

# THE PHYSICAL REVIEW

*A journal of experimental and theoretical physics established by E. L. Nichols in 1893*

SECOND SERIES, VOL. 135, NO. 3B

10 AUGUST 1964

## Nuclear Resonance Fluorescence in $\text{Cu}^{65}\dagger$

G. B. BEARD

*Argonne National Laboratory, Argonne, Illinois and Wayne State University, Detroit, Michigan*

(Received 27 March 1964)

The 1.114-MeV excited state of  $\text{Cu}^{65}$  has been investigated by means of nuclear resonant fluorescent scattering and self-absorption experiments. The level width was found to be  $(1.51 \pm 0.38) \times 10^{-3}$  eV, corresponding to a mean life of  $(4.4 \pm 1.1) \times 10^{-13}$  sec. Angular-distribution measurements of the resonantly scattered gamma rays gave  $\delta = (E2/M1)^{1/2} = -0.52_{-0.05}^{+0.07}$ . From these values,  $B(E2) \downarrow = (0.023 \pm 0.007) \times 10^{-48} \text{e}^2 \text{cm}^4$  and  $B(M1) \downarrow = (0.08 \pm 0.02) (\hbar/2Mc)^2$ . The lifetime agrees with other recent measurements, but the value for  $\delta$  disagrees with results from Coulomb-excitation experiments.

### I. INTRODUCTION

THE low-lying levels of  $\text{Cu}^{65}$  have recently been the subject of several investigations. Information about this nucleus is of interest in connection with the core-excitation model of the nucleus. Cline and Heath<sup>1</sup> have summarized the investigations of the decay scheme by use of  $\text{Ni}^{65}$ ; and Coulomb-excitation experiments have been carried out by several groups.<sup>2-4</sup>

In this work we are concerned with properties of the 1.114-MeV excited state of  $\text{Cu}^{65}$ . Angular-correlation measurements of the gamma rays from the level excited by Coulomb excitation have indicated that this state has a spin and parity of  $\frac{5}{2}^-$  and decays by a mixed  $E2$ - $M1$  transition. The angular-correlation measurements of the 368-1114-keV cascade by Cline and Heath<sup>1</sup> are in agreement with this spin and parity assignment.

The  $E2$  partial lifetime can be determined with good accuracy from Coulomb-excitation experiments. This information, together with a knowledge of the  $E2/M1$  mixing ratio, enables one to calculate the lifetime of the state. For the 1.114-MeV level, a mean life of less than  $10^{-13}$  sec is obtained with a relatively large error because of the uncertainty in the  $E2/M1$  mixing ratio. Another approach is to measure the lifetime of the

state directly by use of nuclear resonant fluorescent scattering. In principle, by measuring the resonant self-absorption and angular distribution of the resonantly scattered gamma rays, the total level width and mixing ratio of the  $E2$  and  $M1$  transitions can be obtained.

According to the decay scheme for  $\text{Ni}^{65}$ , sufficient energy is available to enable the recoil from transitions populating the 1.114-MeV state of  $\text{Cu}^{65}$  to compensate for the recoil Doppler shift occurring in the emission and absorption of the 1.114-MeV photon. Therefore, it appeared feasible to investigate the properties of this level by means of nuclear resonance fluorescence.

### II. EXPERIMENTAL DETAILS

#### 1. Source

The lifetime was expected to be somewhat longer than the collision times for atoms in a solid or liquid. Hence, it was desirable to use a gaseous source so that only a negligible fraction of the recoiling  $\text{Cu}^{65}$  nuclei would undergo collisions with a resultant loss of memory before being de-excited to the ground state. For practical reasons, it was necessary to find an easily produced stable nickel compound having a boiling point below  $1200^\circ\text{C}$ . We found only one compound that fulfilled these conditions, namely, anhydrous  $\text{NiCl}_2$  which has a boiling point of  $975^\circ\text{C}$ .

The recoil energy imparted to the Cu atom in the decay of  $\text{Ni}^{65}$  can be as high as 16.5 eV. This energy usually will be shared among the atoms of the  $\text{NiCl}_2$  molecule and can cause the molecule to break up. Be-

<sup>†</sup> Work supported by the U. S. Atomic Energy Commission and the National Science Foundation.

<sup>1</sup> J. E. Cline and R. L. Heath, *Phys. Rev.* **131**, 296 (1963).

<sup>2</sup> B. Elbek, H. E. Gove, and B. Herskind (to be published).

<sup>3</sup> R. L. Robinson, F. K. McGowan, and P. H. Stelson (to be published).

<sup>4</sup> K. I. Erokhina and I. Kh. Lemberg, *Bull. Acad. Sci. (USSR) Phys. Ser.* **26**, 205 (1962).

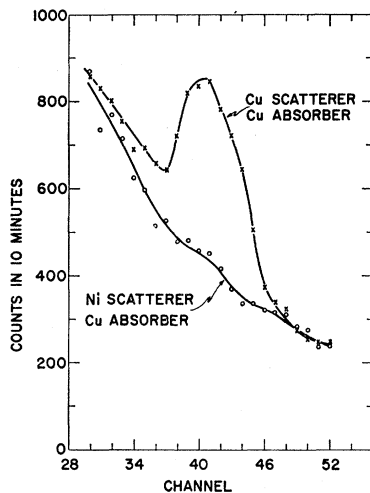


FIG. 1. Resonantly scattered 1.114-MeV quanta. The upper curve shows the scattering with the Cu scatterer and absorber in position and the lower with the comparison Ni scatterer. The runs were of 10-min duration. The nonresonant scattering data were corrected for source decay.

cause the details of the energy sharing processes are complicated and unknown, the effective source strength for photons having the proper energy to be resonantly scattered cannot be determined. Fortunately, this trouble can be avoided by carrying out a resonant self-absorption experiment.

The samples of  $\text{NiCl}_2$  were prepared by adding concentrated HCl to metallic nickel enriched to 99.5%  $\text{Ni}^{64}$ . The mixture was gently heated in a quartz ampoule until the nickel disappeared. Then the system was evacuated and heated further until only anhydrous  $\text{NiCl}_2$  remained. In the first preparations, to help eliminate possible contaminants, the  $\text{NiCl}_2$  was distilled into a second quartz ampoule which was then sealed off. Later work showed this precaution to be unnecessary. The two strongest sources used in the final runs each contained about 14-mg  $\text{NiCl}_2$  in 5-cc ampoules.

The encapsulated samples were irradiated for periods of 6–24 h in a neutron flux of  $(5-7) \times 10^{13}$  neutrons  $\text{cm}^{-2} \text{sec}^{-1}$  in the Argonne CP-5 reactor. The ampoules were then heated to  $1025^\circ\text{C}$  to vaporize the source. Tests made with variations of up to  $\pm 25^\circ$  about this operating temperature showed no change in the resonant fluorescent scattering.

The irradiation of the quartz ampoules produced some undesirable background activities, notably those of  $\text{Si}^{31}$  and  $\text{Cl}^{38}$ . The strong  $\text{Si}^{31}$  activity had a half-life of 2.5 h and decayed over 99.9% by pure  $\beta^-$  emission. Consequently, its background contribution consisted chiefly of bremsstrahlung and caused little trouble. The 37-min  $\text{Cl}^{38}$  activity, however, contained high-energy gamma rays which after being Compton scattered could still give rise to a varying background in the 1.114-MeV region of interest. This difficulty was

avoided by delaying the data taking until after the  $\text{Cl}^{38}$  activity had decreased by an order of magnitude.

The disadvantage of the undesirable  $\text{Si}^{31}$  and  $\text{Cl}^{38}$  activities was more than offset by the ease of handling the relatively strong  $\text{Ni}^{65}$  activities produced and by the fact that the ampoules could be used several times for the complete cycle of irradiation plus heating with no sign of physical deterioration and negligible buildup of long-lived background activity.

## 2. Self-Absorption Measurements

A conventional cylindrical symmetry was used for the resonant scattering experiments.<sup>5</sup> The resonant scatterer consisted of a Cu ring, 1 ft in diameter, 4 in. high, and  $\frac{1}{2}$  in. thick. A similar one of nickel was used for comparison measurements. A  $3 \times 3$ -in. NaI(Tl) crystal was used to detect the resonantly scattered photons and the data were recorded with a multichannel pulse-height analyzer. No resonant scattering was noted with the source at room temperature in the preliminary runs, although an effect amounting to a few percent above background could have escaped detection.

The self-absorption measurements were made with Cu and Ni absorbers which had been matched to within  $\frac{1}{2}\%$  for electronic absorption at room temperature by use of the 1.114-MeV gamma rays from a  $\text{Zn}^{65}$  source. The absorbers were lined with Al foil which acted as a heat reflector and served to keep their temperatures within  $10^\circ\text{C}$  of room temperature. Each run to determine the resonant absorption was of 10-min duration, and the Ni and Cu absorbers were alternated so that corrections for source decay and a changing dead time in the analyzer were limited to less than 1%. After

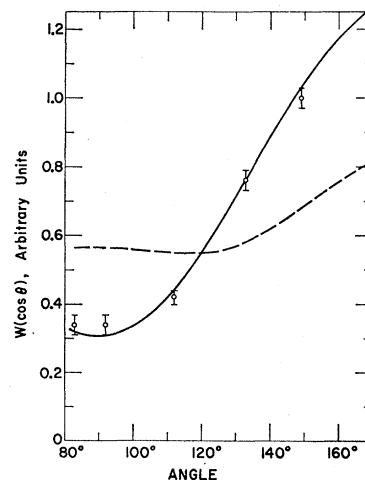


FIG. 2. Angular-correlation data. The solid curve represents the fit to the data for  $A_2=1.02$  and  $A_4=0.07$ . The dashed curve shows the theoretical angular distribution, corrected for the finite angular resolution, for the assumption of pure  $E2$  transitions for a spin sequence of  $\frac{3}{2}-\frac{1}{2}-\frac{3}{2}$ . The two curves are normalized at  $120^\circ$ .

<sup>5</sup> G. B. Beard and W. H. Kelly, Nucl. Phys. 43, 523 (1963).

corrections for source decay were made, individual background contributions measured with the Cu and Ni absorbers and the Ni scatterer agreed to within statistical uncertainties. An average of these was then used for background corrections. Figure 1 shows the observed effect in typical 10-min runs with the Cu absorber in position. As a check, the number of resonantly scattered photons under the photopeak for various runs was plotted against time. The half-lives obtained in this way agreed with the half-life for the decay of  $\text{Ni}^{65}$ .

### 3. Angular-Distribution Measurements

For the angular-distribution measurements, the 3- $\times$ 3-in. NaI(Tl) crystal was replaced by a 2- $\times$ 2-in. crystal. The Cu scatterer remained fixed and the crystal position was varied to change the scattering angle over the range from about  $90^\circ$  to  $150^\circ$ .

## III. EXPERIMENTAL RESULTS

### 1. Lifetime

The resonant absorption was found by forming the ratio  $(C_{\text{Ni}} - C_{\text{Cu}})/(C_{\text{Ni}} - b)$ , where  $C_{\text{Ni}}$  and  $C_{\text{Cu}}$  are the counting rates for Ni and Cu absorbers, respectively, and  $b$  is the background rate. An average of four runs gave an absorption of  $(5.6 \pm 1.4)\%$  for an average path length of 0.33 in. in the copper absorber. As a first approximation,<sup>6</sup> the equation relating the level width  $\Gamma$  to the resonant absorption  $A$  is

$$A = nd(g_2/g_1)\Gamma\lambda^2/4[\pi(\Delta_a^2 + \Delta_s^2)]^{1/2},$$

where

$$\Delta_v^2 = 2kT_v E^2/Mc^2.$$

Here  $n$  is the number of resonant scatterers per  $\text{cm}^3$ ,  $d$  the average absorber thickness (in cm),  $g_2/g_1$  the statistical factor,  $\lambda$  the wavelength of the gamma of energy  $E$ ,  $k$  the Boltzmann constant,  $T_v$  the effective temperature of the absorber or scatterer,  $M$  the atomic mass of the resonant nucleus,  $c$  the speed of light, and  $\Delta_a$  and  $\Delta_s$  are the Doppler widths of absorber and scatterer, respectively.

The numerical values are as follows:  $n = 2.61 \times 10^{22}$  atom/ $\text{cm}^3$ ,  $g_2/g_1 = \frac{3}{2}$ ,  $\lambda^2 = 1.24 \times 10^{-20}$   $\text{cm}^2$ , and (by use of a Debye temperature<sup>7</sup> of  $330^\circ\text{C}$  and the Lamb correction for crystalline binding<sup>6</sup>)  $\Delta_a = 1.08$  eV and  $\Delta_s = 1.06$  eV. This gives a level width of  $1.46 \times 10^{-3}$  eV for an absorption of 5.6%. However, there was a relatively large self-absorption in the  $\frac{1}{2}$ -in.-thick scatterer. Taking this into account, a more accurate calculation gives a level width of  $(1.51 \pm 0.38) \times 10^{-3}$  eV for the 1.114-MeV state of  $\text{Cu}^{65}$ . From the uncertainty principle, the corresponding mean life is  $(4.4 \pm 1.1) \times 10^{-13}$  sec.

<sup>6</sup> F. R. Metzger, Phys. Rev. **103**, 983 (1956); *Progress in Nuclear Physics*, edited by O. R. Frisch (Pergamon Press, London, 1959), Vol. 7, p. 54.

<sup>7</sup> N. F. Mott and H. Jones, *The Theory of the Properties of Metals and Alloys* (Dover Publications, New York, 1958), p. 14.

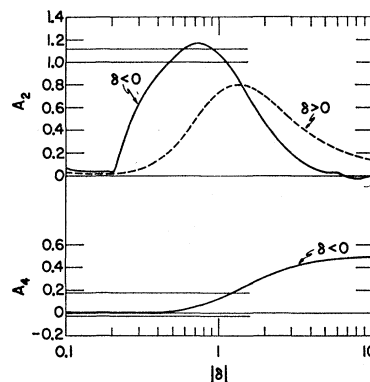


FIG. 3. Theoretical values of  $A_2$  and  $A_4$  as a function of the mixing ratio  $\delta = (E2/M1)^{1/2}$ . The solid curves represent negative values of  $\delta$  while the dashed curve for  $A_2$  is for positive  $\delta$ . The pairs of lines show the experimentally allowed ranges of  $A_2$  and  $A_4$ , after correction for the finite angular resolution.

### 2. Angular Distribution

Figure 2 shows the average angular distribution of two separate runs. The solid curve shows  $W(\cos\theta) = 1 + A_2^2 P_2(\cos\theta) + A_4^2 P_4(\cos\theta)$ , where  $P_2(\cos\theta)$  and  $P_4(\cos\theta)$  are Legendre polynomials,  $A_2 = 1.02$ , and  $A_4 = 0.07$ . These values for  $A_2$  and  $A_4$  were obtained by a least-squares fit to the data points. The dashed line shows the theoretical angular distribution for pure  $E2$  transitions for  $\frac{3}{2} - \frac{7}{2} - \frac{3}{2}$  spin sequence. The experimental points clearly are in disagreement with a  $\frac{7}{2}$  spin assignment to the 1.114 MeV state.

Theoretical values of  $A_2$  and  $A_4$  as a function of the mixing ratio  $\delta = (E2/M1)^{1/2}$  are shown in Fig. 3 on the assumption that the decay proceeds by a  $\frac{3}{2} - \frac{5}{2} - \frac{3}{2}$  spin sequence with the same  $E2/M1$  mixing ratio in each part. The pairs of straight lines show the limits on the values of  $A_2$  and  $A_4$  based on results of the present work. A correction for the finite angular resolution has been made. From the curves it can be seen that either  $\delta = -0.52_{-0.05}^{+0.07}$  or  $\delta = -1.02_{-0.12}^{+0.09}$  will give agreement with the experimental results. It will be shown in the discussion that only  $\delta = -0.52$  is compatible with other results for the  $E2$  and  $M1$  partial lifetimes.

## IV. DISCUSSION

By combining the measured values of  $(4.4 \pm 1.1) \times 10^{-13}$  sec for the mean life and  $\delta = -0.52_{-0.05}^{+0.07}$  one finds an  $E2$  partial lifetime  $\tau(E2) = (2.1 \pm 0.7) \times 10^{-12}$  sec and an  $M1$  partial lifetime  $\tau(M1) = (5.6 \pm 1.5) \times 10^{-13}$  sec. It follows that the reduced transition probabilities for de-excitation are  $B(E2)\downarrow = (0.023 \pm 0.007) \times 10^{-48}$   $e^2\text{cm}^4$  and  $B(M1)\downarrow = (0.08 \pm 0.02) (e\hbar/2Mc)^2$ . On the other hand, for  $\delta = -1.02_{-1.02}^{+0.09}$ ,  $\tau(E2) = (8.6 \pm 2.3) \times 10^{-13}$  sec and  $\tau(M1) = (9.0 \pm 2.5) \times 10^{-13}$  sec.

Recently, other measurements of the lifetime of the 1.114-MeV state have been made, one by the Doppler-

TABLE I. Values for  $B(E2)\downarrow$  and the corresponding  $\tau(E2)$  from Coulomb-excitation measurements.

$B(E2)\downarrow$ ( $e^2 \times 10^{-48}$ cm $^4$ )	$\tau(E2)$ ( $10^{-12}$ sec)	Reference
0.0170	2.9	Elbek <i>et al.</i> (Ref. 2)
0.019	2.6	Erokhina and Lemberg (Ref. 4)
$0.0230 \pm 0.0025$	$2.14 \pm 0.23$	Robinson <i>et al.</i> (Ref. 3)
$0.018 \pm 0.003$	$2.7 \pm 0.5$	Temmer and Heydenburg <sup>a</sup>

<sup>a</sup> G. M. Temmer and N. P. Heydenburg, Phys. Rev. **104**, 967 (1956).

shift method<sup>8</sup> and another using nuclear resonance fluorescence.<sup>9</sup> Tables I and II show the results for these measurements as well as the  $B(E2)\downarrow$  and corresponding  $E2$  partial lifetimes obtained from Coulomb-excitation measurements. A weighted average<sup>10</sup> of these values for  $\tau(E2)$  and  $\tau$  lead to  $\tau(E2) = (2.60 \pm 0.14) \times 10^{-12}$  sec,  $\tau(M1) = (6.7 \pm 0.8) \times 10^{-13}$  sec, and  $\delta^2 = 0.26 \pm 0.03$ . Of the two values of the mixing ratio  $\delta$  that were consistent with the angular distribution coefficient  $A_2$  in Fig. 3, only  $\delta = -0.52$  is consistent with this value of  $\delta^2$ .

With this choice for  $\delta$ , the values of  $\tau(E2)$  and  $\tau$  obtained from the different experiments are in good agreement. However, there still remains the unexplained discrepancy between the mixing ratios obtained from the angular distributions of gamma rays following Coulomb excitation and the value found in the present work. Elbek, Gove, and Herskind,<sup>2</sup> using oxygen ions for excitation, find  $\delta = -0.30 \pm 0.13$ , while Robinson, McGowan, and Stelson<sup>3</sup> and  $\delta = -0.22 \pm 0.06$  with excitation by alpha particles. Such low values of  $\delta$  are incompatible with the results for  $\tau(E2)$  in Coulomb-excitation experiments and the measured lifetime  $\tau$  for the 1.114-MeV state of Cu<sup>65</sup>.

The mixing ratio is of particular interest here because the presence of the  $M1$  contribution is in direct con-

TABLE II. Measured values of the total lifetime  $\tau$ .

$\tau$ ( $10^{-13}$ sec)	Method	Reference
$5.3_{-0.04}^{+0.05}$	Doppler shift	Eswaran <i>et al.</i> (Ref. 8)
$4.4 \pm 1.1$	Resonance fluorescence	This work
$6.5 \pm 1.6$	Resonance fluorescence	Kaipov <i>et al.</i> (Ref. 9)

<sup>8</sup> M. A. Eswaran, H. E. Gove, A. E. Litherland, and C. Broude (to be published).

<sup>9</sup> D. K. Kaipov, R. B. Begzhanov, A. V. Kuzimov, and Yu. K. Shubnyi, Zh. Eksperim. i Teor. Fiz. **44**, 1811 (1963) [English transl.: Soviet Phys.—JETP **17**, 1217 (1963)].

<sup>10</sup> In taking this average, uncertainties of about 15% were arbitrarily assigned to the  $B(E2)$  values which do not have errors assigned in Table 1.

TABLE III. Summary of properties of the 1.114-MeV state. Rows 7 and 8 give the ratio of the observed transition probabilities to the Weisskopf estimate<sup>a</sup> for the  $E2$  and  $M1$  transitions, respectively. ( $R = 1.2A^{1/3} \times 10^{-13}$  cm.)

$$\begin{aligned}
 B(E2)\downarrow &= (0.019 \pm 0.001)e^2 \times 10^{-48} \text{ cm}^4 \\
 \tau(E2) &= (2.60 \pm 0.14) \times 10^{-12} \text{ sec} \\
 B(M1)\downarrow &= (0.065 \pm 0.008)(e\hbar/2Mc)^2 \\
 \tau(M1) &= (6.7 \pm 0.8) \times 10^{-13} \text{ sec} \\
 \tau &= 5.3_{-0.4}^{+0.5} \times 10^{-13} \text{ sec} \\
 \Gamma &= 1.25_{-0.12}^{+0.09} \times 10^{-3} \text{ eV} \\
 T(E2)/T(E2)_w &= 12 \\
 T(M1)/T(M1)_w &= 0.034 \\
 \delta &= -0.51 \pm 0.03
 \end{aligned}$$

<sup>a</sup> D. H. Wilkinson in *Nuclear Spectroscopy*, edited by F. Ajzenberg-Selove (Academic Press Inc., New York, 1960), p. 858.

tradition to the prediction of the simple core-excitation model. This model pictures the Cu<sup>65</sup> nucleus as an even-even core with the odd proton in a  $p_{3/2}$  orbit coupled to the core. The ground state should therefore be  $\frac{3}{2}^-$  with four excited states of spin  $\frac{1}{2}^-$ ,  $\frac{3}{2}^-$ ,  $\frac{5}{2}^-$ , and  $\frac{7}{2}^-$ , all of which should decay by  $E2$  transitions to the ground state since  $M1$  transitions are forbidden. However, at the same time many of the predictions of the core-excitation model appear to be valid for odd- $A$  nuclei. Hence various modifications to the simple model are being considered to account for observed discrepancies such as the high  $M1$  admixtures in the de-excitation of states<sup>11</sup> in Cu<sup>65</sup> and Cu<sup>63</sup>.

Table III summarizes the properties under discussion for the 1.114-MeV level in Cu<sup>65</sup>. The values shown are based on weighted averages of the results from both Coulomb excitation and resonance-fluorescence experiments, except for the exclusion of the anomalously low values of  $\delta$  from the Coulomb-excitation angular-distribution measurements.

#### ACKNOWLEDGMENTS

I wish to thank Dr. L. M. Bollinger and the staff of the Argonne National Laboratory for their kind assistance and hospitality, and in particular to thank Dr. E. B. Shera for his aid in the computer analysis of the angular distribution. I am grateful to Dr. R. L. Robinson and Dr. H. E. Gove for making the results of their work on Cu<sup>63</sup> and Cu<sup>65</sup> available before publication.

<sup>11</sup> For recent discussions in which models based on single-particle coupling to an even-even core are applied to copper isotopes, see H. E. Gove, Phys. Letters **4**, 249 (1963); M. Harvey, Nucl. Phys. **48**, 578 (1963); Ref. 3; and J. B. Cumming and N. T. Porile, Phys. Rev. **122**, 1267 (1961). See also other work cited in these references.