

## Antiferromagnetism in $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ . I. Magnetic Structure\*

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The magnetic structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  has been investigated by means of single-crystal magnetic susceptibility and proton nuclear magnetic resonance (NMR) measurements. A transition to a two-sublattice antiferromagnetic structure with large uniaxial anisotropy occurs below  $17.5^\circ\text{K}$ . The measured paramagnetic susceptibilities yield  $g_{\parallel}=7.3$ ,  $g_{\perp}=2.9$ , and temperature-independent contributions  $N\alpha_{\parallel}=0.0033$ ,  $N\alpha_{\perp}=0.0129$  emu/mole. The Curie-Weiss constant is very small,  $\theta=1\pm 1^\circ\text{K}$ , giving evidence for ferromagnetic and antiferromagnetic exchange energies of equal magnitude. The zero-field proton NMR consists of a single spin-spin doublet with center frequency  $\nu_0(^1\text{H})=17.944\pm 0.003$  Mc/sec at  $T\leq 4^\circ\text{K}$ . From rotation studies of the proton NMR in weak external magnetic fields an ordered magnetic structure ( $C2/m$ ) is inferred in which ferromagnetic  $-\text{CoCl}_2-$  chains, parallel to the  $c$  axis, are coupled antiferromagnetically to adjacent chains. The  $b$  axis is the preferred direction of magnetization.

### I. INTRODUCTION

THE extensive investigations of the magnetic properties of antiferromagnetic  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  at Leiden<sup>1</sup> have stimulated much interest in the properties of other hydrated iron-group halides. Unfortunately, the structures of these halides in their stable hydration states (e.g.,  $\text{MnCl}_2 \cdot 4\text{H}_2\text{O}$ ,  $\text{FeCl}_2 \cdot 4\text{H}_2\text{O}$ ,  $\text{CoCl}_2 \cdot 6\text{H}_2\text{O}$ ,  $\text{NiCl}_2 \cdot 6\text{H}_2\text{O}$ , etc.) are fairly complex in contrast to the simple orthorhombic ( $Pbmn$ ) crystal structure of  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ .<sup>2</sup> For this reason unambiguous interpretations of the experimental observations have often been impossible. By crystallizing the appropriate halides from aqueous solution at slightly elevated temperatures, however, one can obtain a series of crystalline compounds of the type  $MX_2 \cdot 2\text{H}_2\text{O}$ , where  $M \equiv \text{Mn}$ ,  $\text{Fe}$ ,  $\text{Co}$ ,  $\text{Ni}$ , and  $X \equiv \text{Cl}$ ,  $\text{Br}$ . These compounds are closely related structurally<sup>3,4</sup> to  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ . We have examined the powder susceptibilities of these compounds for evidence of magnetic ordering and have found that the  $\text{Fe}$ ,  $\text{Co}$ , and  $\text{Ni}$  salts undergo transitions to magnetically ordered states at temperatures above  $15^\circ\text{K}$ . (The corresponding manganese salts have anomalously low-transition temperatures,  $\sim 2^\circ\text{K}$ , similar to  $\text{MnCl}_2$  and  $\text{MnCl}_2 \cdot 4\text{H}_2\text{O}$ .<sup>5</sup>) Because of the large exchange energies which can be inferred from these measurements (in contrast to the situation in most other hydrated iron-group salts), and because of the simplicity of the corresponding crystal structures, a study of the magnetic properties of these compounds promises to be quite rewarding.

The present paper is concerned with an investigation of the magnetic structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  by single-crystal magnetic susceptibility and proton nuclear

TABLE I. Room-temperature lattice parameters and atomic coordinates of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ .

$C2/m: a_0=7.256 \text{ \AA}, b_0=8.575 \text{ \AA}, c_0=3.554 \text{ \AA}; \beta=97^\circ 33'$			
Position	$a$	$b$	$c$
Co	0	0	0
Cl	0.2373	0	0.5582
O	0	0.2378	0
H	0.06	0.30	0.16

magnetic resonance (NMR) measurements. The crystal structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  is reviewed in Sec. II; the details of our experimental techniques are given in Sec. III. In Sec. IV, the results of our magnetic susceptibility measurements are given. Section V is concerned with our proton NMR measurements and the magnetic structure which can be inferred from them. In Sec. VI, we compare our results with previous measurements on  $\text{CoCl}_2$  and  $\text{CoCl}_2 \cdot 6\text{H}_2\text{O}$ .

### II. CRYSTAL STRUCTURE

The structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  was first deduced by Vainshtein<sup>6</sup> using electron diffraction techniques. Recently, Morosin and Graeber<sup>3</sup> refined the structure by x-ray diffraction techniques. The room-temperature lattice constants and atomic coordinates are given in Table I. The structure has monoclinic symmetry (space group  $C2/m$ ) and is made up of polymeric  $-\text{CoCl}_2-$  chains parallel to the  $c$  axis which are held together by relatively weak hydrogen bonds.

In Fig. 1, the nearly symmetric chlorine bridging in the  $-\text{CoCl}_2-$  chains is compared with the highly asymmetric bridging found in  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ . The  $\text{Co}^{2+}$  ions are surrounded by a nearly perfect square planar arrangement of  $\text{Cl}^-$  ions in (010) planes; the nearest-neighbor octahedron is completed by the hydrate oxygens. The crystal-field symmetry at the cobalt sites is therefore nearly tetragonal; furthermore, the principal axis of the crystal field coincides with the twofold crystallographic symmetry axis ( $b$  axis). The analysis

\* This work was supported by the U. S. Atomic Energy Commission. Reproduction in whole or in part is permitted for any purpose of the U. S. Government.

<sup>1</sup> C. J. Gorter, Rev. Mod. Phys. **25**, 332 (1953); this paper is a review of the important references.

<sup>2</sup> D. Harker, Z. Krist. **93**, 136 (1936).

<sup>3</sup> B. Morosin and E. J. Graeber, Acta Cryst. **16**, 1176 (1963).

<sup>4</sup> B. Morosin and E. J. Graeber (to be published).

<sup>5</sup> R. B. Murray, Phys. Rev. **100**, 1071 (1955); H. M. Gijssman, N. J. Poulsen, and J. Van Den Handel, Physica **25**, 954 (1959).

<sup>6</sup> B. K. Vainshtein, Dokl. Akad. Nauk. SSSR **68**, 301 (1949).

of the magnetic properties of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  is further simplified by the fact that the two cobalt sites in the unit cell are related by the lattice centering and hence are equivalent.

The packing of the  $-\text{CoCl}_2-$  chains is illustrated in Fig. 2. The slight monoclinic distortion of the structure is evidently caused by the hydrogen bonding. The bonding between the chains is quite weak as evidenced by the pronounced cleavage of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  crystals in any plane parallel to the  $c$  axis.

The dihydrated chlorides and bromides of Mn, Fe, and Co form an isomorphous series.<sup>4</sup> The corresponding nickel salts are very similar but differ slightly in the packing of the chains.<sup>4</sup>

### III. EXPERIMENTAL PROCEDURES

The starting materials for sample preparation consisted of  $\text{CoCl}_2 \cdot 6\text{H}_2\text{O}$  (commercial reagent grade, Ni low) and  $\text{CoCl}_2$  obtained by chlorinating Co metal (Johnson Matthey). No measurable differences were observed in the properties of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  crystals prepared from the two different sources.

Single crystals of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  were prepared by slow evaporation at  $70^\circ\text{C}$  of a saturated aqueous solution whose temperature was kept constant within  $\pm 0.05^\circ\text{C}$  by a thermostated oil bath. The very high solubility of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  at  $70^\circ\text{C}$  necessitated great care in sealing the evaporation chambers in order to maintain slow, uniform evaporation rates. The crystals have a pronounced  $[001]$  preferred growth habit and usually exhibit well developed (110) type faces. We were able to obtain single crystals (free of macroscopic defects) as large as  $1 \times 1 \times 5$  cm by the evaporation technique. Although the stable hydrate at room temperature is the hexahydrate, the dihydrated crystals are not very hygroscopic; a thin coating of oil was the only protection from atmospheric moisture which was needed. Single-crystal specimens used in the present study were oriented by x-ray diffraction techniques within an accuracy of  $1^\circ$ .

Magnetic susceptibility measurements were made by the mutual inductance method. The mutual inductor consisted of a multiturn primary wound coaxially on an astatic secondary winding. The coils were immersed in a pumped ( $1.2^\circ\text{K}$ ) liquid-helium bath, and were mounted on the outside of an unsilvered, vacuum-jacketed glass Dewar which contained the sample as-

FIG. 1. Comparison of the polymeric  $-\text{MCl}_2-$  chains in the crystal structures of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  and  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ .

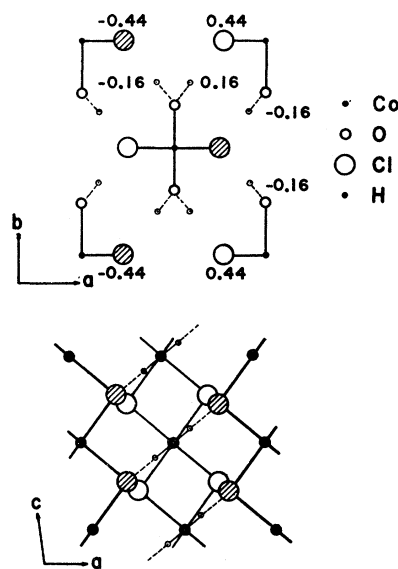
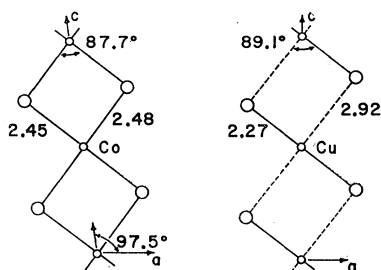


FIG. 2. Crystal structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ . Top: Projection along the  $c$  axis. Bottom: Projection along the  $b$  axis.

sembly. The sample was provided with a thin phenolic thermal radiation shield and made good thermal contact through several thin copper wires with the thermometer and heater (which were kept a few centimeters above the mutual inductor). The sample assembly could be pulled out of the coil and all measurements were based on differences in the observed mutual inductances with the sample in and out of one of the secondary windings. Inductance measurements were made with a Cryotronics Model ML155B mutual inductance bridge at a frequency of 155 cps. The apparatus was calibrated against the magnetic susceptibility of  $\text{Fe}(\text{NH}_4)_2(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$ .<sup>7</sup>

The proton magnetic resonances were observed with the frequency swept FM marginal oscillator shown in Fig. 3, followed by a conventional synchronous detector operating at 400 cps. By using shunt coils outside the cryostat, the oscillator could be made to cover the range 10–60 Mc/sec with a single sample coil. This was made possible by the feedback arrangement employed in our design which permits oscillations to be sustained even when the tank  $L/C$  ratio is very small. At  $4^\circ\text{K}$ , the samples were immersed directly in liquid helium; higher temperatures were obtained in a vacuum-jacketed heat-leak chamber which was provided with a heater.

Temperature measurements above  $25^\circ\text{K}$  were made with a copper-constantan thermocouple; below  $25^\circ\text{K}$ , a calibrated germanium resistance thermometer was used.

### IV. MAGNETIC SUSCEPTIBILITY

The magnetic susceptibilities of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  were measured along the  $a^*$ ,  $b$ , and  $c$  axes, and the results

<sup>7</sup> G. A. Candela and R. E. Mundy, Rev. Sci. Instr. 32, 1056 (1961).

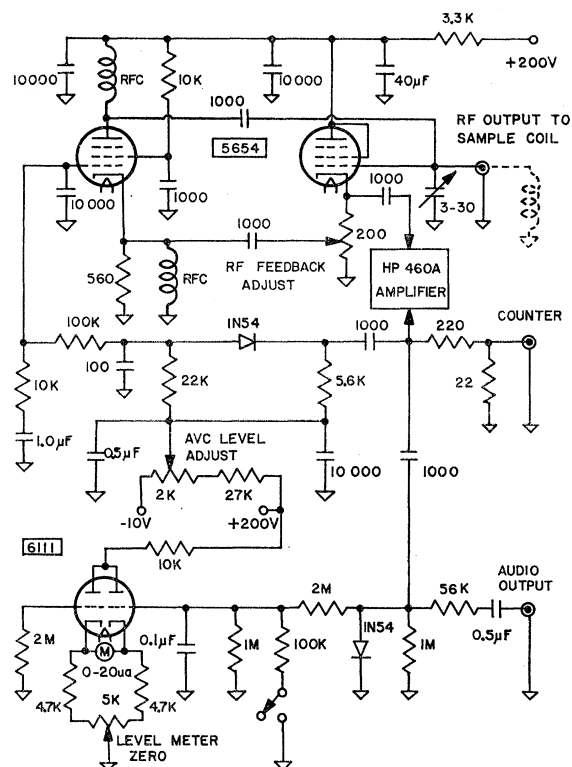


FIG. 3. Schematic of marginal oscillator. Frequency modulation is accomplished by vibrating capacitor or voltage-variable capacitor.

are summarized in Fig. 4. The experimental values confirm the uniaxial character of the magnetic anisotropy expected on the basis of the tetragonal symmetry of the  $\text{Co}^{2+}$  environment. The measurements show that  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  becomes antiferromagnetically ordered below  $\sim 17.5^\circ\text{K}$ , with sublattice magnetizations directed parallel to the  $b$  axis.

The theory of the  $g$  values and magnetic susceptibilities of  $\text{Co}^{2+}$  in magnetically dilute crystals has been given in detail by Abragam and Pryce,<sup>8</sup> and by Kambe *et al.*<sup>9</sup> The  $(3d)^7$  configuration of  $\text{Co}^{2+}$  gives rise to two triplet states and a single state in the lowest  $^4F$  ( $L=3$ ,  $S=3/2$ ) term in an octahedral crystal field. The ground orbital triplet splits into six Kramers doublets under the combined action of spin-orbit coupling and tetragonal distortion of the crystal field. In  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  the tetragonal component is quite large and the separation of the two lowest doublets is probably several hundred wave numbers. Since our measurements were restricted to temperatures below  $150^\circ\text{K}$ , the magnetic susceptibilities should be characteristic of a twofold degenerate ground state which is separated by more than  $kT$  from higher lying states. Furthermore, an inspection of our

$\chi_b^{-1}$  data in the paramagnetic range of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  indicates that exchange effects make a very small contribution to the observed paramagnetic susceptibilities. Consequently, the susceptibilities should follow the relation<sup>10</sup>

$$\chi_i = [Ng_i^2 \mu_B^2 S(S+1)/3kT] + N\alpha_i, \quad (1)$$

where  $\chi_i$  is the  $i$ th principal component of the susceptibility tensor,  $g_i$  is the effective  $g$  value,  $\mu_B$  is the Bohr magneton,  $S=1/2$  is the effective spin of the ground-state doublet, and  $\alpha_i$  is the temperature-independent contribution arising from high-frequency elements of the paramagnetic moment and from small diamagnetic effects. In the range  $25$ – $100^\circ\text{K}$  our data follow Eq. (1) within our experimental error. The extrapolated intercepts of  $\chi_i$  versus  $T^{-1}$  plots yield

$$N\alpha_{11} \equiv N\alpha_b = 0.0033 \text{ emu/mole},$$

$$N\alpha_{12} \equiv N\alpha_c = 0.0129 \text{ emu/mole},$$

and the slopes

$$g_{11} \equiv g_b = 7.3,$$

$$g_{12} \equiv g_c = 2.9.$$

The extrapolated temperature intercepts of  $(\chi_i - N\alpha_i)^{-1}$  versus  $T$  in both cases occur at  $T = 1 \pm 1^\circ\text{K}$ , which confirms that the Curie-Weiss constant  $\theta$  is much smaller than the Néel temperature  $T_N$ , and hence justifies our use of Eq. (1). Our results for  $\chi_{a^*}$  are less accurate than those for  $\chi_b$ ,  $\chi_c$  because of the small size of the crystal used in the  $a^*$  measurements; however, within our experimental uncertainty the values obtained for  $\alpha_{a^*}$  and  $g_{a^*}$  agree with the corresponding  $c$ -axis values.

A detailed analysis of our measured susceptibilities and  $g$  values is not possible at this time because of the lack of sufficient information (such as optical absorption data) for determining the various crystal-field parameters. It is noteworthy, however, that our observations are quite consistent with susceptibilities calculated by Kambe *et al.*<sup>9</sup> within the lowest orbital triplet of  $\text{Co}^{2+}$  if

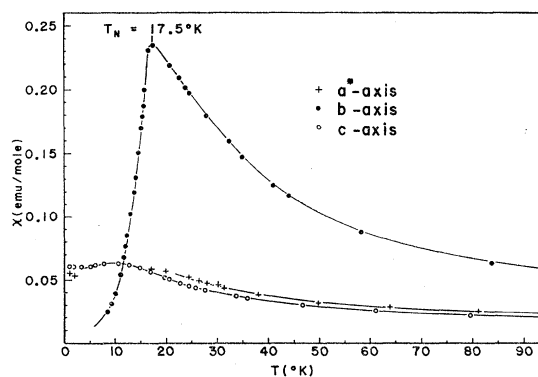


FIG. 4. Plot of single-crystal molar magnetic susceptibilities of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  as a function of temperature.

<sup>8</sup> A. Abragam and M. H. L. Pryce, Proc. Roy. Soc. (London) A206, 173 (1951).

<sup>9</sup> K. Kambe, S. Koide, and T. Usui, J. Phys. Soc. Japan 7, 15 (1952).

<sup>10</sup> J. H. Van Vleck, *The Theory of Electric and Magnetic Susceptibilities* (Oxford University Press, New York, 1932), p. 181 ff.

we take  $\eta \approx 4\delta/3\lambda \approx +5$ , where  $\delta$  is the tetragonal distortion parameter (i.e., the separation between the lowest levels in the absence of spin-orbit coupling) and  $\lambda \approx -180 \text{ cm}^{-1}$  is the spin-orbit coupling constant.

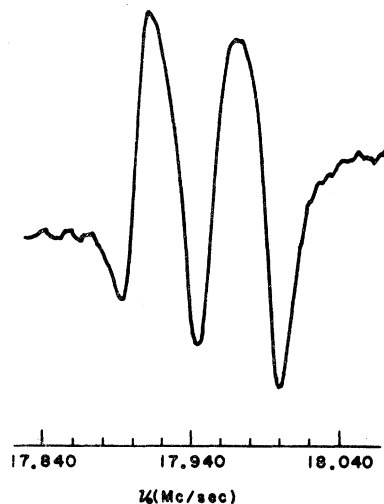
The small value of  $\theta$  shows that the antiferromagnetic exchange forces acting on the  $\text{Co}^{2+}$  spins are compensated by ferromagnetic forces of essentially equal magnitude. Thus, ferromagnetic interactions must play an important role in determining the magnetic properties of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  despite its antiferromagnetic structure.

### V. PROTON NUCLEAR MAGNETIC RESONANCE

The proton NMR in the paramagnetic state was observed in the liquid-hydrogen range; the onset of magnetic ordering was detected at  $17.5 \pm 0.1^\circ\text{K}$  by the disappearance of the resonance on cooling through the transition.

A search for the zero-field proton NMR in the ordered state of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  yielded a single resonance.<sup>11</sup> The observed resonance, shown in Fig. 5, is a doublet with separation  $\Delta\nu \approx 50 \text{ kc/sec}$ , presumably due to dipolar spin-spin interactions between the two protons of the water molecule. (In the following discussion of the proton spectra all frequencies refer to the central frequency of the doublet.) The zero-field frequency, extrapolated to  $T=0^\circ\text{K}$ , is  $\nu_0(^1\text{H}) = 17.944 \pm 0.003 \text{ Mc/sec}$  corresponding to an internal field  $H_I$  at every proton site (due to the ordered  $\text{Co}^{2+}$  spins) of 4.214 kOe. Below  $4^\circ\text{K}$  the zero-field resonance exhibits a negligible temperature dependence; between 4 and  $16^\circ\text{K}$ , the observed frequencies accurately follow a  $(\nu_0 - \nu) \propto T^{6.5}$  relation with an extrapolated zero-frequency temperature of  $19.8^\circ\text{K}$ . This behavior of the sublattice magnetization provides evidence for a large gap in the spin-wave spectrum and is qualitatively consistent with the large magnetic anisotropy inferred from the measured  $g$  values.

FIG. 5. Second derivative absorption spectrum of zero-field proton resonance in  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  at  $4^\circ\text{K}$ .



<sup>11</sup> A. Narath, B. Morosin, and A. T. Fromhold, Jr., Bull. Am. Phys. Soc. 8, 359 (1963).

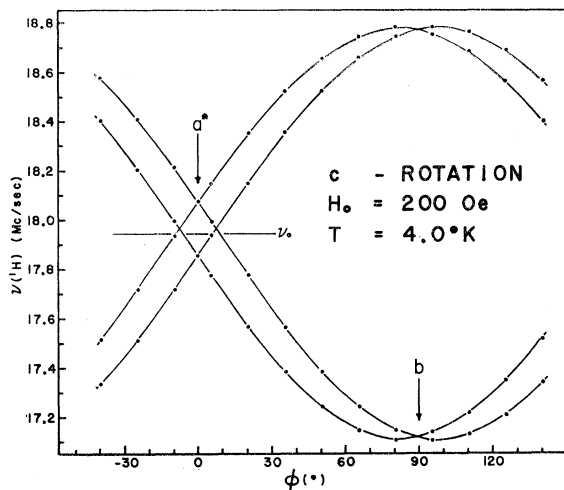


FIG. 6. Proton resonance diagram for rotation of  $H_0 = 200 \text{ Oe}$  in  $a^*b$  plane at  $4.0^\circ\text{K}$ .

The eight protons in the chemical unit cell are all related by symmetry operations. (The two hydrogen atoms of each water molecule are related by the twofold axis, the two water molecules associated with a given cobalt ion are related by reflection symmetry, and the lattice centering operation provides the remaining equivalence.) The crystallographic equivalence of all proton positions, together with the existence of only a single internal field, require that the magnetic point group be identical to the crystallographic point group, except for the possible replacement of ordinary symmetry operations by antioperations. Hence, the  $\text{Co}^{2+}$  moments lie either along the  $b$  axis or in the  $ac$  plane. The magnetic susceptibility measurements, however, show unequivocally that the  $b$  axis is the preferred spin direction. We can conclude, therefore, that no appreciable canting occurs in the magnetic structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ .

In order to determine the most probable spin arrangement, it is necessary to determine the direction of the internal field at the proton sites. This can be accomplished easily by observing the behavior of the nuclear resonance in weak external magnetic fields.<sup>12</sup> Since the spin direction has already been determined, it is only necessary to determine the absolute magnitudes of the internal-field components; hence, only a single field rotation is required.

If we assume that the directions of sublattice magnetization are unaffected by the external field, the resonance condition is

$$\omega/\gamma = H_T \equiv |(\mathbf{H}_0 + \mathbf{H}_I)|, \quad (2)$$

where  $\mathbf{H}_0$  is the external field and  $\mathbf{H}_I$  is the internal field. In our experiments  $\mathbf{H}_0$  was rotated in a plane normal to the  $c$  axis. We take  $\phi$  to be the angle between  $\mathbf{H}_0$  and

<sup>12</sup> N. J. Poulis and G. E. C. Hardeman, Physica 18, 201 (1952).

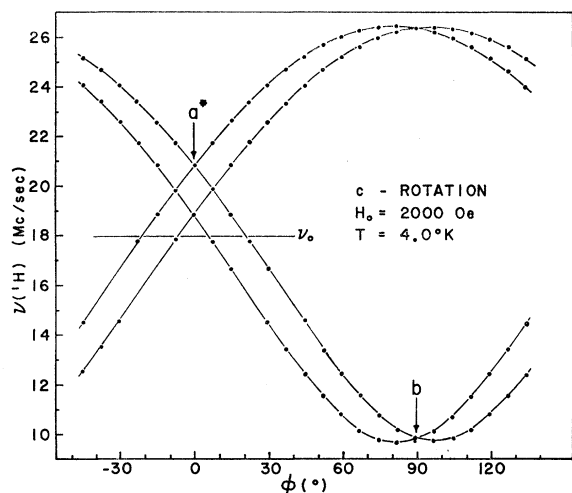


FIG. 7. Proton resonance diagram for rotation of  $H_0 = 2000$  Oe in  $a^*b$  plane at  $4.0^\circ\text{K}$ .

the  $a^*$  axis, and choose a coordinate system in which the  $a^*$ ,  $b$ , and  $c$  crystallographic axes lie along the  $x$ ,  $y$ ,  $z$  directions, respectively. The components of the net field are

$$H_T^x = H_0 \cos\phi + H_I^x,$$

$$H_T^y = H_0 \sin\phi + H_I^y,$$

$$H_T^z = H_I^z,$$

and the resonance condition becomes

$$\omega/\gamma = [H_0^2 + H_I^2 + 2H_0H_I^{xy}]^{1/2}, \quad (3)$$

where

$$H_I^{xy} = H_I^x \cos\phi + H_I^y \sin\phi. \quad (4)$$

Since  $H_I$  is unusually large in  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ , our rotation studies were carried out with  $H_0 < H_I$ . Using this condition, the qualitative behavior of the resonance patterns can be obtained by expanding Eq. (3) in powers of  $H_0/H_I$ . The leading terms are given by

$$\frac{\omega}{\gamma} = H_I \left\{ 1 + \frac{H_0^2}{2H_I^2} + H_I^{xy} \left[ \frac{H_0}{H_I^2} - \frac{H_0^3}{2H_I^4} \right] - (H_I^{xy})^2 \frac{H_0^2}{2H_I^4} + \dots \right\}. \quad (5)$$

Since  $H_I^{xy}$ , the internal-field component in the direction of  $H_0$ , varies sinusoidally with  $\phi$ , the resonance patterns are expected to be sinusoidal for sufficiently small values of  $H_0/H_I$ . The observed  $4.0^\circ\text{K}$  rotation patterns, shown in Fig. 6 for  $H_0 = 200$  and in Fig. 7 for  $H_0 = 2000$  Oe, follow these predictions and can be made to fit Eq. (3) exactly by a suitable choice of internal field parameters.

The observed rotation patterns have the  $2\pi$  periodicity required of an antiferromagnetic structure, and are symmetric about the  $a^*$  and  $b$  axes. Only four distinct resonances are observed for a general orientation of the external field; the rotation patterns of the four signals

TABLE II. Comparison of calculated and observed proton local fields in antiferromagnetic  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ , for spin ordering parallel to the  $b$  axis.

Space group	Spin structure		Dipole field at $^1\text{H}$ position (kOe)		
	$J_L$	$J_T$	$H_I^x$	$H_I^y$	$H_I^z$
$Ic2/m$	—	—	0.56	2.84	1.45
$Cc2/m$	—	+	1.28	2.91	0.62
$Pc2/m$	+	—	0.43	4.12	0.53
Observed			0.546	4.134	0.607

are identical in shape and differ only in position along the  $\phi$  axis. The two positions of maximum  $H_I^{xy}$  occur at  $\phi(\text{max}) = (82.5, 97.5) \pm 0.1^\circ$ . The magnitude of  $H_I^{xy}(\text{max})$  was calculated from the measured frequency at  $\phi(\text{max})$ , using the exact relation

$$H_I^{xy}(\text{max}) = (H_T^2 - H_I^2 - H_0^2)/2H_0, \quad (6)$$

for values of  $H_0$  ranging from 0.2–10 kOe. The average of our measurements gives

$$H_I^{xy}(\text{max}) = 4.170 \pm 0.010 \text{ kOe}.$$

The values of  $H_I^x$ ,  $H_I^y$ , and  $H_I^z$  follow immediately from  $H_I$ ,  $H_I^{xy}(\text{max})$ , and  $\phi(\text{max})$ , and are given in the last line of Table II.

The internal field at the proton sites is the result of dipolar interactions with the  $\text{Co}^{2+}$  moments. The dipole fields can be calculated from

$$H_I^i = \sum_j B^{ij}, \quad (7)$$

$$B^{ij} = \int_0^\infty \left( \frac{3x^i x^j - \delta_{ij} r^2}{r^5} \right) \mu_j(\mathbf{r}) d\tau, \quad (8)$$

where  $H_I^i$  is the  $i$ th component of the dipole field and  $x^i$ ,  $x^j = x, y, z$  are the components of the vector  $\mathbf{r}$  which connects a given proton site to the volume element  $d\tau$  having magnetic moment components  $\mu_j(\mathbf{r})$ . If we assume that the moment distribution around the  $\text{Co}^{2+}$  ions is spherical, the integral in Eq. (8) can be replaced by a sum over point dipoles. From a consideration of possible superexchange paths in  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ , it follows that the most important exchange interactions should be the intrachain ( $J_L$ ) coupling along the  $c$  axis and the nearest-neighbor interchain ( $J_T$ ) coupling. We have computed the appropriate lattice dipole sums for the three magnetic structures shown in Fig. 8 which are consistent with the above arguments. The computations were carried out by direct summations over a sufficient number of lattice points within a spherical volume to assure an accuracy of  $\pm 0.1\%$  in the calculated values.<sup>13</sup> The magnetic moment used in the calculation was  $\mu_y(\text{Co}^{2+}) = 3.65 \mu_B$  as determined from our susceptibility measurements. Since the limits of error in the x-ray determination of the hydrogen positions are quite

<sup>13</sup> B. Morosin and A. Narath, J. Chem. Phys. 40, 1958 (1964).

large, the geometry of the water molecule was adjusted to conform more closely to that found in other hydrated salts.<sup>14</sup> We chose  $\text{O-H}=0.97 \text{ \AA}$  and  $\angle\text{H-O-H}=108^\circ$ , instead of the x-ray values of  $0.85 \text{ \AA}$  and  $102^\circ$ , respectively. The hydrogen atoms were placed in the nearest-neighbor  $\text{Cl-O-Cl}$  plane as determined by the x-ray measurements. The components of  $\mathbf{H}_I$  calculated in this way are compared in Table II with the experimental values. The agreement for a structure consisting of ferromagnetic chains with antiferromagnetic interchain couplings is seen to be quite good; the agreement for the two other structures, on the other hand, is very poor. We have examined the sensitivity of the fit to possible distortions in the moment distribution by calculating the contribution to  $\mathbf{H}_I$  arising from any magnetic moment centered on the  $\text{Cl}^-$  ions. It was found that a 10% delocalization of the moment in the  $Pc2/m$  structure reduces the calculated values of  $H_I^x$ ,  $H_I^y$ , and  $H_I^z$  by 45, 9, and 30%, respectively. However, the conclusion that only the  $Pc2/m$  structure is capable of explaining both the magnitude of  $\mathbf{H}_I$  and its small angular deviation from the  $b$  axis is not changed.

## VI. DISCUSSION

Our value of  $T_N=17.5^\circ\text{K}$  agrees well with that determined recently by Shinoda *et al.*<sup>15</sup> from their observation of a  $\lambda$ -type specific heat anomaly at  $17.20^\circ\text{K}$ . This transition temperature is unusually high for a hydrated salt and results from the efficient packing which is inherent in the crystal structure of the dihydrated iron-group chlorides and bromides.

The intrachain exchange coupling proceeds through symmetric,  $\sim 90^\circ$   $\text{Co-Cl-Co}$  bridges. This linkage is identical to that responsible for the intralayer coupling in  $\text{CoCl}_2$  ( $T_N=25^\circ\text{K}$ <sup>16</sup>); in both cases this interaction is ferromagnetic. The antiferromagnetic nearest-neighbor interchain coupling in  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  involves a  $\text{Co-Cl-Cl-Co}$  linkage ( $\text{Cl-Cl}=4.28 \text{ \AA}$ ) similar to that responsible for the antiferromagnetic interlayer coupling in  $\text{CoCl}_2$ . In the case of  $\text{CoCl}_2$ , the ratio of the intralayer to interlayer exchange constants is  $\sim 13$ .<sup>16</sup> The small Curie-Weiss constant of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  can be understood by considering the relative number of neighbors which are coupled by the various interactions: The ferromagnetic interaction  $J_L$  couples each  $\text{Co}^{2+}$  spin to only two  $\text{Co}^{2+}$  neighbors; the antiferromagnetic interaction  $J_T$ , on the other hand, connects to twelve neighbors. Furthermore, it is likely that a third interaction  $J_{T'}$ , involving  $\text{Co-Cl-Cl-Co}$  ( $\text{Cl-Cl}=3.81 \text{ \AA}$ ) exchange paths along the  $a$  axis is important. The interaction couples to six neighbors, and is probably also

<sup>14</sup> S. W. Peterson and H. A. Levy, *J. Chem. Phys.* **26**, 220 (1957).

<sup>15</sup> T. Shinoda, H. Chihara, and S. Seki (to be published).

<sup>16</sup> M. E. Lines, *Phys. Rev.* **131**, 546 (1963); this work contains many of the earlier references.

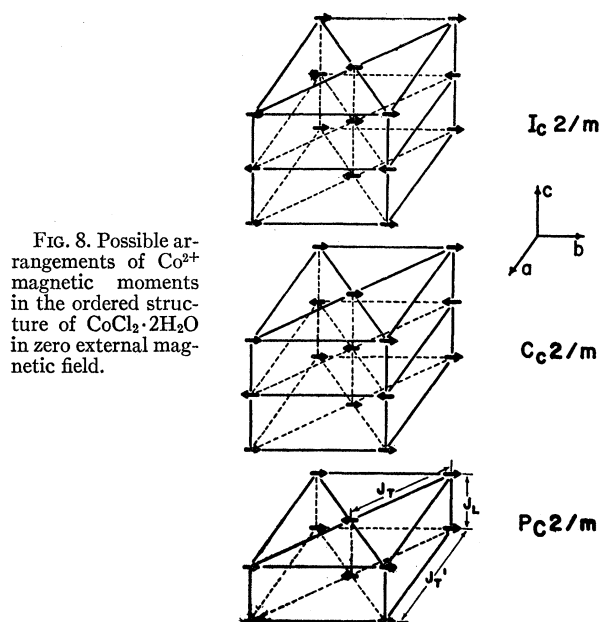


FIG. 8. Possible arrangements of  $\text{Co}^{2+}$  magnetic moments in the ordered structure of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$  in zero external magnetic field.

antiferromagnetic. Thus, although the antiferromagnetic interactions are presumably much weaker than the ferromagnetic intrachain interaction, the fact that the former involve a much greater number of neighbors accounts for the small value of  $\theta$ .

In the case of  $\text{CoCl}_2 \cdot 6\text{H}_2\text{O}$ , the ferromagnetic coupling  $J_L$  is entirely absent. The strongest coupling is antiferromagnetic and involves  $\text{Co-Cl-Cl-Co}$  bridges ( $\text{Cl-Cl}=4.07 \text{ \AA}$ )<sup>17</sup>; the ordering temperature is consequently quite low ( $T_N=2.29^\circ\text{K}$ ).<sup>18</sup>

That  $J_{T'}$  is not negligibly small is suggested by the observation of two discontinuities in the high-field magnetization ( $H_0 \parallel b$ ) behavior of  $\text{CoCl}_2 \cdot 2\text{H}_2\text{O}$ .<sup>19</sup> Since  $J_{T'}$  couples *ferromagnetic* neighbors in the zero-field structure, it is possible that the first discontinuity involves a transition to a triangular spin arrangement. The determination of the magnitude of the various exchange constants and their anisotropies, on the basis of low- and high-field magnetization measurements, will be the subject of a future communication.

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<sup>17</sup> J. Mizuno, *J. Phys. Soc. Japan* **15**, 1412 (1960); R. D. Spence, P. Middents, Z. El Saffar, and R. Kleinberg, *J. Appl. Phys. Suppl.* **35**, 854 (1964).

<sup>18</sup> W. K. Robinson and S. A. Friedberg, *Phys. Rev.* **117**, 402 (1960).

<sup>19</sup> A. Narath and D. C. Barham, *Bull. Am. Phys. Soc.* **9**, 112 (1964).