCTION**

THE binary compounds crystallizing in the tetra-<br>hedrally coordinated cubic sphalerite and hexag-<br>onal wurtzite structures are the simplest crystals HE binary compounds crystallizing in the tetrahedrally coordinated cubic sphalerite and hexaglacking a center of symmetry and, hence, capable of exhibiting piezoelectric and related effects depending on polar symmetry. Compounds of the bivalent column I IB metals, zinc and cadmium, and the bivalent column VI elements, sulfur, selenium, and tellurium, are stable to high temperatures and can be made sufficiently insulating to allow precise measurements of piezoelectric, elastic, and dielectric constants. Such data eventually may serve to verify a quantitative theory of piezoelectricity and elasticity in these structure

types which have been of great interest since the earliest lattice theories of crystal elasticity.<sup>1</sup> Until recently, only cubic zinc sulfide crystals of natural origin were available for such measurements, but interest in semiconducting properties of II-VI compounds has led to growth processes yielding good crystals of most of these compounds. Piezoelectric<sup>2-4</sup>

<sup>\*</sup> Supported in part by Aeronautical Research Laboratory, U. S. Air Force, and Sandia Corporation.

<sup>&</sup>lt;sup>1</sup> M. Born, *Atomtheorie des Festen Zustandes* (B. G. Teubner, Leipzig, 1923); also, M. Born and M. Goeppert-Mayer, in Handbuch der Physik, edited by S. Flügge (Verlag Julius Springer, Berlin, 1933), pp. 623-794.<br><sup>2</sup> H.

Fourteenth Annual Symposium on Frequency Control, U. S. Army Research and Development Laboratory, Fort Monmouth,

New Jersey, 1960 (unpublished), p. 304.<br>
<sup>3</sup> A. R. Hutson, Phys. Rev. Letters 4, 505 (1960).<br>
<sup>4</sup> T. Tanaka and S. Tanaka, J. Phys. Soc. Japan 15, 726 (1960). The extremely low values found by these authors may be due to electric conductivity since they use a low-frequency method.

and elasti<sup>2,5-7</sup> constants of cadmium sulfide and the elastic constants of cadmium telluride<sup>8</sup> have already been reported. The present work<sup>9,10</sup> gives the first piezoelectric measurements on the selenides and tellurides of zinc and cadmium, and more complete data on cadmium sulfide, including the pyroelectric effect. For comparison, dynamic elastic and piezoelectric measurements were made on natural cubic zinc sulfide (sphalerite); the results agreed well with static measurements made more than 50 years<sup>11</sup> ago. Our results show a pronounced break in the level of piezoelectric effect between the hexagonal crystals CdS and CdSe, and the cubic crystals CdTe, ZnS, ZnSe, and ZnTe. We have not been able to obtain both cubic and hexagonal crystals of any single compound in adequate size or quality. The piezoelectric coupling between elastic and electric energy is of particular theoretical<sup>12</sup> and practical<sup>13,14</sup> interest in II-VI crystals, because their conductivity can be controlled. The attenuation of progressing elastic waves caused by such interaction has been reported.<sup>15</sup>

### **II. MEASUREMENT PROCEDURE**

## **A. Preparation of Test Specimens**

CdS, CdSe, and ZnTe crystals were grown from the vapor phase by a slightly modified Reynolds-Green<sup>16,10</sup> method. The CdS and CdSe crystals were grown from General Electric Company vacuum-purified, luminescent-grade powders. The ZnTe source material was prepared by reacting New Jersey Zinc Company "super-purity" Zn-11 with American Smelting and Refining Company "high-purity" tellurium. The normally *n-type* CdS and CdSe crystals were doped with approximately 10 ppm (parts per million) of copper acceptors, and the normally  $p$ -type ZnTe crystals were doped with 10 ppm of indium donors. The resistivities of these compensated crystals were increased further from  $10^6 - 10^7 \Omega$  cm to  $10^9 - 10^{10} \Omega$  cm by heating for 1 h at 700°C and quenching to room temperature. This

E. Gutsche, Physica Status Solidi 1, 30 (1961).

- Meeting, Monterey, California, March 1961. H. Jaffe, D. Berlin-court, and L. Shiozawa, Bull. Am. Phys. Soc. 6, 139 (1961).
- <sup>10</sup> Some of the present data and additional information on crystal
- growth and treatment are contained in L. R. Shiozawa et al., U. S. Air Force Report ARL 62-365, 1962 (unpublished).<br>
<sup>11</sup> W. G. Cady, *Piezoelectricity* (McGraw-Hill Book Company, Inc., New York, 1946), pp. 159, 229.<br>
<sup>12</sup>
	-

Letters 7, 237 (1961).<br><sup>14</sup> D. L. White, J. Appl. Phys. 33, 2547 (1962).<br><sup>16</sup> H. D. Nine and R. Truell, Phys. Rev. **123**, 799 (1961).<br><sup>16</sup> D. C. Reynolds and S. J. Czyzak, Phys. Rev. **79**, 543 (1950);

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- L. C. Green, D. C. Reynolds, S. J. Czyzak, and W. M. Baker; J. Chem. Phys. 29, 1375 (1958).

treatment tended to redissolve the compensating impurities that had partially precipitated during slow cooling of the original growth runs. Test specimens were sectioned from large, 25-100 g, single crystals by means of an abrasive-slurry band saw. Crystals were lapped with  $3-\mu$  garnet and lightly etched with HCl or 1:1 HNO<sub>3</sub> (for CdS-CdSe and ZnTe, respectively). Crystallographic orientation and dimensional orthogonality were held to a tolerance of  $\pm 1^{\circ}$ . The specimen dimensions were held to a tolerance of less than  $\pm 1\%$ . Some of the ZnTe specimens contained one or more twins, but since the (111) twin composition planes were parallel to the electroded faces, and since the twinning operation is a rotation about the (111) axis normal to the composition plane, the measurements were not affected by their presence. The CdS and CdSe crystals were twin free. Crystals were electroded with air-drying silver paint or, in the case of ZnTe, an electroless gold coating.

ZnSe and CdTe crystals were obtained from the General Electric Company Research Laboratories through the courtesy of Manuel Aven and Max Lorenz, respectively. A natural ZnS crystal (sphalerite) (originating from Sonora, Mexico) of greenish-yellow to brown color in transmitted light was at hand. (Ill) plates were prepared from these crystals as described for ZnTe. A bar elongated in the  $\lceil 110 \rceil$  direction was cut from the ZnS crystal to allow a more accurate determination of the elastic constants.

# **B. Piezoelectric, Dielectric, and Elastic Measurements**

### *Hexagonal Crystals*

The measurement scheme is similar to the one used by two of the authors on barium titanate crystals<sup>17</sup> and followed resonance methods largely established by Mason,<sup>18</sup> supplemented by contour mode resonances of square plates.<sup>19</sup> The electroelastic tensor for the dihexagonal polar crystal class  $(6mm=C_{6v})$  contains the following nonzero constants:

 $s_{11} = s_{22}, s_{33}, s_{12}, s_{13}=s_{23}, s_{44}=s_{55}, s_{66}=2(s_{11}-s_{12})$  $d_{31}=d_{32}, d_{15}=d_{24}, d_{33};$  $\epsilon_{11} = \epsilon_{22}, \epsilon_{33}.$ 

The following bars and plates were used: *A,* square plates perpendicular to the optic *(c)* axis; *B,* plates parallel to  $c$ ;  $C$ , bars with length perpendicular to  $c$ , thickness parallel to  $c$ ; D, bars with length at 30 $^{\circ}$ , 45 $^{\circ}$ , and 60° from *c* and width perpendicular to *c.* The plates were about 15 mm by  $2 \text{ mm}$  thick and the bars

<sup>6</sup> D. I. Bolef, N. T. Melamed, and M. Menes, J. Phys. Chem. Solids 17, 143 (1960).

<sup>&</sup>lt;sup>6</sup> H. J. McSkimmin, T. B. Bateman, and A. R. Hutson, J.<br>Acoust. Soc. Am. 33, 856 (1961).<br>A<sup>T.</sup> E. Cutsche Bhusine Status Solidi 1, 20, (1961).

<sup>8</sup> H. J. McSkimmin and D. G. Thomas, J. Appl. Phys. **33,** 56 (1962). <sup>9</sup> A partial account was given at the American Physical Society

<sup>17</sup> D. Berlincourt and H. Jaffe, Phys. Rev. **Ill,** 143 (1958).

<sup>18</sup> W. P. Mason, *Piezoelectric Crystals and Their Application to Ultrasonics* (D. Van Nostrand Company, Inc., Princeton, New Jersey, 1950).

<sup>19</sup> IRE Standards on Piezoelectric Crystals: Determination of the Elastic, Piezoelectric, and Dielectric Constants—The Electromechanical Coupling Factor, 1958, Proc. Inst. Radio Engrs. 46 765 (1958).

were about 20 mm long, 4 mm wide, and less than 1 mm thick.

The dielectric constants at constant stress  $(\epsilon_{33}^T \text{ and }$  $\epsilon_{11}$ <sup>T</sup>) were measured on *A* and *B* plates at 10 kc/sec in the dark. The dielectric constants at constant strain  $(\epsilon_{33}^8 \text{ and } \epsilon_{11}^8)$  were measured at frequencies above the thickness extensional mode  $(\epsilon_{33}^S)$  or thickness shear mode  $(\epsilon_{11}^S)$  and its first five overtones.

The piezoelectric constants  $d_{31}$  or  $d_{31}'$  and the elastic constants  $s_{11}^E$  or  $s_{11}^{\prime E}$  were determined from the fundamental extensional mode of bars *C* and *D.* The elastic constant  $s_{44}^D = 1/c_{44}^D$  was measured using overtones of the thickness shear mode of plates *B* with small circular driving electrodes. Harmonics up to the 25th were readily measured. In similar fashion, the elastic constant  $c_{33}$ <sup>*D*</sup> was obtained from overtones of the thickness extensional mode of plates *A*, and in this case harmonics up to the 17th were readily measured. The planar Poisson's ratio  $-s_{12}E/s_{11}E$  was determined from the ratio of the resonance frequencies of the two fundamental extensional modes of plates *A,* and also from the ratio of the frequency constants of bars *C* and plates  $A$ . In each case the agreement was within 1.5%, and an average value was taken.

Rayleigh corrections to resonance frequencies were made for finite lateral dimensions of bars *C* and D, and all such corrections were less than  $1\%$ . A summary of directly measured values after Rayleigh correction is given in Table I. Results of static pressure tests used in determining the signs of piezoelectric constants are also summarized. The hydrostatic *d* constant  $(d_h = 2d_{31})$  $+d_{33}$ ) was measured using a calibrated hydrostatic stress. Within the resolution of the measurement, noted in Table I,  $d_h=0$ . From the data listed in the Table the complete sets of elastic and piezoelectric constants are obtained by calculation.17-19

#### *Cubic Crystals*

Only one crystal specimen was necessary for the measurements on the cubic crystals, a square plate with surface perpendicular to [111]. Defining *Z'* parallel to  $[111]$  and  $X'$  parallel to [110], the piezoelectric constant  $d_{31}$ <sup>'</sup> was obtained from the resonance and antiresonance frequencies of the fundamental extensional mode.<sup>19</sup> The piezoelectric constant referred to the cubic axes is then given by

$$
d_{14} = \sqrt{3}d_{33}' = -2\sqrt{3}d_{31}'.\tag{1}
$$

The elastic constants  $s_{11}^{\prime}$  *E* and  $s_{12}^{\prime}$  *E* were obtained from the ratio of the resonance frequencies of the two fundamental planar extensional modes of the square plate, as with the hexagonal crystals. This is justified by planar isotropy about [111], since  $s_{66} = 2(s_{11} - s_{12})$ . The elastic constant  $c_{33}^{\prime}$ <sup>*D*</sup> was obtained from overtones of the thickness extensional mode of the plate. The elastic constants referred to cubic axes are then obtained by solution of the set of simultaneous equations below

TABLE I. Directly measured constants of cadmium sulfide and cadmium selenide bars and plates (25°C).

	$_{\rm CdS}$	CdSe
Elastic constants, s in $10^{-11}$ m <sup>2</sup> /N, c in $10^{10}$ N/m <sup>2</sup>		
$S_{11}E$	2.069	2.338
$-s_{12}E/s_{11}E$	0.483	0.480
$s_{44}D^{'}$	6.412	7.466
$c_{33}D$	9.623	8.477
$s_{11}$ 'E(59° 25')		2.350
$s_{11}$ 'E(29° 10')		2.624
$s_{11}$ 'E(45° 30')	2.356	
$s_{11}$ 'E(29°)	2.318	
	Dielectric constants	
$\epsilon_{33}{}^{T}/\epsilon_0$	10.33	10.65
$\frac{\epsilon_{11}^T/\epsilon_0}{\epsilon_{11}^S/\epsilon_0}$	9.35	9.70
	9.02	9.53 <sub>5</sub>
$\epsilon_{33}{}^{T}/\epsilon_{0}(-196^{\circ}\rm{C})$	9.48	
$\epsilon_{11}{}^{T}/\epsilon_0$ ( $-196$ °C)	8.48	
	Piezoelectric coupling factors	
$k_{31}$	0.119 <sub>1</sub>	0.083 <sub>6</sub>
$k_{31}$ ' (59° 25')		0.141
$k_{31}^{37}(29°10')$ $k_{31}'(45°30')$		0.027
	0.150 <sub>3</sub>	
$k_{31}$ '(29°)	0.0356	
	Additional measurements	
$ d_h $ <0.05 $\times$ 10 <sup>-12</sup> C/N (CdS and CdSe)		
$d_{33}$ ~ +10 <sup>-11</sup> C/N (compression test, CdS and CdSe)		
$d_{31}$ negative (compression test, CdS and CdSe)		
$d_{31}$ '(29° 10') positive (compression test, CdSe)		
$d_{31}$ '(59° 25') positive (compression test, CdSe)		
$d_{31}$ '(29°) positive (compression test, CdS)		
$d_{31}$ '(45° 30') positive (compression test, CdS)		

and the inversion relation of the *c* matrix.

and

$$
c_{33}' = \frac{1}{3}(c_{11} + 2c_{12} + 4c_{44}),
$$
  
\n
$$
s_{11}' = \frac{1}{4}(2s_{11} + 2s_{12} + s_{44}),
$$
\n(2)

$$
s_{12} = \frac{1}{12} (2s_{11} + 10s_{12} - s_{44}).
$$

Due to the low piezoelectric coupling of ZnTe, CdTe, and ZnSe, the difference between open-circuit and short-circuit elastic constants may be neglected. Directly measured data are summarized in Table II.

For ZnS a bar elongated along  $\lceil 110 \rceil$  with thickness parallel to  $\lceil 001 \rceil$  was used, as well as a square plate perpendicular to  $\lceil 111 \rceil$ , allowing a more precise determination of the elastic constants. The elastic constants  $s_{11}$ <sup>'</sup><sup>*E*</sup> and  $s_{12}$ <sup>'</sup><sup>*E*</sup> were determined as with the cubic crystals, and  $c_{44}$ <sup>*D*</sup> = 1/s<sub>44</sub><sup>*D*</sup> was determined from overtones of the thickness shear mode of the [110] bar (electrodes on end or edge faces). Directly measured data are listed in Table II.

The volume resistivity of the CdTe specimen was only  $\sim$  2×10<sup>5</sup>  $\Omega$  cm at 25°C, increasing to  $\sim$  2×10<sup>9</sup> at —196°C. In view of this, the dielectric and piezoelectric measurements were made at  $-196^{\circ}$ C. Measurements on ZnS were repeated at  $-196^{\circ}$ C, and the low temperature  $d_{14}$  and  $e_{14}$  for CdTe were corrected to 25<sup>o</sup>C by arbitrarily applying the ratio between 25 and  $-196^{\circ}$ C values of  $d_{14}$  and  $e_{14}$  obtained for ZnS. Directly measured data are listed in Table II.

		ZnS ZnS ZnTe ZnSe $(25^{\circ}$ C) $(-196^{\circ}$ C) $(25^{\circ}$ C) $(25^{\circ}$ C) $(-196^{\circ}$ C)			CdTe
		Elastic constants, s in 10 <sup>-11</sup> m <sup>2</sup> /N, c in 10 <sup>10</sup> N/m <sup>2</sup>			
${\mathfrak{s}_1}_1{}'^E$	1.108	1.087 1.566		1.275	2.405 (2.445) $(at 25^{\circ}C)$
$-s_{12}^{\prime E}/s_{11}^{\prime E}$	0.414	0.416	0.380	0.407	0.458
$c_{33}^{\prime\prime}{}^{D}$	14.08	<b>Contract Advised</b>	9.249		11.77 7.535
$S_{44}D$		2.154 2.131	$\cdots$		
		Dielectric constants			
$\epsilon_{11}{}^{T}/\epsilon_0$		$8.37$ $8.14$ $10.10$		9.1 <sub>2</sub>	9.6 <sub>5</sub>
		Piezoelectric constants, $10^{-12}$ C/N			
$d_{31}$		$0.91_7$ $1.00_0$ $0.26_4$		0.31 <sub>s</sub>	0.48 <sub>5</sub>
		Density, $10^3$ kg/m <sup>3</sup>			
ρ	4.088	$4.099a$ 5.636		$5.26_2$	5.86

TABLE II. Directly measured constants on cubic ZnS, ZnTe, ZnSe, and CdTe.

 $^{\rm a}$  Corrected density assuming average thermal expansion of  $4$   $\times10^{-6}/{\rm degC}$  from  $\rm -196$  to  $\rm 25\,^{\rm o}C.$ 

# **C. Measurement of Pyroelectric Effects**

The pyroelectric effects in hexagonal CdS and CdSe were measured by immersing plates *A* in liquid nitrogen. A capacitance of  $1 \mu F$  was connected across the test specimen and an electronic electrometer was connected across this capacitor. The resistance of the test specimens was about  $10^8 \Omega$  at room temperature in the dark, and this resistance increases with decreasing temperature. The time constant was therefore greater than 100 sec, allowing sufficient time for temperature equilibrium.

# **D. Measurement of Open-Circuit** *Q* **of CdS with Varying Illumination Level**

The effect of illumination-controlled conductivity on the mechanical quality factor  $Q_M$  of CdS was determined by measurement of the resonance and antiresonance resistances of bars C. With the fundamental relationship  $Q = \omega U/P$ , with U the averaged stored energy and *P* the power dissipated, it can be shown by standard equivalent circuits of piezoelectric crystals<sup>20</sup> that, in the presence of high conductive losses,

$$
Q_{\rm MOC} = \frac{\omega_a C^T k_m^2 (1 - k_m^2) (R_r R_0^2 / X^2 + R_r + R_0)}{R_0^2 / X^2 + 1 - k_m^2}, \quad (3)
$$

where  $Q_{\text{MOC}}$  = open-circuit mechanical  $Q, R$ <sup>r</sup> = resonance resistance measured in the dark,  $C<sup>T</sup>$  = free capacitance measured in the dark,  $k_m^2 = (\omega_a^2 - \omega_r^2)/\omega_a^2$  (measured in the dark), and  $X = 1/\omega_a C^T (1 - k_m^2)$ .  $R_0$  in Eq. (3) actually represents the effective photoconductance at the antiresonance frequency. It is obtained by solution of the relationship below, with *Ra* the measured

resistance at antiresonance.

$$
R_a = \frac{X^2/R_r + R_0 + R_r}{X^2/R_0R_r + 2 + R_rR_0/X^2 + R_r/R_0}.\tag{4}
$$

The short-circuit mechanical *Q* is given by

$$
1/Q_{\rm MSC} = \omega_R R_r k_m^2 C^T. \tag{5}
$$

For determination of *QMOC* the impedance at antiresonance *Za* was measured as a function of illumination. The illumination was provided by a tungsten projection lamp, the output of which first passed through a water cell and a glass filter in order to remove the infrared. The illumination was calibrated at two distances between the light source and the test element using a thermopile, which was placed at the position of the CdS bar. The illumination was varied by changing the distance between the test specimen and the light source. The test specimen was illuminated on the face perpendicular to its width. This face was about 3.1 mm by 20 mm and the width was 4.5 mm. The crystal was fairly clear and, therefore, quite transparent to visible light with wavelength over about 5200 A.

### **III.** RESULTS

# **A. Piezoelectric, Elastic, and Dielectric Data**

Complete sets of piezoelectric, elastic, and dielectric constants for hexagonal CdS and CdSe are listed in

TABLE III. Elastic, dielectric, and piezoelectric constants of wurtzite CdS and CdSe, 25°C. *s* in 10<sup>-11</sup> m<sup>2</sup>/N; *d* in 10<sup>-12</sup> C/N; *c* in 10<sup>10</sup> N/m<sup>2</sup>; *e* in C/m<sup>2</sup>.

						Inversion of s tensor	
	CdS	CdSe		CdS		CdSe	$CdS^*$
${s_{11}}^E$	2.069	2.338	${c_{11}}^E$		9.07	7.41	8.581
$s_{33}E$	1.697	1.735	$c_{33}E$		9.38	8.36	9.370
$s_{12}E$	$-0.999$	$-1.122$	$c_{12}^E$		5.81	4.52	5.334
$s_{13}E$	$-0.581$	$-0.572$	$c_{13}{}^E$		5.10	3.93	4.615
$s_{44}E$	6.649	7.595	$c_{44}{}^E$		1.504	1.317	1.487
S66	6.136	6.920	$c_{66}$		1.630	1.445	
$s_{11}$ <sup>D</sup>	2.040	2.322	$c_{11}^{\phantom{1}D}$		9.13	7.42	
$s_{33}$ D	1.581	1.670	$c_{33}D$		9.623	8.477	
$s_{12}$	$-1.028$	$-1.138$	$c_{12}D$		5.88	4.53	
$s_{13}$ $D$	$-0.523$	$-0.539$	$c_{13}D$		4.97	3.86	
$s_{44}D$	6.412	7.466	$c_{44}D$		1.560	1.340	
$d_{31}$	$-5.18$	$-3.92$	$e_{31}$		$-0.244$	$-0.160$	$-0.244$
$d_{33}$	$+10.32$	$+7.84$	$e_{33}$		$+0.440$	$+0.347$	$+0.489$
$d_{15}$	$-13.98$	$-10.51$	$e_{15}$		$-0.210$	$-0.138$	
$k_{33}$	0.262	0.194	$\epsilon_{33}{}^{T}/\epsilon_{0} =$	10.33		10.65	
$k_{31}$	$0.119_1$	0.083 <sub>6</sub>	$\epsilon_{11}{}^{T}/\epsilon_{0} =$		9.35	9.70	
$k_{15}$	0.188 <sub>5</sub>	0.130 <sub>5</sub>	$\epsilon_{11}{}^{8}/\epsilon_0 =$		9.02	9.33	
k,	0.154	0.124	$\epsilon_{33}{}^{8}/\epsilon_0 =$		9.53	10.20	
		Estimated accuracy $(\pm)$					
	$_{\rm CdS}$	CdSe	CdS CdSe			CdS	$_{\rm CdSe}$
$\mathfrak{g}_{11}{}^{E,D}$	$0.2\%$	$0.2\%$ $d_{31}$	$2\%$	$3\%$	$\epsilon_{33}{}^{T}$	$2\%$	$2\%$
$S_{12}E,D$	$0.5\%$	$0.5\%$ $d_{33}$	$2\%$	$3\%$	$\epsilon_{11}{}^T$	$2\%$	$2\%$
$S_{44}E,D$	$0.2\%$	$0.2\%$ $d_{15}$	$3\%$	$4\%$	$\epsilon_{11}{}^{\mathbf{S}}/\epsilon_{11}{}^T$	$0.5\%$	$0.5\%$
$c_{33}^{\phantom i D}$	$0.2\%$	$0.2\%$ $k_{15}$	$3\%$	$4\%$			
$\mathfrak{s}_\mathbf{3}\mathbf{s}^{E,D}$	$3\%$	$1.0\%$ $k_{31}$	$1\%$	$2\%$			
$\mathfrak{s}_1\mathfrak{s}^{E,D}$	$5\%$	$1.5\%$ $k_{33}$	$4\%$	$4\%$			
		k,	$4\%$	$4\%$			

a See reference 6.

W. P. Mason, Proc. Inst. Radio Engrs. 23, 1252 (1935).

Elastic constant	Temperature coefficient at $25^{\circ}$ C, $10^{-6}$ / $^{\circ}$ C
	CdS
$S_{11}^E$	$+116$
$S_{12}E$	$+87$
$c_{33}D$	$-216$
$s_{44}D$	$+96$
	ZnS
	Average temperature coefficient
	$-196$ to 25°C, $10^{-6}$ /°C
${\mathfrak{s}_{11}}'^E$	$+98$
$S_{12}^{\prime}$ <sup>E</sup>	$+78$
$s_{44}D$	$+50$
	CdTe
${s_{11}}^{\prime E}$	$+74$

TABLE IV. Temperature coefficients of elastic constants (not corrected for thermal expansion).

Table III. Estimated accuracy limits are noted for most of the constants. The directly measured piezoelectric and elastic tensors are those for *d* and *s.* With the exception of  $c_{33}$  and  $c_{44}$ , which were measured directly, error limits in the *c* matrix may be considerably higher; the *c* matrix of McSkimmin *et al.<sup>6</sup>* is, therefore, shown and used for calculation of preferred values for  $e_{33}$  and  $e_{31}$  of CdS  $(e_{nj} = d_{ni}c_{ij}^E)$ .

Table IV shows temperature coefficients of several of the elastic constants of CdS at 25°C. In the temperature range  $-196$  to  $100^{\circ}$ C the elastic constants change almost linearly, and the transverse coupling factor  $k_{31}$ remains constant at  $0.119 \pm 0.001$ . The temperature coefficients of some of the elastic constants of ZnS and CdTe are also shown in Table IV. The temperature coefficients listed in the Table were not corrected for thermal expansion.

Complete sets of piezoelectric, elastic, and dielectric constants for cubic ZnS, ZnTe, ZnSe, and CdTe are shown in Table V. Error limits are also shown in Table V, and it is immediately evident that the errors in the elastic constants are relatively high for all except ZnS. The method of deriving a complete set of elastic constants from only one crystal plate, described in Sec. II B, involves a solution of a quadratic equation with near cancellation of terms. The extra bar used in the measurements on ZnS allows considerably higher accuracy. The higher error limits on the elastic compliance tensor for CdTe cause even larger errors in the elastic stiffness tensor (except  $c_{44}$ ) and the agreement with reference 8 is only fair.

## **B. Pyroelectric Data**

For CdS and CdSe the total changes of polarization from 25 to  $-196^{\circ}$ C were 0.090 and 0.077  $\mu$ C/cm<sup>2</sup>, respectively. In both cases, that crystal face which becomes positive on extension (positive side of Z axis) is negative with increasing temperature, so the pyroelectric constant at constant stress  $\left(\frac{\partial P}{\partial \theta}\right)_T$  is negative. If one assumes that the change in polarization is linear

with temperature in this range,<sup>21</sup> the pyroelectric coefficients  $(\partial P/\partial \theta)_T$  are  $-4 \times 10^{-4}$  and  $-3.5 \times 10^{-4}$  $\mu$ C/cm<sup>2</sup> °C for CdS and CdSe, respectively.

As noted, the pyroelectric measurements were made at constant stress, and piezoelectric charges due to thermal expansion were, therefore, included. The total pyroelectric effect in the temperature range  $-196~(\theta_1)$ to 25<sup>o</sup>C  $(\theta_2)$  is given by the following:

 $\Delta P_3$  (constant stress) =  $\Delta P_3$  (constant strain)

$$
+\int_{\theta_1}^{\theta_2} (e_{33}\alpha_3+2e_{31}\alpha_1)d\theta,\quad (6)
$$

where  $\alpha_3$ ,  $\alpha_1$ = thermal expansion coefficients parallel and perpendicular to *c,* respectively.

The integral in the equation above represents the secondary pyroelectric effect. Results shown in part A indicate that there is little variation with temperature of  $e_{33}$  or  $e_{31}$ . Thermal expansion coefficients have been determined only from 0 to 300°C. By extrapolation the average thermal expansion coefficients in the range  $-196$  to 25°C are in  $10^{-6}/$ °C:  $\alpha_1 = 4.0$ ,  $\alpha_3 = 2.1$  for CdS and  $\alpha_1 = 4.4, \alpha_3 = 2.45$  for CdSe. Using these the secondary effects are  $-0.0204$  and  $-0.0124$  for CdSe, respectively,

TABLE V. Piezoelectric, elastic, and dielectric constants of<br>cubic ZnS, ZnTe, ZnSe, CdTe. s in  $10^{-11}$  m<sup>2</sup>/N, c in  $10^{10}$  N/m<sup>2</sup>,<br>d in  $10^{-12}$  C/N, and e in C/m<sup>2</sup>. s<sub>44</sub><sup>B</sup> and s<sub>44</sub><sup>D</sup>, c<sub>4</sub><sup>B</sup> and c<sub>44</sub><sup>D</sup>, e<sub>11</sub><sup></sup>

	ZnS $(25^{\circ}C)$	ZnS $(-196^{\circ}C)$	ZnTe $(25^{\circ}C)$	ZnSe $(25^{\circ}C)$	CdTe $(-196^{\circ}C)$ (25°C)	CdTe <sup>b</sup>
$s_{11}$ $s_{12}$ $s_{44}{}^E$ $s_{44}{}^D$ $c_{11}$ $c_{12}$ $c_{44}E$ $c_{44}{}^D$ $\epsilon_{11}{}^T/\epsilon_0$ $\epsilon_{11}{}^{\bf 8}/\epsilon_0$ $d_{14}$ $e_{14}$	1.839 $-0.707$ 2.168 2.154 10.46 6.53 4.613 4.643 8.37 $8.3_2$ 3.1 <sub>8</sub> $0.14_7$ $0.079_5$	1.786 $-0.685$ 2.148 2.131 10.71 6.67 4.655 4.693 8.1 <sub>4</sub> 8.0 <sub>8</sub> 13.4 <sub>6</sub> $0.16_{2}$ 0.089	2.40 $-0.873$ 3.21 3.21 7.13 4.07 3.12 3.12 10.1 <sub>0</sub> 10.1 <sub>0</sub> 0.9 <sub>1</sub> 0.028 <sub>4</sub> 0.017	2.26 $-0.85$ 2.27 2.27 8.10 4.88 4.41 4.41 $9.1_{2}$ $9.1_{2}$ 1.1 <sub>0</sub> 0.049 0.026	3.83 $-1.58$ 5.11 5.11 6.15 4.30 1.96 1.96 9.6 <sub>5</sub> 9.6 <sub>5</sub> 1.6a <sup>3</sup> $0.0335$ * $0.026$ <sup>a</sup>	5.351 3.681 1.994
$k_{14}$		ZnS	Estimated accuracy $(\pm)$ ZnTe		ZnSe	CdTe
$s_{11}$ $S_{12}$ $s_{44}E, s_{44}D$		$0.2\%$ $0.5\%$ $0.2\%$	$1\%$ $1\%$ $1\%$		$2\%$ $2\%$ $3\%$	$1.5\%$ $1.5\%$ $1.5\%$
$d_{31}$ $\epsilon_{11}$ <sup>T</sup> , $\epsilon_{11}$ <sup>8</sup> $k_{14}$ $d_{14}$ $e_{14}$		$2\%$ $2\%$ $3\%$ $3\%$	$2\%$ $4\%$ $5\%$ $6\%$		$2\%$ $4\%$ $5\%$ $8\%$	$2\%$ $4\%$ $5\%$ 6%

\* Using ratios of values for ZnS at 25 and -196°C, these values are, respectively, 1.54, 0.0304, and 0.023 at 25°C.<br>respectively, 1.54, 0.0304, and 0.023 at 25°C.

<sup>21</sup> R. Frerichs and W. Minkus, Report on Contract No. AF 33(616)-5625, 1960 (unpublished). This report indicates that  $(\partial P/\partial \theta)_T$  is not constant with temperature for CdS, but the changes are not particularly pronounced.



FIG. 1.  $\rho$  and  $\rho_0$  for CdS vs perpendicular illumination.

representing only 23 and 16% of the total pyroelectric effect.

# **C. Dependence of Mechanical** *Q* **on Photoconductivity in CdS**

The variation of the effective dc volume resistivity<sup>22</sup>  $\rho$  vs incident light power for the CdS specimen is shown in Fig. 1. The effective resistivity  $\rho_0 = R_0 l w/t$ , where  $R_0$ is given by the solution of Eq. (4), is also shown as function of incident light power.  $\rho_0$  thus represents the effective volume resistivity at the antiresonance frequency. Figures 2 and 3 show the open-circuit mechanical Q as function of incident light power and  $\rho_0$ , respectively. The open-circuit *Q,* here associated with the elastic constant  $s_{11}$ <sup>D</sup>, goes through a minimum as function of light intensity, as noted by Hutson.<sup>3</sup> For comparison, the short-circuit mechanical *Q* for CdS is 10 000.

#### **IV. ELEMENTARY CALCULATION OF PIEZOELECTRIC EFFECTS FROM LATTICE DATA**

The availability of measured piezoelectric constants for a number of *AB* compounds invites a new attempt to relate these constants to atomic structure. As a first step, this may be done from the elementary assumption that the atoms may be replaced by point charges of fixed value and that nearest-neighbor distances *AB=b*  (bond length) remain equal during elastic deformation. For the cubic (sphalerite) structure, this approach<sup>23</sup> may be applied to an elastic shear strain  $S<sub>4</sub>$  coupled with a relative displacement of the *A* and *B* sublattices normal to the plane of shear, and gives the relation

$$
e_{14} = ne/d^2 = (3/16)ne/b^2, \tag{7}
$$

where *ne* is the effective charge of the atom and *d*   $= 4b/\sqrt{3}$  is the cubic lattice constant. Similar calculations may be made for the *ideal* hexagonal wurtzite lattice, in which each *A* atom is exactly at the center of a tetrahedron of *B* atoms and vice versa, just as in the sphalerite structure. The hexagonal lattice constants are then  $c=8b/3$  and  $a=(8/3)^{1/2}b$ ; *a* is the distance between nearest *like* atoms. We first consider a strain system  $S_3$ ,  $S_1 = S_2 = -\frac{1}{2}S_3$ , that is, an elongation parallel to the hexagonal axis and a contraction of one-half the amount in the basal plane, resulting in zero volume change. All strains are small compared to unity, and terms in *S<sup>2</sup>* are disregarded. The piezoelectric charge density is then

$$
D_3 = e_{31}S_1 + e_{31}S_2 + e_{33}S_3 = (e_{33} - e_{31})S_3. \tag{8}
$$

The condition of equal nearest-neighbor distance de-



FIG. 2. Mechanical *Q* at antiresonance for CdS lateral expander bar vs light intensity. *(Quoc* calculated from resistance at resonance and antiresonance.)

28 H. Jaffe, Phys. Rev. **66,** 357 **(1944).** 

<sup>22</sup> Most of the light which created the photoconductivity in this experiment is very highly absorbed by CdS, and the conductivity was, therefore, highest near the illuminated **surface,** hence the term "effective" volume resistivity.

mands that the strain  $S_3$  be entirely provided by a change in the spacing of the *AB* double layer, since the vectors connecting the *B* atoms in one double layer to the *A* atoms of the next double layer remain parallel to the *Z* axis, which is still a sixfold symmetry axis under the particular strain system applied (Fig. 4). Application of the Pythagoras theorem to the triangle *LMN*  (Fig. 4) before and after deformation shows that the prescribed lateral strain  $S_1 = S_2 = -\frac{1}{2}S_3$  is present.

The calculation of the electric charge density  $D_3$  of a system of double layers requires the fixing of a boundary condition for the whole crystal on the surfaces normal to the Z axis.<sup>24</sup> This is obtained from the requirement that the potential difference between these surfaces shall be zero before the crystal is strained. One may achieve this by placing single layers containing only one-fourth of the atoms at the two ends of the crystal, or by omitting one-fourth of the atoms from the outside half of the terminating double layers. The same result is obtained by assuming complete double layers and placing equal external charges of opposite sign on the end faces, such that they create a potential difference equal and opposite to that due to the summed potential steps in the double layers. Using the first approach, we have (Fig. 4)

$$
D_3 = \frac{3}{4} N n e c S_3 / 2, \qquad (9)
$$

where *N* is the number of *AB* molecules per unit volume. The hexagonal unit cell of volume  $\frac{1}{2}a^2c\sqrt{3}$ contains 2 molecules, whence

$$
D_3 = \frac{1}{2}\sqrt{3}neS_3/a^2. \tag{10}
$$

Comparison of Eqs. (10) and (8) gives

$$
e_{33}-e_{31}=+\sqrt{3}ne/2a^2=+(3\sqrt{3}/16)ne/b^2.
$$
 (11)



FIG. 3. QMOC VS  $\rho_0$  for CdS transverse expander bar. (QMOC calculated from resistance at resonance and antiresonance.)

The positive sign here indicates that extension along *Z*  gives positive charge on the *A* atom side of the double layer.

Next we consider an isotropic strain  $S_1 = S_2 = S_3$ , satisfied by an equal change of all bond lengths without change in bond angles, resulting in zero electric dis-



FIG. 4. Section through wurtzite lattice parallel to symmetry plane<br>
[parallel to hexagonal  $c(Z)$  and [parallel to hexagonal *c(Z)* and normal to  $a(X)$  axis]. entirely supplied by spacing change in two double layers of combined thickness one-fourth of unit cell height *c.* Curved lines indicate crystal boundaries for zero initial potential difference.

<sup>24</sup> This was not yet recognized in the abstract (reference 9) and the values for *n* in that abstract are partly incorrect.



FIG. 5. Shear strain  $S_4$  in symmetry plane of wurtzite lattice. Each double layer is rigidly rotated in respect to the *c* axis to satisfy equality of the bonds within the double layer.

placement:

$$
D_3 = (2e_{31} + e_{33})S_1 = 0,
$$
\nand

\n
$$
(12)
$$

$$
e_{31} = -\frac{1}{2}e_{33}.
$$

The effect of a shear strain *Si* in the *YZ* plane consists of a tilting of the *AB* double layers in respect to the *Z* axis (Fig. 5). Equality of the 3-dimensional bond framework inside the double layers requires the *B* atoms to remain on the normals at the centers *P* of equilateral triangles of *A* atoms in the tilted basal plane. This leads to a sidewise displacement of the *B*  atoms relative to the *A* atoms of  $S_4c/8$ , resulting in electric displacement

and

$$
e_{15} = e_{24} = D_2/S_4 = -\sqrt{3}ne/6a^2 = -(\sqrt{3}/16)ne/b^2. \quad (14)
$$

 $D_2 = -NnecS_4/8 = -\sqrt{3}n\epsilon S_4/6a^2$ 

By comparison with Eqs. (11) and (12)

$$
e_{15} = -\frac{1}{3}(e_{33} - e_{31}) = e_{31}.
$$
 (15)

 $(13)$ 

If our model of point charges is to retain the ideal wurtzite structure independent of temperature and hydrostatic pressure, symmetry permits only an isotropic change in lattice parameters as a result of temperature and pressure changes. The two thermal expansion coefficients must then be equal and the elastic constants satisfy

$$
s_{11} + s_{12} = s_{33} + s_{13}.\tag{16}
$$

The resultant electric displacement is zero, hence the pyroelectric effect disappears, and the piezoelectric strain constants satisfy

$$
d_h = d_{33} + 2d_{31} = 0. \tag{17}
$$

The preceding model considerations for the ideal wurtzite structure may also be applied to the sphalerite structure if the latter is referred to a trigonal [111]

TABLE VI. Effective atomic charge  $n$  on metal atom calculated from bond length  $b$  (in 10<sup>-10</sup> m) and piezoelectric constants  $e$  $(in C/m^2).$ 

	b		$e_{14}$	n		
Cubic						
ZnS	2.34		0.147	$+0.268$		
ZnSe	2.46		0.049	0.099		
ZnTel	2.64		0.0284	$+0.066$		
CdTe	2.81		0.031	0.081		
	Ь	r	$e_{15}$	n	$e_{33}-e_{31}$	n
Hexagonal						
ZnŌb	1.98	0.0188	$-0.5$	1.1	1.8	1.3
CdS	2.53	0.0058	$-0.210$	$+0.77$	0.731	$+0.90$
CdSe	2.63	0.0041	$-0.138$	$+0.55$	0.507	$+0.68$

\*  $r = 1 - (3/8)^{1/2}c/a$  indicates deviation from ideal wurtzite structure.<br>b The values for  $e_{18}$  and  $e_{28} - e_{21}$  were obtained using piezoelectric data of Hutson (see reference 3) and elastic data of T. B. Bateman [J.

axis (cube diagonal) as *Z* axis, because the two structures differ only by rotation of successive double layers around this axis. Indeed, if the elastoelectric matrix of the sphalerite class and Eq. (7) are transformed to this rotated coordinate system, Eqs. (11), (12), (15), (16), and (17) result, as well as the nonexistence of a pyroelectric effect. Landauer<sup>25</sup> derived a pyroelectric effect for the sphalerite lattice, but this paradoxical result is due to his failure to postulate zero potential difference before temperature change, as discussed above for stress application.

Equation (12) is well satisfied by  $e_{33}$  and  $e_{31}$  of CdS. For CdSe the deviation is probably within the limit of error of  $e_{33}$  and  $e_{31}$ . Equation (15) is only approximately fulfilled for both CdS and CdSe. This is expressed in alternate values for *n* in Table VI. It is noteworthy that Eq. (17) is satisfied by the experimental *d* constants of CdS and CdSe within their much closer tolerances, although it was derived from a more restricted model. The observed pyroelectric effect is small—the total change in moment from 77 to 300°K corresponds to only one-thousandth of the charge density of each layer and may well be related to temperature dependence of the deviation from ideal wurtzite structure, which also manifests itself in the observed anisotropy of thermal expansion. The elastic isotropy Eq. (16) is satisfied within  $5\%$  for CdS and CdSe.

Equations  $(7)$ ,  $(11)$ , or  $(14)$  can be used to calculate the effective charge for our model. The results are given in Table VI, which also includes hexagonal ZnO for which approximate piezoelectric data are available.<sup>3,12</sup> By convention, the sign of the piezoelectric constant  $d_{33}$  is taken to be positive in all crystals of class 6 mm.<sup>26</sup> To obtain the sign of the effective charge on the *A*  (metal) atoms from the piezoelectric data and the model theory, one must have an experimental connec-

<sup>&</sup>lt;sup>25</sup> R. Landauer, J. Chem. Phys. 32, 1784 (1960).<br><sup>26</sup> Standards on Piezoelectric Crystals, Proc. Inst. Radio Engrs. 37, 1387 (1949).

tion between the sign of  $d_{33}$  (hence,  $e_{33}$ ) and the  $AB$ sequence in the double layer. This has been obtained by x-ray intensity measurements for ZnS,27 CdS,28 CdSe,<sup>29</sup> and ZnTe.<sup>28,10</sup> In each case, a positive electric charge appears on an extension parallel to the *Z* axis on the metal side of the double layers; from this fact, our theory derives the positive charge of the metal atoms.

The values for effective charge *n* in Table VI show increasing polarity with increasing weight of the metal atom, Zn, Cd, and decreasing weight of the nonmetal, Te, Se, S, and O. These sequences conform with the general chemical rule that electronegativity decreases with increasing atomic number in each column of the periodic system, although it is of interest that Pauling<sup>30</sup> finds Cd to be slightly more negative than Zn on the basis of thermochemical data. If we accept the point of view that a tetrahedrally bonded fully covalent crystal would have two negative charges on the metal atom,<sup>31</sup> even the most weakly piezoelectric crystal studied, ZnTe, is found to be more than  $50\%$  ionic since *n* (Table VI) is still positive.

### **V. CONCLUSIONS**

The elastic data for the six II-VI compounds reported in this paper show great similarity with little distinction between the sphalerite and wurtzite structures<sup>32</sup> as shown by Table VII. The level of compliance increases smoothly with atomic number of both *A* and *B* atoms. The piezoelectric constants for the wurtzitetype crystals nearly satisfy the symmetry requirements of the cubic sphalerite type, but have much higher magnitude. We believe that the stronger piezoelectricity and the preference for the wurtzite structure are both direct consequences of increasing ionicity of the bond.

27 D. Coster, K. S. Knol, and T. A. Prins, Z. Physik 63, 345  $(1930).$ 

28 W. R. Cook, Jr. (private communication). 29 R. Zare, W. R. Cook, Jr., and L. R. Shiozawa, Nature **189,**  217 (1961).

30 L. Pauling, *The Nature of the Chemical Bond* (Cornell University Press, Ithaca, New York, 1960), 3rd ed., p. 93.<br><sup>31</sup> L. Pauling, reference 30, p. 246.<br><sup>32</sup> V. A. Zhdanov and L. Brysneva, Soviet Phys.—Cryst. 6,

514 (1962) have recognized this for ZnS and CdS.

TABLE VII. Short-circuit elastic constants normalized to  $s_{11}$ <sup>E</sup>.

	Cubic-Rotated		Cubic-Rotated		Hexagonal		
	ZrS	ZnTe	ZnSe	CdTe	CdS	CdSe	
$s_{12}/s_{11}$	$-0.42$	$-0.38$	$-0.41$	$-0.46$	$-0.48$	-0.48	
$s_{13}/s_{11}$	$-0.20$	$-0.20$	$-0.15$	$-0.26$	$-0.28$	$-0.245$	
$s_{33}/s_{11}$	0.78	0.82	0.74	0.80	0.81	0.74	
$s_{44}/s_{11}$	3.72	3.47	3.95	3.70	3.20	3.24	
$s_{66}/s_{11}$	2.84	2.76	2.82	2.92	2.96	2.96	
$s_{14}/s_{11}$	0.62	0.50	0.73	0.56	0	0	

The effective charges derived from the piezoelectric data appear reasonable. A quantitative theory should be based on lattice dynamics including nearest-neighbor repulsive forces, atom polarizability, and long-range forces, in addition to the Coulomb interactions. Bondangle-dependent forces will also be substantial in partly covalent tetrahedral structures. Theoretical efforts in some of these directions include those of von Hippel,<sup>33</sup> Birman,<sup>34</sup> Tolpygo,<sup>35</sup> and especially Cochran.<sup>36</sup> The break in the level of piezoelectric constants between the hexagonal and cubic crystals indicates the limited validity of the present geometric theory. It seemed worthwhile, however, to show that a purely geometric consideration produces results of the right order of magnitude and a reasonable chemical sequence.

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- <sup>33</sup> A. von Hippel, Z. Physik 133, 158 (1952).<br>
<sup>34</sup> J. L. Birman, Phys. Rev. 111, 1510 (1958).<br>
<sup>35</sup> K. B. Tolpygo, Fiz. Tverd. Tela 2, 2655 (1960) [translation:<br>
Soviet Phys.—Solid State 2, 2367 (1961)].<br>
<sup>36</sup> W. Cochn i
- W. Cochran, in *Advances in Physics,* edited by N. F. Mott (Taylor and Francis, Ltd., London, 1961), Vol. 10, p. 401.