ISOMERISM OF C,(g) CLUSTER AND ITS MANIFESTATIONS IN THE SYSTEM THERMODYNAMICS ****

ZDENEK SLANINA

The J Heyrovskj Institute of Physlcal Chemrstry and Electrochemistry, Czechoslovak Academy of Saences, Mbchova 7, CS-121 38 Prague 2 (Czechoslovakia)

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ABSTRACT

In contrast to earlier conclusions based on simple models, the newest calculatrons showed that the C₆(g) cluster isomer of the lowest potential energy is a cyclic structure of D_{3h} symmetry The evaluation given in the present study, however, shows that increasing temperature increases the importance of the energetically higher linear structure whtch becomes the dominant component of the equilibrium gaseous mixture of isomers in the end Therefore, the D_{3h} structure alone cannot be used in simulating the $C_6(g)$ system thermodynamics, and it is necessary to apply the overall terms including the contributions of all the isomers The effects of rsomerrsm are especially noticeable with the heat capacity term whose temperature dependence shows a markedly extremal course This study fundamentally changes both the values of the quantities used so far and the approaches to the thermodynamics of this system

INTRODUCTION

The most recent study by Raghavachari et al [1] represents a substantial development to the solution of the structural problem of the $C_6(g)$ system, this problem being still best attacked by theoretical means (see, e g., refs 2 and 3), which is connected with the rather extreme conditions during observation of this system (the temperature of 2500 K in ref 4) The study of carbon clusters is undertaken (see, e.g., refs $5-8$) because of their technological applications (for references see, e g, ref 3) and, more recently, of their presumed presence and significant role m the chemlsm of interstellar space $[9-15]$ The description of the thermodynamics and composition of the equlhbnum gas phase above graphite at hgher temperatures represents an important item of information for a series of application treatments, and

^{*} Dedicated to Academician Antonin A Vlček on the occasion of his 60th birthday

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therefore it 1s desirable that the values of these data be known with the highest possible accuracy. The data predominantly used at present [16] are based on the assumption of linearity and very approximate values of molecular parameters, m particular they do not take mto account the lsomerlsm of these clusters The present paper 1s intended to fill this gap, starting from ref 1 as the source of molecular information about the $C_6(g)$ isomers

DESCRIPTION OF THE SYSTEM

The C_6 system was studied [1] in two different atomic orbital basis sets, 3-21G and $6\text{-}31\text{G}^*$, both of them giving the potential hypersurfaces with six stationary points four of these structures are local energy minima, which was shown by means of the harmomc vibrational analysis m the 3-21G basis Table 1 presents a survey of these four isomers, and the description of their energetics adopts two higher approximations which go beyond the level of the approxlmatlons used for evaluation of molecular geometry [l] In particular, ths means mvolvement of correlation effects at the level of the Møller-Plesset theory [17] within the complete fourth-order treatment (MP4) and possibly also with the estimate of higher, finer effects ("Best") In both these energy series, however, the order of isomers 1s the same, no difference being observed between application of the potential energy scale and the scale of potential energy with mcluslon of the zero-pomt vibrational motions Reference 1 denotes these four isomers with the identifying numbers 1, 2, 4 and 6 whch are also included m Table 1

In all the approaches considered, the cychc structure, lowest m energy, with the D_{3h} point group of symmetry and the A'_1 symmetry of electronic wavefunction is conventionally denoted as 4 Then there follows the linear $D_{\alpha h}$ structure with the ${}^{3}\Sigma_{\alpha}^{-}$ triplet electronic state denoted as 1 The third structure is again linear $D_{\alpha h}$, but its electronic state symmetry is ${}^{3}\Sigma_{u}^{+}$ it is

TABLE 1 Survey of relative energies a of $C_6(g)$ isomers

^a Reference 1, ΔE_i and $\Delta H_{0,i}^{\Theta}$ denote potential energy and ground-state energy, respectively, relative to the global minimum (4) , in kJ mol⁻¹

denoted as 2 Finally, the highest in energy is the cyclic structure of D_{6h} symmetry and ${}^{1}A'_{1}$ electronic state it is denoted as 6

The molecular parameters of these isomers from ref 1 serve in the present paper for construction of their partition functions in the usual approximation of rigid rotator and harmonic oscillator [18] The rotational partition function 1s constructed on the basis of the 3-21G molecular geometnes, although the molecular geometry of the 6-31G^{\star} quality is also used for comparison m some cases The calculations of thermodynanuc quantities are carried out side by side for both the energetics series of Table 1, 1 e $6-31G^{\star}/MP4$ and "Best" Finally, the thermodynamic functions of graphite are taken from ref 16

THE ISOMERISM CONTRIBUTION TO THERMODYNAMICS

In terms of the potential energy with mcluslon of zero-point vibrations for the *i*-th isomer with respect to the structure 4, $\Delta H_{0,14}^{\Theta}$, and the partition function q_i , of the *i*-th isomer, the mole fractions or weight factors w_i of these isomers are given, m our case, as follows [19,20]

$$
w_{i} = \frac{q_{i} \exp\left(-\Delta H_{0,i,4}^{\Theta}/RT\right)}{\sum_{j} q_{j} \exp\left(-\Delta H_{0,j,4}^{\Theta}/RT\right)}
$$
(1)

Sometimes, in the literature the simple Boltzmann factors w' , are given instead of these more rigorous w_i , values

$$
w'_{i} = \frac{\exp(-\Delta E_{i,4}/RT)}{\sum_{j} \exp(-\Delta E_{j,4}/RT)}
$$
(2)

They are constructed only on the basis of the relative potential energy terms $\Delta E_{,\:4}$

The existence of four different isomers justifies four different partial equlhbnum processes to be considered

$$
6C(s) = C_6(g, t) \tag{3}
$$

which are characterized by their standard molar enthalpy changes ΔH_{T}^{Θ} , entropy changes $\Delta S_{T,t}^{\Theta}$, and heat capacity changes at constant pressure $\Delta C_{p,T,i}^{\Theta}$. The technique of observation used for the study of C₆ (viz mass spectroscopy [4]) of course allows no differentiation between the individual isomers and takes them as a whole group Hence It 1s necessary to introduce the thermodynamic terms ΔH_T^{Θ} , ΔS_T^{Θ} , ΔC_{pT}^{Θ} which are called overall terms [19,20], all the isomers contribute to these values according to their weights w_r

$$
\Delta H_T^{\Theta} = \sum_{i}^{4} w_i \Delta H_{T,i}^{\Theta} \tag{4}
$$

$$
\Delta S_T^{\Theta} = \sum_{i}^{4} w_i \left(\Delta S_i^{\Theta} - R \ln w_i \right) \tag{5}
$$

$$
\Delta C_{\mathsf{p},T}^{\Theta} = \sum_{i}^{4} w_{i} \Delta C_{\mathsf{p},T,i}^{\Theta} + \frac{1}{RT^{2}} \left[\sum_{i}^{4} w_{i} \left(\Delta H_{T,i}^{\Theta} \right)^{2} - \left(\Delta H_{T}^{\Theta} \right)^{2} \right]
$$
(6)

Whereas the overall terms (4) – (6) are related to a certain chemical reaction $(1 e (3))$, it is also possible to introduce the isomerism contributions related to a reference structure, usually the most stable isomer In our case the contnbutlons are related to the structure 4 and are defined as correction terms which must be added to the partial value of thermodynamic function of the isomer 4 to obtain the respective overall term

$$
\delta_4 H_4^{\text{(iso)}} = \Delta H_T^{\Theta} - \Delta H_{T4}^{\Theta} \tag{7}
$$

$$
\delta_4 S_4^{\text{(iso)}} = \Delta S_T^{\Theta} - \Delta S_{T4}^{\Theta} \tag{8}
$$

$$
\delta_4 C_{\mathbf{p},4}^{(\text{iso})} = \Delta C_{\mathbf{p},T}^{\Theta} - \Delta C_{\mathbf{p},T,4}^{\Theta} \tag{9}
$$

These isomerism contributions are independent of the particular stoichiometry and represent thus more general, transferable terms

In the case of the heat capacity term a notice must be added In eqn (6) the temperature dependence of w , is taken into account If the observation were specially arranged to have fixed w , values even at changing temperatures, the term (6) and (9), called the relaxation term, would be reduced to the special case of the so-called isofractional term [19,20]

$$
\Delta C_{\mathbf{p},T,w}^{\Theta} = \sum_{i}^{4} w_{i} \Delta C_{\mathbf{p},T,i}^{\Theta} \tag{10}
$$

$$
\delta_4 C_{\mathsf{p},w\,4}^{(\mathrm{iso})} = \Delta C_{\mathsf{p}\,T,w}^{\,\Theta} - \Delta C_{\mathsf{p}\,T\,4}^{\,\Theta} \tag{11}
$$

For methodical reasons, both isofractional and relaxation types of quantities will be considered

RESULTS AND DISCUSSION

The behaviour of the $C_6(g)$ system is obviously determined by the interplay of the isomers 4 and 1 (Table 2) Whereas relative stability of the D_{3h} isomer decreases with temperature, that of the linear structure 1 increases until a temperature at which the stability order 1s interchanged

TABLE 2

 \vert f

Temperature dependences of weight factors a_{w} , and simple Boltzmann factors b_{w}' of $C_6(g)$ isomers in their equilibrium mixture **Temperature dependences of weight factors** α **w, and simple Boltzmann factors** β **w; of** $C_6(g)$ **isomers in their equilibrium mixture**

^a Mole fractions in isomeric equilibrium mixture, in \mathcal{G}_2 , $i = 4, 1, 2$, or 6 (for identifying numbers, see Table 1) b In parentheses **a** Mole fractions in isomenc equilibrium mixture, in \mathcal{R} , $i = 4, 1, 2$, or 6 (for identifying numbers, see Table 1) **b In parentheses**

This temperature is about 1900 and 1100 K in the cases of the isomer energetics from the approximations $6-31G^{\star}/MP4$ and "Best", respectively Above these stablhty interchange temperatures the ratio of structure 1 continues to increase until ths structure becomes dommant The molar fraction of structure 2 also increases with temperature, but it does not exceed 10% even at the highest temperatures studied The molar fraction of the last isomer, cyclic D_{6h} structure, is negligible at all the temperatures investigated In particular It can be stated that at the temperature of $observation [4]$ the most significant component of the equilibrium gas phase 1s the linear structure 1 (and not the structure 4, which could be deduced from a straightforward conslderatlon of the stability order at absolute zero)

Table 2 also shows that, except for low temperatures, the simple Boltzmann factors w' , cannot be used instead of the rigorous w, values Specially, these w' factors do not allow the interchange of relative isomer stabilities In other words this means that the rotational-vibrational motions of the mdlvldual Isomers are essential for evaluation of then populations m the equlhbnum nuxture

Table 3 gives a survey of temperature course of the isomerism contributions The isomerism contribution to the enthalpy term $\delta_4 H_4^{\text{(iso)}}$ related to the structure 4 increases with mcreasmg temperature and reaches tens of kJ mol^{-1} at higher temperatures Still more distinct values are observed with the isomerism contribution to the entropy term $\delta_4S_4^{(iso)}$ In the TS scale it makes about 150 kJ mol⁻¹ at 3000 K From this it is clear that a simulation of the $C_6(g)$ thermodynamics by means of the partial terms belonging to the ground state structure (1 e 4) would lead to tremendous errors

Whereas the isofractional contribution of isomerism to heat capacity $\delta_4C_{\text{p},w4}^{(\text{iso})}$ increases with increasing temperature, the relaxational contribution exhibits a marked maximum In the isomer energetics approximated by $6-31G^{\star}$ /MP4 this maximum appears at 1750 K and attains the value of 84 J K^{-1} mol⁻¹, whereas in the approximation denoted as "Best" the respective maximum comes sooner, at about 1000 K, and is about 79 J K^{-1} mol^{-1} These maxima are due to the temperature dependence of w , and are so distinct that they could serve as experimental means for revealing the isomerism of a reaction component

Table 3 also enables evaluation of the effect of mterchange of molecular geometry of isomers, 1 e on going from 3-21G to 6-31G^{*} structures All the four quantities studied are less sensitive to ths Interchange, the changes being below 1 kJ mol⁻¹ or 1 J K⁻¹ mol⁻¹

Beside the full four-membered set we can also consider sets with a smaller number of members, e g, the triad $4,1,2$ or the pair $4,1$ Thereby we admit a variable dimension of the isomeric set n , and thus we work with the isomerism contributions $\delta_n X_4^{(iso)}$ instead of the $\delta_4 X_4^{(iso)}$ terms considered so far Thus it is possible to study the convergency properties of the $\delta_n X_4^{\text{iso}}$ quantities as functions of the number n of the set members (Table 4) In

TABLE 3

^a Related to the global minimum, 4, see Table 1, *H* terms in kJ mol⁻¹, S and C_p m J K⁻¹ mol⁻¹ In the upper and lower (1 e in parentheses) The metallist of the fact that the manufactures of iom
E ^a Related to the global minimum, 4, see Table 1, *H* terms in kJ mol⁻¹, S and C_p in J K⁻
hnes, data are given based on 3-21G and 6-31G^{*} structural parameters [1], respectively
^b Isofractional $\delta_4 C_p^{(u_0)}$, a lines, data are given based on $3-21G$ and $6-31G^*$ structural parameters [1], respectivel

B Isofractional $\delta_4 C_5^{\text{USO}}$, and relaxation $\delta_4 C_5^{\text{USO}}$ terms

' See Table 1

TABLE 4

Convergency properties of isomerism contributions ^a $\delta_n H_4^{(iso)}$, $\delta_n S_4^{(iso)}$, and $\delta_n C_{p,4}^{(iso)}$ with increasing number n of isomeric set members $\frac{b}{b}$

^a See Table 3 for a specification

^b Isomeric sets $n = 2, 4, 1, n = 3, 4, 1, 2, n = 4, 4, 1, 2, 6$ (for identifying numbers 4, 1, 2, 6, see Table 1)

accordance with neghgble populations of the structure 6, the differences between $n = 3$ and $n = 4$ are also negligible However, the role of the linear structure 2 is already perceptible, the greatest differences being observed in

TABLE 5 Standard molar terms ^a for partial and overall ^b reactions $6C(s) = C_6(g)$

^a Standard states ideal gas and solid at 1 atm = 101325 Pa pressure, *H* terms in kJ mol⁻¹. S and C_p in J K⁻¹ mol⁻¹ Derived for the best estimation [1] of the heat of formation at 0 K of the structure $4^c \Delta H_{0.4}^{\Theta} = 1177.14 \text{ kJ mol}^{-1}$

^b The relaxation term is given with the overall ΔC_{pT}^{Θ}

^d For the sake of extremal behaviour visualization, cf $\Delta C_{\text{p}}^{\Theta}$ = -146 J K⁻¹ mol⁻¹

 $\frac{1}{2}$ For identifying numbers 1, 2, 4, 6, see Table 1

the relaxational contribution to heat capacity. This is especially distinct in the "Best" approxlmatlon, because at the end of the interval studied the structure 2 becomes even more significant than the structure 4 (cf Table 2)

Of course, the terms from Tables 2-4 are applicable to any reaction with participation of $C_6(g)$ Nevertheless, especially important are the equilibria over graphte (3), Table 5 gives a survey of their partial and overall standard molar changes of enthalpy, entropy, and heat capacity at constant pressure It is noteworthy that the extremal temperature course of the $\delta_4 C_{p4}^{(180)}$ term is retained also with the overall relaxational reaction terms ΔC_{pT}^{\bullet} of the reactions (3)

CONCLUDING REMARKS

It has been shown that, although the cyclic D_{3h} isomer represents the ground state structure in the $C_6(g)$ system, the linear structure with triplet electronic state becomes the most populated or even predominant isomer at the temperatures relevant for observation This interplay of lsomenc structures markedly affects the values of overall thermodynamic terms and necessitates a careful regard for the isomerism contributions These conclusions obviously will not be restricted only to the particular $C_6(g)$ system, but the isomerism will apparently play a substantial part also in the case of other carbon clusters (and not necessarily only the hgher ones) These qualitative conclusions will most probably not depend on the use of the rigid rotator and harmonic oscillator approximation to partition functions So far $C₃$ is the largest carbon aggregate for which a more sophisticated description of thermodynamics is available [21,22], while for higher clusters one could guess their deviations from the simple model from spectral data on polyacetylenes and cyanopolyyenes [23,24]

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