A STUDY OF THE FORMATION OF LINBO3 IN THE SYSTEM Li2CO3-Nb2O5

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ABSTRACT

The formation process of LiNbO₃ in the system Li₂CO₃-Nb₂O₅ was discussed from the results of non-isothermal or isothermal TG experiments and X-ray analysis. The mixture Li₂CO₃ and Nb₂O₅ in mole ratios of 1:3, 1:1 or 3:1 was heated at a rate of 5°C min⁻¹ or at various temperatures fixed in the range 475 to 677°C. If the system has a composition of Li₂CO₃ + 3Nb₂O₅ or 3Li₂CO₃ + Nb₂O₅, the reaction between Li₂CO₃ and Nb₂O₅ proceeds with CO₂ evolution to form LiNbO₃ at ca. 300-600°C, but Nb₂O₅ or Li₂CO₃ remains unreacted. A composition of Li₂CO₃ + Nb₂O₅ gives LiNbO₃ at 300-700°C. The diffusion of Li₂O through the layer of LiNbO₃ is rate-controlling with an activation energy of 51 kcal mol⁻¹. The reaction between LiNbO₃ and Nb₂O₅ gives LiNb₃O₈ at 600-700°C. At 700-800°C, a slight formation of Li₃NbO₄ occurs by the reaction between LiNbO₃ and Li₂O at the outer surface of LiNbO₃ and the Li₂O component of Li₃NbO₄ diffuses toward the boundary of the LiNb₃O₈ layer through the LiNbO₃ layer. The single phase of LiNbO₃ is formed above 850°C.

INTRODUCTION

Lithium niobate (LiNbO₃) is a ferroelectric material having a high Curie point. Single crystals of LiNbO₃ are of importance as electro-optic materials¹. Sintered ceramics of LiNbO₃ are of great interest because they have many applications in the field of dielectrics. LiNbO₃ is formed by the solid-state reaction between Li₂CO₃ and Nb₂O₅. The preparation of reactive powder of LiNbO₃ with homogeneous composition is important to obtain its dense sintered ceramics. Therefore, it is necessary to study the formation of LiNbO₃ by the reaction between Li₂CO₃ and Nb₂O₅. In this paper, we elucidated the mechanism for the formation of LiNbO₃ in the system Li₂CO₃-Nb₂O₅ with various compositions.

EXPERIMENTAL

The starting materials were niobium pentoxide (99.9% pure) and lithium carbonate (G.R. grade). The particle size of Nb_2O_5 for 400 particles was micro-



Fig. 1. Log normal probability graph of Nb₂O₅ particles size.

scopically determined in the range of $0.1-1.0 \mu$. Figure 1 shows the log probability plots of the size distribution of Nb₂O₅ particles. This indicates that the Nb₂O₅ particle sizes obey the log normal distribution. The Nb₂O₅ particles were approximately cylindrical in shape. By means of SEM, the particle size of Li₂CO₃ was found to be in the range 1.0-3.0 μ . The particles were approximately platy in shape. Powder of Nb₂O₅ and Li₂CO₃ was thoroughly mixed in a mortar with a pestle in the mole ratios of 1:3, 1:1, 3:1. The mixed powder was stored in a desiccator with silica gel.

The reaction between Nb₂O₅ and Li₂CO₃ was followed by a TG experiment. The TG experiment was carried out with an apparatus attached to a RMB-5V type microbalance (Shimazu Seisaku Sho), the accuracy of which corresponds to ± 1 %. The mixed powder (ca. 30 mg) was lightly packed in a fused-silica basket (7 mm in diameter and 3 mm in depth) and it was suspended in a fused-silica tube (30 mm in diameter) through which dry air or nitrogen was allowed to flow at a rate of 20 ml min⁻¹. The reaction temperature was measured with a Pt-Pt/13%Rh thermocouple, being attached to the inside of the tube at the height of the basket. The non-isothermal TG experiment was carried out by heating at a rate of 5°C min⁻¹ under flowing air. The isothermal TG experiment was carried out at various temperatures fixed in the range of 475 to 677°C under the same condition. The buoyancy correction was checked at elevated temperatures under flowing air. X-ray analysis was performed for the samples obtained by TG experiments. The DTA experiment was carried out with a Thermoflex apparatus (Rigaku-Denki). A heating rate of 10°C min⁻¹ was applied. α -Al₂O₃ was taken as the standard material.

RESULTS

Figure 2 shows weight loss curves on heating of a mixed powder of Li₂CO₃



Fig. 2. Weight loss curves on heating the mixed powder of Li₂CO₃ and Nb₂O₃ in mole ratios 1:1 (curve A), 1:3 (curve B) or 3:1 (curve C). $\emptyset = 5^{\circ}$ C min⁻¹, flowing air: 20 ml min⁻¹.



Fig. 3. DTA curves on heating the mixed powder of Li₂CO₃ and Nb₂O₅ in mole ratios 1:1 (curve A), 1:3 (curve B) or 3:1 (curve C). $\emptyset = 10^{\circ}$ C min⁻¹, Pt-Pt/13%Rh thermocouple, static air. Sample weight; curve A: 339 mg, curve E: 452 mg, curve C: 348 mg.



Fig. 4. X-ray diffraction patterns of samples heated to temperatures corresponding to points on TG curve using a composition of $Li_2CO_2 + 3Nb_2O_5$. $\triangle = Nb_2O_5$; $\times = LiNbO_2$; $\bigcirc = LiNb_2O_5$. $\varnothing = 5^{\circ}C \min^{-1}$; (a) 560°C, (b) 650°C, (c) 880°C.

and Nb₂O₅ in the mole ratios of 1:1 (curve A), 1:3 (curve B) or 3:1 (curve C) under flowing air. The ordinate corresponds to the percentage of the weight loss of CO₂ calculated from the amount of Li₂CO₃ contained in the mixed powder by use of the decomposition equation of Li₂CO₃: Li₂CO₃ \rightarrow Li₂O + CO₂. In curve A, the weight loss continues to increase from 300°C, the degree of the increase falling slightly at ca. 600°C and is completed at 720°C. In curve B, it begins to occur at 300°C, a rapid increase being observed from 480°C and is completed at 630°C. Curve C shows that there is an inflection point at ca. 600°C, as indicated by the dotted line. The weight loss in curve C may proceed at two stages: the first at 300-600°C and the second at 600-820°C. Figure 3 shows DTA curves on heating of the mixed powder of Li₂CO₃ and Nb₂O₅ in the mole ratios 1:1 (curve A), 1:3 (curve B) or 3:1 (curve C). Curve A shows an endothermic peak at 470-720°C and an exothermic peak at 720-800°C. Curve B shows one endothermic peak at 500-640°C and two exothermic peaks at 640-810°C. Curve C shows one large endothermic peak in the range 470-780°C.

Figure 4 shows the X-ray diffraction patterns of the samples heated to temperatures corresponding to points on the TG curve with a composition of $Li_2CO_3 + 3Nb_2O_5$. At 560 and 650°C, the peaks for LiNbO₃ are observed, those for Nb₂O₅ remaining. The weak (410) reflection for LiNb₃O₈ is seen² at 650°C. The single phase of LiNb₃O₈ is obtained at 880°C. Fig. 5 shows the X-ray diffraction patterns of the samples heated to temperatures on the TG curve with a composition of $3Li_2CO_3 + Nb_2O_5$. The peaks for LiNbO₃ are observed, those for Li₂CO₃ and Nb₂O₅ remain at 600°C. With a rise in reaction temperature at 700-870°C, the peaks for LiNbO₃ are lowered and those³ for Li₃NbO₄ are simultaneously increased. The single phase of Li₃NbO₄ is obtained at 910°C. Figure 6 shows changes of the X-ray intensities for LiNbO₃, LiNb₃O₈, Li₃NbO₄ and Nb₂O₅ in the samples heated to temperatures on the TG curve when a system with a composition of Li₂CO₃ and Nb₂O₅ is used. LiNbO₃ increases continuously with a rise in reaction temperature. However, Nb₂O₅



Fig. 5. X-ray diffraction patterns of samples heated to temperatures corresponding to points on TG curve using a composition of $3Li_2CO_3 + Nb_2O_5$. $\bigcirc := Li_2CO_3$; $\triangle := Nb_2O_5$; $\times := LiNbO_2$; $\bigoplus = Li_3NbO_4$. $\varnothing := 5^{\circ}C \min^{-1}$; (a) 600°C, (b) 700°C, (c) 740°C, (d) 790°C, (e) 870°C, (f) 910°C.



Reaction temperature (°C)

Fig. 6. Changes of X-ray intensities for Nb₂O₅, LiNbO₃, LiNb₃O₈ or Li₂NbO₄ in samples heated to temperatures corresponding to points on TG curve using a composition of Li₂CO₃ \div Nb₂O₅. $\nabla = Nb_2O_5(001); \Delta = LiNbO_5(012); O = LiNb_3O_6(410); \oplus = Li_2NbO_4(400). \emptyset =: 5^{\circ}C/min.$



Fig. 7. Changes of intensities of (410) reflection for LiNb₂O₃ in samples with a composition of Li₂CO₃ \div Nb₂O₃ beated at various temperatures. $\bigcirc -600^{\circ}$ C; $\bigcirc = 700^{\circ}$ C; $\bigcirc = 800^{\circ}$ C; $\bigcirc = 900^{\circ}$ C.



Fig. 8. Weight loss curves of the mixed powder of Li₂CO₃ and Nb₂O₅ in mole ratio 1:1. \bigcirc = 475°C; \bigcirc = 510°C; \bigcirc = 557°C; \bigcirc = 606°C; \bigcirc = 636°C; \triangle = 677°C.

continues to decrease and disappears at 750°C, which is close to the temperature of the complete weight loss determined in Fig. 2(A). LiNb₃O₈ begins to appear at ca. 600°C, reaches the maximum at 700°C and disappears at 850°C. The weak peak for Li₃NbO₂ is observed at 700-750°C. Figure 7 shows the X-ray intensity for LiNb₃O₈ in the samples heated at various temperatures in the range 600-900°C when a composition of Li₂CO₃ \div Nb₂O₅ is used. LiNb₃O₈ increases continuously after 0.5 h at 600°C and decreases after 0.5 h at 700-900°C. It disappears after 5 h at 800°C or 2 h at 900°C.

Figure 8 shows weight loss curves of the mixed powder of Li_2CO_3 and Nb_2O_5 at temperatures in the range 475 to 677°C. The weight loss increases parabolically at each temperature.

DISCUSSION

In each composition, the amount of weight loss when the reaction was finished was consistent with that of CO_2 calculated from the complete decomposition of Li_2CO_3 (Fig. 2). This indicates that the weight loss on TG curves is due to CO_2 evolution. It is said⁴ that Li_2CO_3 begins to decompose to Li_2O and CO_2 at 618 °C. No weight loss was observed in the TG measurement of pure Li_2CO_3 up to ca. 500 °C. There was little difference in the weight loss curves under the different atmospheres. The results of the X-ray analysis for the samples obtained by TG experiments (Figs. 4-6) showed the formation of lithium niobate (LiNbO₃, LiNb₃O₈ or Li₃NbO₄). These imply that CO₂ evolution is associated with the reaction between Li_2CO_3 and Nb_2O_5 , resulting in the formation of lithium niobate.

With a composition of $\text{Li}_2\text{CO}_3 + 3\text{Nb}_2\text{O}_5$, CO_2 evolution started at 300°C, a rapid increase in its amount being observed from 480°C and was finished at 630°C (Fig. 2(B). The temperature range of 480-630°C coincides with that of the endothermic peak on DTA curve (Fig. 3(B). The results of the X-ray analysis showed the presence of LiNbO₃ at 560 and 650°C. Thus, it is concluded that the reaction between Li₂CO₃ and Nb₂O₅ proceeds endothermally with the formation of LiNbO₃ at 300-630°C. The presence of LiNb₃O₈ above 650°C is due to the further reaction between LiNbO₃ and Nb₂O₅: LiNbO₃ ÷ Nb₂O₅ → LiNb₃O₈. The formation of LiNb₃O₈ may exothermally proceed at the two stages, as shown in Fig. 3(B).

As described above, the reaction between $3Li_2CO_3$ and Nb_2O_5 proceeds at the two stages: the first at 300-600 °C and the second above 600 °C. The reaction at the two stages accompanies the large endothermic effect, as shown in Fig. 3(C). When the first stage was finished at 600 °C, LiNbO₃ was formed (Fig. 5). The percentage of CO₂ evolution reached 34% at 600 °C. This indicates that the equimolecular reaction between Li_2CO_3 and Nb_2O_5 occurs to form LiNbO₃ at the first stage. Li_3NbO_4 was detected by X-ray analysis at 700 °C. It is concluded that further reaction between LiNbO₃ and Li₂CO₃ occurs to form Li₃NbO₄ at the second stage.

With a composition of $Li_2CO_3 \div Nb_2O_5$, CO_2 evolution started at 300°C, the degree of its increase falling slightly above 600°C and was finished at 720°C (Fig. 2(A). The results of X-ray analysis (Fig. 6) showed the increase of LiNbO₃ with simultaneous decrease of Nb₂O₅ at 500-700°C. On the other hand, LiNb₃O₈ began to form at 600°C and disappeared at 850°C through the maximum at 700°C. This indicates that the reaction between Li₂CO₃ and Nb₂O₅ occurs to form LiNbO₃ with evolution of CO₂ at 300-700°C and the further reaction between LiNbO₃ and Nb₂O₅ results in the formation of LiNb₃O₈ at 600-700°C. LiNb₃O₈ in addition to LiNbO₃ remains in the reaction product (Fig. 6), even after complete evolution of CO₂ at 720°C. Thus, there must be an amount of Li₂O in it because the equivalent amount of Li₂CO₃ and Nb₂O₅ is added. This may be consumed for the Li₃NbO₄ formation by the reaction between LiNbO₃ and Li₂O. This is supported by the formation of Li₃NbO₄ observed at 700-750°C. Accordingly, it is thought that the LiNbO₃ formation above 700°C is due to the reaction between LiNb₃O₈ and Li₃NbO₄. DTA curve 3-A can be explained as follows: an endothermic peak is due to CO_2 evolution and an exothermic peak corresponds to $LiNb_3O_8$ formation due to the overlap of the endothermic peak with the exothermic peaks corresponding to those of curve 3-B.

As described above, the weight loss in Fig. 8 is associated with CO₂ evolution, i.e., LiNbO₃ formation. LiNb₃O₈ increased continuously at 600°C after 0.5 h (Fig. 7), the condition of which corresponds nearly to the fractional conversion F = 60-70%of LiNbO₃ formation in Fig. 8. In the range F = 0-60% without LiNb₃O₈ formation, kinetic data of Fig. 8 were treated with various equations⁵⁻⁸. As a result, it was found that the kinetic data fit best to Jander's equation⁵, in spite of some deviation. The main cause for the deviation is considered to be due to the wide size distribution of Nb₂O₅ particles, as shown in Fig. 1. Gallagher⁹ has evaluated the effect of the size distribution of particles on the reaction rate by use of the Serin-Ellickson equation. We similarly applied his method to the data in Fig. 8 by introducing the size distribution of particles into the Jander's equation. The equation is expressed by

$$[1 - (1 - F)^{1/3}]^2 = kt$$
⁽¹⁾

$$k = 2DC_0/r^2 \tag{2}$$

$$F = 1 - \left(1 - \sqrt{2DC_0 t/r^2}\right)^3$$
(3)

where k = rate constant, t = reaction time, D = diffusion coefficient, $C_0 =$ concentration of reactant at the interface, and r = particle radius. The Nb₂O₅ particles were distributed according to the log normal distribution (Fig. 1). It is necessary to evaluate the fractional conversion about each of particles with the log normal distribution and then compute the total fractional conversion of all the reacted particles. The total fraction conversion, F, is expressed by^{9, 10}

$$F = \sum_{m=-\infty}^{\infty} F_m(\delta V/V)_m = \sum_{m=-\infty}^{\infty} \left[1 - \left(1 - \sqrt{G/\sigma_g^{2m/L}}\right)^3\right] (\delta V/V)_m$$
(4)

where $F_{m} :=$ the fractional conversion in a particle with a radius equal to that of the *m* th slice on the log normal distribution, $(\delta V/V)_{m}$ = the volume fraction in the *m* th slice, $G = 2DC_{0}t/(r'_{g})^{2}(r'_{g}) =$ geometric mean radius by volume), $\sigma_{g} =$ geometric standard deviation by volume, L = the number of slices into which the interval log σ_{g} is divided (L = 5 in this case), m = a number: -14.5, ..., -1.5, -0.5, 0, 0.5, 1.5, ..., 14.5, for L = 5. In eqn (4), the standard deviation range of $+3\log \sigma_{g}$ to $-3\log \sigma_{g}$ is put on both sides of the mean. From Fig. 1, the values of both r_{g} and σ_{g} are graphically evaluated¹¹: $r_{g} = 1.8$ and $\sigma_{g} = 2.0$. If a value of G is evaluated from eqn (4) for a measured value of F, Jander's curves are computed over a wide range of values of σ_{g} on a reduced time scale¹² and can be compared with the experimental data on the same scale. However, it is impossible to compute G directly from F. Hence, the G value corresponding to a given value of F in F = 0-0.70 was computed within an error less than ± 0.002 of F value by trial and error on a FACOM230-60/75 computer.



Fig. 9. Computed Jander's curves on a reduced time scale as a parameter of $\sigma_{\rm g}$ and experimental points of Fig. 8 plotted on the same time scale. Experimental points: $\bigcirc = 510^{\circ}$ C; $\bigcirc = 557^{\circ}$ C: $\times = 606^{\circ}$ C; $\bigcirc = 636^{\circ}$ C.

Figure 9 shows the experimental points of Fig. 8 plotted on a reduced time scale and the Jander's curves computed on the same scale as a parameter of σ_g by use of the above computed values of F and G. The curve for $\sigma_g = 1$ corresponds to the case of uniform particle size. A comparison of the experimental points with the Jander's curves for a variety of σ_g indicates that LiNbO₃ formation can be described by Jander's equation having the particle size distribution of Nb₂O₅ in $\sigma_g = 3.0$ to 4.0. The discrepancy of the above σ_g value with $\sigma_g = 2.0$ determined from Fig. 1 may result from a difference in the shape of particles⁹: the particle size in the case of Fig. 8 is assumed to be spherical, but is cylindrical in reality. The k constants were obtained in both cases of $\sigma_g = 3.0$ and 4.0 and the value of activation energy from the plots of log k against 1/T was determined to be 51 kcal mol⁻¹. The SEM observation showed that the reacted powders at 750°C in Fig. 2(A) are cylindrical in spite of a reduction in size. On the contrary, the plate-like particles which have the same shape as Li₂CO₃ particles were not observed. This suggest that the reaction between Li₂CO₃ and Nb₂O₅ proceeds by the diffusion of Li₂O through the formed layer of LiNbO₃.

The mechanism for LiNbO₃ formation in the system $Li_2CO_3-Nb_2O_5$ is summarized as follows. With a composition of $Li_2CO_3 + 3Nb_2O_5$ or $3Li_2CO_3 + Nb_2O_5$, the equimolecular reaction between Li_2CO_3 and Nb_2O_5 proceeds with CO_2 evolution to form LiNbO₃ at ca. 300-600 °C, but Nb₂O₅ or Li₂CO₃ remains unreacted. The reaction of a composition of $Li_2CO_3 + Nb_2O_5$ can be illustrated by Fig. 10. At 300-700 °C, the reaction between Li_2CO_3 and Nb_2O_5 occurs to form LiNbO₃. The diffusion of Li_2O through the layer of LiNbO₃ is rate-controlling with the activation energy of 51 kcal mol⁻¹. At 600-700 °C, LiNb₃O₈ results from the reaction between LiNbO₃ and Nb₂O₅. CO₂ evolution is finished at 720 °C. Near this temperature, an excess amount of Li₂O remains at the outer surface of LiNbO₃. Li₂O reacts with 144



Fig. 10. Schematic representation of a powder reaction of a composition of $Li_2CO_3 + Nb_2O_5$. (a) 300-600°C; (b) 600-700°C; (c) 700-850°C; (d) above 850°C.

LiNbO₃ to form Li₃NbO₄. At 700-850°C, the Li₂O component of Li₃NbO₄ diffuses toward the boundary of the LiNb₃O₈ layer through the LiNbO₃ layer. The single phase of LiNbO₃ develops above 850°C.

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