THERMODYNAMICS OF ASSOCIATED SOLUTIONS CONTAINING ACETONITRILE AND 2-BUTANOL

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ABSTRACT

Vapour-liquid and liquid-liquid equilibria and excess molar enthalpy data for ternary mixtures containing 2-butanol, acetonitrile and a non-associating component have been successfully analysed using an association model with binary parameters alone. The model assumes four association constants for the alcohol, two for acetonitrile and solvation constants between unlike molecules, allowing for a non-polar interaction term given by the NRTL equation.

INTRODUCTION

The thermodynamic properties of solution of non-associating components with acetonitrile or one of the butanols have been explained with association models based on mole fraction statistics [1,2]. These models were combined to analyse the properties of binary and ternary mixtures of acetonitrile and l-butanol [3] or 2-methyl-l-propanol [4].

In this work, the model is applied to mixtures containing acetonitrile and 2-butanol because the following experimental results are available: vapour-liquid equilibrium (VLE) data for 2-butanol + acetonitrile and 2 b utanol + acetonitrile + benzene at 60° C [5]; liquid-liquid equilibrium (LLE) data for 2-butanol + acetonitrile + cyclohexane or $+n$ -hexane or + n-heptane at 25°C [6]; excess molar enthalpy data for 2-butanol + acetonitrile and 2-butanol + acetonitrile + benzene at 25° C [7].

ASSOCIATION MODEL

In a ternary mixture formed by 2-butanol, acetonitrile and benzene, the association model assumes the association of the alcohol and acetonitrile,

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and solvation between each pair of the associating components and benzene. The non-polar interactions between all the components are expressed by the NRTL equation [8]. The equilibrium constants of the association and solvation are defined in terms of the mole fractions of the molecular species existing in the mixture.

Let 2-butanol be denoted by A, acetonitrile by B and benzene by C. The equilibrium constants for the association of the alcohol involving linear open polymers and cyclic polymers are given by

$$
K_2 = x_{A_2}/x_{A_1}^2 \qquad \text{for } A_1 + A_1 = A_2 \tag{1}
$$

$$
K_3 = x_{A_3}/x_{A_2}x_{A_1} \quad \text{for } A_1 + A_2 = A_3
$$
 (2)

$$
K = x_{A_{i+1}} / x_{A_i} x_{A_1} \quad \text{for } A_1 + A_i = A_{i+1}, i \ge 3
$$
 (3)

$$
K_{cy} = \theta / i = x_{A_i}(\text{cyclic}) / x_{A_i}(\text{open}) \text{ for } A_i(\text{open}) = A_i(\text{cyclic}), i > 4
$$
 (4)

and those of acetonitrile cyclic dimer and linear polymers are

$$
K'_{\mathbf{B}} = x_{\mathbf{B}_2}(\text{cyclic}) / x_{\mathbf{B}_1}^2 \quad \text{for } \mathbf{B}_1 + \mathbf{B}_1 = \mathbf{B}_2(\text{cyclic})
$$
 (5)

$$
K_{\mathbf{B}} = x_{\mathbf{B}_{i+1}} / x_{\mathbf{B}_{i}} x_{\mathbf{B}_{i}} \qquad \text{for } \mathbf{B}_{1} + \mathbf{B}_{i} = \mathbf{B}_{i+1}, \ i \geq 1 \tag{6}
$$

Two solvation constants between the alcohol and acetonitrile are expressed by

$$
K_{A,B} = x_{A,B} / x_{A,X_{B_1}} \quad \text{for } A_i + B_1 = A_i, \quad i \ge 1
$$
 (7)

$$
K_{A,B_j} = x_{A,B_j}/x_{A_j}x_{B_j} \quad \text{for } A_i + B_j = A_i, \quad i \ge 1, \ j \ge 2
$$
 (8)

and those of the associating components and benzene are as follows

$$
K_{A,C} = x_{A,C}/x_{A,XC_1} \quad \text{for } A_i + C_1 = A_i, i \ge 1
$$
 (9)

$$
K_{\text{BC}} = x_{\text{BC}} / x_{\text{B}_1} x_{\text{C}_1} \qquad \text{for } \text{B}_1 + \text{C}_1 = \text{BC} \tag{10}
$$

These equilibrium constants change with temperature according to the van't Hoff relation. The enthalpies of formation are assumed to be independent of temperature

$$
\frac{\partial \ln K_2}{\partial (1/T)} = -\frac{h_2}{R}, \qquad \frac{\partial \ln K_3}{\partial (1/T)} = -\frac{2h_A - h_2}{R}
$$
\n
$$
\frac{\partial \ln K}{\partial (1/T)} = -\frac{h_A}{R}, \qquad \frac{\partial \ln \theta}{\partial (1/T)} = -\frac{h_A}{R}
$$
\n
$$
\frac{\partial \ln K'_B}{\partial (1/T)} = -\frac{h'_B}{R}, \qquad \frac{\partial \ln K_B}{\partial (1/T)} = -\frac{h_B}{R}
$$
\n
$$
\frac{\partial \ln K_{A,B}}{\partial (1/T)} = -\frac{h_{A,B}}{R}, \qquad \frac{\partial \ln K_{A,B}}{\partial (1/T)} = -\frac{h_{A,B}}{R}
$$
\n
$$
\frac{\partial \ln K_{A,C}}{\partial (1/T)} = -\frac{h_{A,C}}{R}, \qquad \frac{\partial \ln K_{B,C}}{\partial (1/T)} = -\frac{h_{B,C}}{R}
$$
\n(11)

The activity coefficients of each component in the ternary mixtures, derived from the model assumptions, are expressed by

$$
\ln \gamma_{I} = \ln \frac{x_{I_{1}}}{x_{I_{1}}^{*}x_{I}} + \frac{\sum_{J=A} \tau_{JI}G_{JI}x_{J}}{\sum_{K=A} G_{KI}x_{K}} + \sum_{J=A} \frac{x_{J}G_{IJ}}{\sum_{K=A} G_{KI}x_{K}} \left\{ \tau_{IJ} - \frac{\sum_{R=A} x_{R}\tau_{RJ}G_{RJ}}{\sum_{K=A} G_{KJ}x_{K}} \right\}
$$
(12)

where

$$
\tau_{JI} = \left(\frac{g_{JI} - g_{II}}{\rho}\right) / T \tag{13}
$$

$$
G_{JI} = \exp(-\alpha_{JI}\tau_{JI})\tag{14}
$$

and $\alpha_{JI} (= \alpha_{IJ})$ is the non-randomness parameter set at 0.3.

The monomer mole fractions x_{A_i} , x_{B_i} , and x_{C_i} in eqn. (12) are related to the nominal mole fraction in terms of the equilibrium constants, and are obtained from the simultaneous solution of eqns. (15) - (19)

$$
x_{A} = \left\{ \left[1 + K_{A,B}x_{B_{1}} + K_{A,C}x_{C_{1}} + \frac{K_{A,B_{1}}K_{B}x_{B_{1}}^{2}}{(1 - w)} \right] \times \left[x_{A_{1}} + 2K_{2}x_{A_{1}}^{2} + \frac{K_{2}K_{3}x_{A_{1}}^{3}(3 - 2z)}{(1 - z)^{2}} \right] + \frac{K_{2}K_{3}K^{2}\theta x_{A_{1}}^{5}}{(1 - z)} \right\} / S \qquad (15)
$$

$$
x_{A} = \left\{ \left[x_{A,B_{1}} + \frac{K_{A,B_{1}}K_{B}x_{B_{1}}^{2}(2 - w)}{(1 - z)^{2}} \right] \left[x_{A,B_{1}} + \frac{K_{2}K_{3}x_{A_{1}}^{3}}{1 - z^{2}} \right] \right\}
$$

$$
x_{\mathbf{B}} = \left\{ \left\| K_{\mathbf{A},\mathbf{B}} x_{\mathbf{B}_1} + \frac{K_{\mathbf{A},\mathbf{B}_1} K_{\mathbf{B}} x_{\mathbf{B}_1}^2 (2 - w)}{(1 - w)^2} \right\| x_{\mathbf{A}_1} + K_2 x_{\mathbf{A}_1}^2 + \frac{K_2 K_3 x_{\mathbf{A}_1}^3}{(1 - z)} \right\}
$$

$$
+2K'_{B}x_{B_{1}}^{2}+\frac{x_{B_{1}}}{(1-w)^{2}}+K_{BC}x_{B_{1}}x_{C_{1}}\bigg\}/S
$$
\n(16)

$$
x_{\rm C} = \left\{ K_{\rm A,C} x_{\rm C_1} \left[x_{\rm A_1} + K_2 x_{\rm A_1}^2 + \frac{K_2 K_3 x_{\rm A_1}^3}{(1-z)} \right] + K_{\rm BC} x_{\rm B_1} x_{\rm C_1} + x_{\rm C_1} \right\} / S \tag{17}
$$

where S is the stoichiometric sum, given by

$$
S = \left[1 + K_{A,B}x_{B_1} + K_{A,C}x_{C_1} + \frac{K_{A,B_1}K_Bx_{B_1}^2}{(1 - w)}\right]
$$

$$
\times \left[x_{A_1} + 2K_2x_{A_1}^2 + \frac{K_2K_3x_{A_1}^3(3 - 2z)}{(1 - z)^2}\right] + \frac{K_2K_3K^2\theta x_{A_1}^5}{(1 - z)}
$$

+
$$
\left[K_{A,B}x_{B_1} + K_{A,C}x_{C_1} + \frac{K_{A,B_1}K_Bx_{B_1}^2(2 - w)}{(1 - w)^2}\right]
$$

$$
\times \left[x_{A_1} + K_2 x_{A_1}^2 + \frac{K_2 K_3 x_{A_1}^3}{(1-z)} \right] + 2K'_B x_{B_1}^2 + \frac{x_{B_1}}{(1-w)^2} + 2K_{BC} x_{B_1} x_{C_1} + x_{C_1}
$$
 (18)

with $z = Kx_{A_1}$ and $w = K_Bx_{B_1}$.

The total sum of mole fraciions of the species present in the mixture must be equal to unity

$$
\left[1 + K_{A,B}x_{B_1} + K_{A,C}x_{C_1} + \frac{K_{A,B_1}K_Bx_{B_1}^2}{(1 - w)}\right]\left[x_{A_1} + K_2x_{A_1}^2 + \frac{K_2K_3x_{A_1}^3}{(1 - z)}\right]
$$

$$
-\frac{K_2K_3\theta}{K^3}\left[\ln(1 - z) + z + \frac{z^2}{2} + \frac{z^3}{3} + \frac{z^4}{4}\right]
$$

$$
+ K'_Bx_{B_1}^2 + \frac{x_{B_1}}{(1 - w)} + K_{BC}x_{B_1}x_{C_1} + x_{C_1} = 1
$$
(19)

The monomer mole fractions of the alcohol and acetonitrile in the pure liquids are obtained from eqns. (20) and (21) respectively. That of pure liquid benzene is given by $x_{C_1}^* = 1$.

$$
x_{A_1}^{\star} + K_2 x_{A_1}^{\star^2} + \frac{K_2 K_3 x_{A_1}^{\star^3}}{(1 - z^{\star})} - \frac{K_2 K_3 \theta}{K^3} \left[\ln(1 - z^{\star}) + z^{\star} + \frac{z^{\star^2}}{2} + \frac{z^{\star^3}}{3} + \frac{z^{\star^4}}{4} \right]
$$

= 1 (20)

$$
K'_{\mathbf{B}} x_{\mathbf{B}_1}^{\star^2} + \frac{x_{\mathbf{B}_1}^{\star}}{(1 - w^{\star})} = 1
$$
\n(21)

The ternary excess molar enthalpy of the mixture, given by the sum of the chemical and physical contribution, is expressed by

$$
H^{E} = H_{\text{chem}}^{E} + H_{\text{phys}}^{E}
$$

= $\left\{ \left[1 + K_{A,B}x_{B_{1}} + K_{A,C}x_{C_{1}} + \frac{K_{A,B_{1}}K_{B}x_{B_{1}}^{2}}{(1 - w)} \right] \right\}$
 $\times \left[h_{2}K_{2}x_{A_{1}}^{2} + \frac{h_{A}K_{2}K_{3}x_{A_{1}}^{3}(2 - z)}{(1 - z)^{2}} \right]$
+ $\frac{h_{A}K_{2}K_{3}K^{2}\theta x_{A_{1}}^{5}}{(1 - z)} + \left[1 + K_{A,B_{1}}\left(x_{A_{1}} + K_{2}x_{A_{1}}^{2} + \frac{K_{2}K_{3}x_{A_{1}}^{3}}{(1 - z)}\right) \right] \frac{h_{B}K_{B}x_{B_{1}}^{2}}{(1 - w)^{2}}$
+ $h_{B}'K_{B}'x_{B_{1}}^{2} + \left[x_{A_{1}} + K_{2}x_{A_{1}}^{2} + \frac{K_{2}K_{3}x_{A_{1}}^{3}}{(1 - z)}\right]$

$$
\times \left[h_{A,B} K_{A,B} x_{B_{1}} + h_{A,C} K_{A,C} x_{C_{1}} + \frac{h_{A,B} K_{A,B} K_{B} x_{B_{1}}^{2}}{(1 - w)} \right]
$$

+ $h_{BC} K_{BC} x_{B_{1}} x_{C_{1}} / S$
- $x_{A} \left[h_{2} K_{2} x_{A_{1}}^{\star 2} + \frac{h_{A} K_{2} K_{3} x_{A_{1}}^{\star 3} (2 - z^{\star})}{(1 - z^{\star})^{2}} + \frac{h_{A} K_{2} K_{3} K^{2} \theta x_{A_{1}}^{\star 5}}{(1 - z^{\star})} \right] / S_{A}^{\star}$
- $x_{B} \left[h_{B}^{'} K_{B}^{'} x_{B_{1}}^{\star 2} + \frac{h_{B} K_{B} x_{B_{1}}^{\star 2}}{(1 - w^{\star})^{2}} \right] / S_{B}^{\star}$
+ $R \sum_{I=A} x_{I} \left\{ \frac{\sum_{J=A} x_{J} [\partial(\tau_{JI} G_{JI}) / \partial(1/T)]}{\sum_{K=A} G_{K I} x_{K}}$
- $\sum_{J=A} \tau_{JI} G_{JI} x_{J} \sum_{K=A} x_{K} [\partial(G_{KI}) / \partial(1/T)] \right\}$
- $\frac{\sum_{J=A} \tau_{JI} G_{JI} x_{J} \sum_{K=A} x_{K} [\partial(G_{KI}) / \partial(1/T)]}{(\sum_{K=A} G_{K I} x_{K})^{2}}$ (22)

where $z^* = Kx_{A_1}^*$ and $w^* = K_Bx_{B_1}^*$; S_A^* and S_B^* are given by

$$
S_{A}^{\star} = x_{A_{1}}^{\star} + 2K_{2}x_{A_{1}}^{\star 2} + \frac{K_{2}K_{3}x_{A_{1}}^{\star 3}(3 - 2z^{\star})}{(1 - z^{\star})^{2}} + \frac{K_{2}K_{3}K^{2}\theta x_{A_{1}}^{\star 5}}{(1 - z^{\star})}
$$
(23)

$$
S_B^{\star} = 2K'_B x_{B_1}^{\star 2} + \frac{x_{B_1}^{\star}}{(1 - w^{\star})^2}
$$
 (24)

The temperature dependence of the energy parameters is assumed to be given by

$$
g_{JI} - g_{II} = C_{JI} + D_{JI}(T - 273.15) \tag{25}
$$

DATA REDUCTION

The VLE data were reduced using the thermodynamic relation
\n
$$
\phi_I y_I P = \gamma_I x_I \phi_I^s P_I^s \exp[v_I^L (P - P_I^s)/RT]
$$
\n(26)

where y is the vapour phase mole fraction and P is the total pressure. The vapour pressures of pure components, P^s , were taken from the original references or were calculated by the Antoine equation whose constants are available from the literature [9]. The fugacity coefficients, ϕ_t at *P* and ϕ_t at

 P_i^s , were calculated from the volume-explicit virial equation of state, truncated after the second term. The second virial coefficients were estimated by the method of Hayden and O'Connell [10]. The liquid molar volumes v^L were calculated from the modified Rackett equation [ll]. Values of the related parameters for the evaluation of these properties are given by Prausnitz et al. [12].

LLE calculations were performed by simultaneous solution of the following equations

$$
\left(\gamma_I x_I\right)^{\text{I}} = \left(\gamma_I x_I\right)^{\text{II}}\tag{27}
$$

$$
\left(\sum_{I=A} x_I\right)^I = 1, \left(\sum_{I=A} x_I\right)^{II} = 1
$$
\n(28)

where the superscripts I and II indicate the equilibrated liquid phases.

CALCULATED RESULTS

The association parameters of 2-butanol and acetonitrile were taken from previous papers: for 2-butanol, $K_2 = 25$, $K_3 = 60$, $K = 30$ and $\theta = 65$ at 25 °C, $h_2 = -21.2$ kJ mol⁻¹ and $h_A = -23.5$ kJ mol⁻¹ [2]; for acetonitrile $K_B' = 8.35$ and $K_B = 2.1$ at 45°C, $h_B' = -8.9$ kJ mol⁻¹ and $h_B = -6.7$ kJ mol^{-1} [1]. The enthalpies of complex formation are also the same as those given previously: $h_{A,B} = -22$ and $h_{A,B} = -16.8$ kJ mol⁻¹ for 2-butanol acetonitrile [3,4]; $h_{A,C} = -8.3 \text{ kJ} \text{ mol}^{-1}$ for 2-butanol + benzene [2]; $h_{BC} =$ -5.2 kJ mol⁻¹ for acetonitrile + benzene [1]. The values of the solvation constants are as follows: $K_{A,B} = 20$ and $K_{A,B} = 15$ at 60 °C for 2-butanol acetonitrile; $K_{A,C} = 2.0$ at 25 °C for 2-butanol + benzene [2]; $K_{BC} = 0.2$ at 45 $^{\circ}$ C for acetonitrile + benzene [1].

Table 1 gives the energy parameters obtained from the reductions of experimental phase equilibrium data of binary mixtures. The optimum energy parameters for the binary vapour-liquid equilibria were determined from the minimization of the sum of the squares of relative deviations in pressure plus the sum of the squares of deviations in the vapour phase mole fraction by means of the simplex method [22]. For partially miscible mixtures, the mutual solubility data were used to obtain the binary energy parameters. Figures 1A and 1B compare the experimental vapour liquid equilibria with the calculated results. Table 2 summarizes the results of excess molar enthalpy obtained by minimizing the sum of the squares of deviations in the excess molar enthalpy for all data points. Figure 2 shows the experimental and calculated excess molar enthalpy results of the two binary systems containing 2-butanol.

The ternary VLE and LLE data were calculated using the association model with only the binary parameters given in Table 1. The absolute

TABLE 1

Binary parameters and absolute arithmetic mean deviations as obtained from phase equilibrium data reduction

^a MS, mutual solubility data.

Fig. 1. Vapour-liquid equilibria: A, 2-butanol (A) + acetonitrile (B) at 60° C (data of Nagata [5]); B, 2-butanol (A) + benzene (B) at 45° C (data of Brown et al. [13]). ——, Calculated; 0, experimental.

TABLE 2

Binary parameters and absolute arithmetic mean deviations as obtained from excess molar enthalpy data reduction at 25° C

System $(A + B)$	data points	No. of Parameters					Absolute	Ref.
		C_{BA} (K)	C_{AB} (K)	D_{BA}	D_{AB}	α_{AB}	arith. mean deviation $(J \text{ mol}^{-1})$	
2-Butanol $+$ acetonitrile 15		-480.42	-17.97	-2.3988	-1.2126 0.3		- 9.5	
2-Butanol								
$+$ benzene	18	-687.39	577.73		$0.1422 - 6.4613$ 0.3		- 6.0	20
Acetonitrile $+$ benzene	15	399.37	-21.88	2.6005	-0.9393	0.3	-1.3	21

arithmetic mean deviations of the vapour phase mole fraction between the experimental and predicted values for the vapour-liquid equilibria of the 2-butanol (A) + acetonitrile (B) + benzene (C) system at 60 °C were Δy_A = 0.0035, $\Delta y_B = 0.0063$ and $\Delta y_C = 0.0056$. These values are calculated from $\Delta y_I = \sum_{j=1}^{N} |y_I(J, \text{expt}) - y_I(J, \text{calc})|/N$, where N is the number of data points. The absolute arithmetic mean deviation of the pressure was 0.646 kPa, and average relative deviation 1.3%.

Fig. 2. Excess molar enthalpies for two binary systems at 25° C. —, Calculated Experimental: A, 2-butanol + acetonitrile, \bullet , data of Nagata and Tamura [7]; B, 2-butanol benzene, \circ , data of Nagata and Tamura [20]; \triangle , data of Brown et al. [13].

Fig. 3. Ternary liquid-liquid equilibria at 25 °C: $___\$, calculated; $\bullet ____\$ g, experimental tie line, data of Nagata [6]. A, 2-butanol+ acetonitrile+ cyclohexane; B, 2-butanol+ acetonitrile + n -hexane; C, 2-butanol + acetonitrile + n -heptane.

Figure 3 shows the predicted LLE results for the three ternary mixtures. The ternary H^E data for the 2-butanol + acetonitrile + benzene system at 25° C were predicted using the association model with the binary parameters presented in Table 2. The absolute arithmetic mean deviation between the calculated and experimental values of the excess molar enthalpy was 17.8 J $mol⁻¹$.

It may be concluded that the association model reproduces the VLE and H^E data of the 2-butanol + acetonitrile system and predicts the ternary VLE, LLE and H^E data of the 2-butanol + acetonitrile + non-associating component systems with good accuracy.

LIST OF SYMBOLS

342

Subscripts

Superscripts

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