

Short communication

Thermochemistry of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$

Jianguo Zhou^{a,*}, Fengying Zhao^a, Qian Yang^b, Yan Lu^a, Shuping Xia^c, Shiyang Gao^{a,c}

^a College of Chemistry and Environmental Science, Henan Normal University, Xixiang 453007, China

^b Institute of Applied Chemistry, Shaanxi Normal University, Xi'an 710069, China

^c Xi'an Branch, Institute of Salt Lakes, Chinese Academy of Sciences, Xi'an 710043, China

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Abstract

The enthalpies of solution of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$ in approximately 1 mol dm^{-3} aqueous hydrochloric acid and of RbCl in aqueous (hydrochloric acid + boric acid + sodium chloride) were determined. From these results and the enthalpy of solution of H_3BO_3 in approximately 1 mol dm^{-3} $\text{HCl}(\text{aq})$ and of sodium chloride in aqueous (hydrochloric acid + boric acid), the standard molar enthalpy of formation of $-(5128.02 \pm 1.94)\text{ kJ mol}^{-1}$ for $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$ was obtained from the standard molar enthalpies of formation of $\text{NaCl}(\text{s})$, $\text{RbCl}(\text{s})$, $\text{H}_3\text{BO}_3(\text{s})$ and $\text{H}_2\text{O}(\text{l})$. The standard molar entropy of formation of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$ was calculated from the Gibbs free energy of formation of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$ computed from a group contribution method.

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Keywords: $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$; Standard molar enthalpy of formation; Solution calorimetry; Molar enthalpy of solution

1. Introduction

Since the discovery of the promising second harmonic generation properties of $\beta\text{-BaB}_2\text{O}_4$ (BBO) [1] and LiB_3O_5 (LBO) [2], the chemistry of borates has become of great interest to scientists due to their diverse industrial uses and rich structural chemistry. The studies of borate hydrates have been extensively explored in recent years and many new tetraborate hydrates have also been synthesized, the structure and thermal behavior being described [3–8]. All these compounds contain the $[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}$ tetraborate anion which is the same as that of borax. Recently, Ben Ali et al. [9] synthesized a new hydrated double metals tetraborate $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$ and determined its crystal structure.

In previous work [10–15], the standard molar enthalpies of formation of some hydrated alkali metals borates and hydrated alkali earth metals borates were reported. The thermodynamic properties of some hydrated double metals borates were also studied [16–18]. As part of the systematic study of the thermochemistry of hydrated borates and hydrated double borates of alkali metals and alkali earth metals, this paper reports the

standard molar enthalpies of formation as well as the calculated entropy of formation of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$.

2. Experimental

2.1. Synthesis of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]\cdot 4\text{H}_2\text{O}$

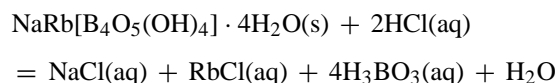
All of the chemical reagents used in synthesis were of analytical grade. Crystals of hydrated sodium rubidium tetraborate were obtained from an aqueous solution of $\text{RbB}_5\text{O}_6(\text{OH})_4\cdot 2\text{H}_2\text{O}$ and NaOH in a molar relation of 1/1, by the slow evaporation at room temperature (7 days) [9]. Colourless transparent crystals were filtered and washed with redistilled water and ether, respectively, and dried at room temperature. Composition of the crystal was determined as follows: Na and Cs were analyzed by atomic absorption spectroscopy (Hitachi Z5000 atomic absorption spectrometer); B was determined by titration with a standard solution of NaOH in the presence of mannitol; H_2O content was determined by thermal dehydration. The powder X-ray diffraction data of the synthesized compound was obtained using Bruker D8 advance with $\text{Cu K}\alpha$ radiation. TG-DSC curves were obtained on a Setaram-LabsysTM thermal analyzer with a heating rate of $1\text{ }^\circ\text{C/min}$ in flowing N_2 . TG-DTA curves were obtained on a Shimadzu DT-40 thermal analyzer in air with a heating rate of $10\text{ }^\circ\text{C/min}$. FT-IR spectra was

* Corresponding author. Tel.: +86 373 3326335; fax: +86 373 3329115.
E-mail addresses: jgzhou@henannu.edu.cn, zhoujgwj@sina.com (J. Zhou).

recorded on a FTS-40 FT-IR spectrometer (Bio-Rad) using KBr pellets.

2.2. Method of calorimetric experiment

Thermochemical reaction used for deriving $\Delta_f H_m^\circ$ of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$ is



The standard molar enthalpy of formation of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$ could be obtained by solution calorimetry in combination with the standard molar enthalpies of formation of $\text{RbCl}(\text{s})$, $\text{NaCl}(\text{s})$, $\text{H}_3\text{BO}_3(\text{s})$ and $\text{H}_2\text{O}(\text{l})$. The $\text{H}_3\text{BO}_3(\text{s})$ and $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}(\text{s})$ were each dissolved in approximately 1 mol dm^{-3} aqueous hydrochloric acid, the calculated amount of $\text{NaCl}(\text{s})$ was dissolved in aqueous ($\text{HCl} + \text{H}_3\text{BO}_3$) which consisted of approximately 1 mol dm^{-3} $\text{HCl}(\text{aq})$ and the calculated amount of H_3BO_3 and then the calculated amount of RbCl was dissolved in the mixed solution ($\text{HCl} + \text{H}_3\text{BO}_3 + \text{NaCl}$).

In the previous paper [21,22], the enthalpy of solution of $\text{H}_3\text{BO}_3(\text{s})$ in $\text{HCl}(\text{aq})$ and $\text{NaCl}(\text{s})$ in aqueous ($\text{HCl} + \text{H}_3\text{BO}_3$) were determined. In this paper, $\Delta_f H_m^\circ$ of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$ in $\text{HCl}(\text{aq})$ and of RbCl in aqueous ($\text{HCl} + \text{H}_3\text{BO}_3 + \text{NaCl}$) are determined. Both RbCl and NaCl (99.99% pure) were heated at 873 K for 3 h and stored in a desiccator. The H_3BO_3 (99.99% pure) was used as obtained. The HCl solvent was prepared from azeotropic hydrochloric acid and redistilled water, and its concentration determined by titration with standard sodium carbonate.

A RD496-III heat conduction microcalorimeter (Southwest Institute of Electron Engineering, China) was used. The sensitivity of the instrument was measured through electrical calibration and the accuracy and precision were determined by chemical calibration. The calibration was repeated after each experiment and the average calibration constant was used. The temperature of the calorimetric experiments was $298.15 \pm 0.005 \text{ K}$. A detailed description is found elsewhere [15,19]. The total time required for the complete reaction was about 1 h, depending on the samples. No solid residues were observed in the solution after the calorimetric experiments.

3. Results and discussion

3.1. Characterization of the synthetic sample

The analytical data of the compound is (calc.): Na_2O 8.39% (8.34%), Rb_2O 25.21% (25.17%), B_2O_3 37.48% (37.45%), H_2O 28.92% (29.04%). The characteristic d values (I/I_0) are presented in Table 1.

The IR spectrum of the compound is shown in Fig. 1. The absorption bands observed at 3584 and 3366 cm^{-1} are assigned to the stretching mode of the OH group. The band at 1631 cm^{-1} is due to the bending mode of this group. Thus, the compound contains crystallization water. The bands observed at 1442, 1349

Table 1
The powder X-ray diffraction data for $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$

d (Å)	I/I_0 (%)	d (Å)	I/I_0 (%)	d (Å)	I/I_0 (%)
8.6021	26.5	3.3564	31.8	2.7077	27.2
6.4285	43.8	3.2361	21.9	2.6532	30.0
5.4956	26.9	3.1912	26.1	2.6323	34.3
4.9569	25.1	3.0653	74.6	2.5589	22.3
4.6850	26.9	3.0281	33.9	2.5328	33.6
4.5552	30.0	2.9507	29.7	2.3901	21.2
4.4385	100.0	2.9174	19.8	2.0692	19.8
4.3794	33.9	2.8077	48.8	1.9161	22.6
4.0081	23.7	2.7848	23.7	1.7397	23.3
3.5557	32.5	2.7349	25.4	1.6892	19.8

and 944 cm^{-1} are, respectively, attributed to the antisymmetric and symmetric stretching modes of the group B(3)–O [20]. The bands observed in the region 1269–1135 cm^{-1} are due to the in-plane bending mode of the group B–O–H [20]. The bands at 1064, 1004, 836 and 813 cm^{-1} are assigned to the antisymmetric and symmetric stretching modes of the group B(4)–O [20]. The bands at 711 and 685 cm^{-1} are due to the out-of-plane bending mode of the group B(3)–O [20]. The band observed at 603 cm^{-1} is characteristic for the tetraborate anion and the bands at 522 and 464 cm^{-1} are due to the bending mode of the group B(4)–O [20].

TG-DSC curves showed the loss of 19.18% of mass in the range of 30–180 °C temperature range due to the loss of four molecules of crystallization water (calculated, 19.36%). The TG-DTA curves showed that the mass loss is 28.92% in the 30–400 °C temperature range and is due to the loss of six water molecules (calculated, 29.04%).

All these results showed that the synthesized compound is pure and has the general formula $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$ and it is suitable for calorimetric measurements.

3.2. Results of calorimetric experiment

The molar enthalpy of solution of RbCl in aqueous ($\text{HCl} + \text{H}_3\text{BO}_3 + \text{NaCl}$) measured at 298.15 K was $18.00 \pm 0.09 \text{ kJ mol}^{-1}$ ($n = 5$), where the uncertainty is twice the standard deviation of the mean. The molar enthalpy of solution of $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$ in approximately

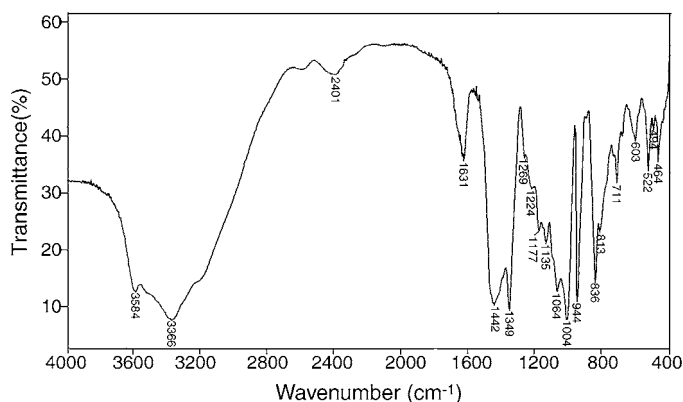


Fig. 1. The FT-IR spectrum of synthetic $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$.

Table 2
Thermochemical cycle and results for the derivation of $\Delta_f H_m^\circ$ (NaRbB₄O₇·6H₂O, 298.15 K)

Reaction	$\Delta_r H_m$ (kJ mol ⁻¹)
NaRbB ₄ O ₇ ·6H ₂ O(s) + 81.776(HCl·53.230H ₂ O)	55.62 ± 0.25
= Na ⁺ (aq) + Rb ⁺ (aq) + 2Cl ⁻ (aq) + 4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O)	(1)
4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O) = 4H ₃ BO ₃ (s) + 79.776(HCl·54.577H ₂ O)	(2)
Na ⁺ (aq) + Cl ⁻ (aq) + 4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O)	-87.32 ± 0.32
= NaCl(s) + 4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O)	(3)
Na ⁺ (aq) + Rb ⁺ (aq) + 2Cl ⁻ (aq) + 4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O)	-5.14 ± 0.02
= RbCl(s) + Na ⁺ (aq) + Cl ⁻ (aq) + 4H ₃ BO ₃ (aq) + 79.776(HCl·54.577H ₂ O)	(4)
81.776(HCl·54.577H ₂ O) = 81.776(HCl·53.230H ₂ O) + 110.154H ₂ O(l)	-18.00 ± 0.09
H ₂ (g) + Cl ₂ (g) + 109.154H ₂ O(l) = 2(HCl·54.577H ₂ O)	(5)
RbCl(s) = Rb(s) + 1/2Cl ₂ (g)	2.19 ± 0.04
NaCl(s) = Na(s) + 1/2Cl ₂ (g)	(6)
4H ₃ BO ₃ (s) = 4B(s) + 6H ₂ (g) + 6O ₂ (g)	(7)
H ₂ O(l) = H ₂ (g) + 1/2O ₂ (g)	(8)
NaRbB ₄ O ₇ ·6H ₂ O(s) = Na(s) + Rb(s) + 4B(s) + 6H ₂ (g) + 13/2O ₂ (g)	(9)
	(10)
	(11)
	435.35 ± 0.20
	411.15 ± 0.10
	4379.20 ± 3.20
	285.83 ± 0.04
	5128.02 ± 1.94 ^a

$$^a \Delta_f H_m^\circ = \Delta_r H_1 + \Delta_r H_2 + \Delta_r H_3 + \Delta_r H_4 + \Delta_r H_5 + \Delta_r H_6 + \Delta_r H_7 + \Delta_r H_8 + \Delta_r H_9 + \Delta_r H_{10}.$$

1 mol dm⁻³ HCl(aq) at 298.15 K was 55.62 ± 0.08 kJ mol⁻¹ ($n=5$). Table 2 gives the thermochemical cycle for the derivation of the standard molar enthalpy of formation of NaRb[B₄O₅(OH)₄]₂·4H₂O. The molar enthalpies of solution of H₃BO₃(s) of (21.83 ± 0.08) kJ mol⁻¹ in approximately 1 mol dm⁻³ HCl(aq), and of NaCl(s) of -(5.14 ± 0.02) kJ mol⁻¹ in the mixture of HCl and H₃BO₃ were taken from our previous work [21,22]. The standard molar enthalpies of formation of H₂O(l), NaCl(s), RbCl(s) and H₃BO₃(s) were taken directly from the CODATA Key Values [23], namely -(285.83 ± 0.04), -(411.15 ± 0.10), -(435.35 ± 0.20) and -(1094.8 ± 0.80) kJ mol⁻¹, respectively. The standard molar enthalpy of formation of HCl(aq) and the enthalpy of dilution of HCl(aq) were calculated from the data in NBS tables [24], respectively. From these data, applying Hess's law, the standard molar enthalpy of formation of NaRb[B₄O₅(OH)₄]₂·4H₂O was calculated to be -(5128.02 ± 1.94) kJ mol⁻¹, according to the following equation:

$$\Delta_f H_m^\circ = \Delta_r H_1 + \Delta_r H_2 + \Delta_r H_3 + \Delta_r H_4 + \Delta_r H_5 + \Delta_r H_6 + \Delta_r H_7 + \Delta_r H_8 + \Delta_r H_9 + \Delta_r H_{10}$$

The enthalpy of formation of NaRb[B₄O₅(OH)₄]₂·4H₂O can also be estimated by a group contribution method [25], which can be expressed as shown in following equation:

$$\begin{aligned} \Delta_f H_m^\circ(\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 4\text{H}_2\text{O}, \text{s}) \\ = \Delta_f H_m^\circ(\text{Na}^+, \text{aq}) + \Delta_f H_m^\circ(\text{Rb}^+, \text{aq}) \\ + \Delta_f H_m^\circ([\text{B}_4\text{O}_5(\text{OH})_4]^{2-}, \text{aq}) + 4\Delta_f H_m^\circ(\text{H}_2\text{O}) \end{aligned}$$

in which, the $\Delta_f H_m^\circ$ for [B₄O₅(OH)₄]²⁻ and H₂O have the values of -3464.46 and -290.42 kJ mol⁻¹, respectively [21]. The $\Delta_f H_m^\circ$ of -240.12 and -251.17 kJ mol⁻¹ for Na⁺ and Rb⁺, respectively, were taken from the NBS tables [24]. The calculated standard molar enthalpy of formation is, by using this scheme, -5117.43 kJ mol⁻¹. The relative error is 0.211%.

We also used a group contribution method to calculate $\Delta_f G_m^\circ$ of NaRb[B₄O₅(OH)₄]₂·4H₂O to be -4591 kJ mol⁻¹ according to

the following equation:

$$\begin{aligned} \Delta_f G_m^\circ(\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 4\text{H}_2\text{O}, \text{s}) \\ = \Delta_f G_m^\circ(\text{Na}^+, \text{aq}) + \Delta_f G_m^\circ(\text{Rb}^+, \text{aq}) \\ + \Delta_f G_m^\circ([\text{B}_4\text{O}_5(\text{OH})_4]^{2-}, \text{aq}) + 4\Delta_f G_m^\circ(\text{H}_2\text{O}) \end{aligned}$$

in which the values -3095.99 and -237.28 kJ mol⁻¹ for the $\Delta_f G_m^\circ$ of [B₄O₅(OH)₄]²⁻ and H₂O, respectively, were taken from the literature [24], and the $\Delta_f G_m^\circ$ of -261.91 and -283.98 kJ mol⁻¹ for Na⁺ and Rb⁺, respectively, were taken from the NBS tables [24]. Combining the $\Delta_f H_m^\circ$ of NaRb[B₄O₅(OH)₄]₂·4H₂O, the standard molar entropy of formation of NaRb[B₄O₅(OH)₄]₂·4H₂O has been calculated to be -1801.174 J mol⁻¹ K⁻¹ according to following equation:

$$\Delta_f S_m^\circ = \frac{\Delta_f H_m^\circ - \Delta_f G_m^\circ}{T}$$

Finally, the standard molar entropy of NaRb[B₄O₅(OH)₄]₂·4H₂O was calculated to be 467.757 J mol⁻¹ K⁻¹ according to reaction (11) in Table 2. The standard molar entropies of the elements were taken from the NBS tables [24] to be (51.21, 76.78, 5.86, 130.68 and 205.14) J mol⁻¹ K⁻¹ for Na(s), Rb(s), B(s), H₂(g) and O₂(g), respectively.

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