

Note

**A NEW METHOD FOR THE DETERMINATION OF THE ORDER OF REACTION FOR A SOLID STATE REACTION FROM THE DYNAMIC DTA CURVE**

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The concept of an order of reaction in the solid state has a limited significance compared with reactions in other phases. However, it is essential to calculate the so-called "order of reaction" for the purpose of calculating other kinetic parameters such as activation energy, frequency factor, specific reaction rate, etc.

Kissinger's shape index method [1] is usually used to determine the order of reaction from the DTA curve, but it has been recently pointed out that this method is not applicable for higher order reactions [2]. Further, the simplest method suggested by Piloyan et al. [3] for evaluating the activation energy does not include any consideration for the evaluation of the order of reaction. A new simple method, therefore, is suggested for the evaluation of the activation energy as well as the order of reaction from the same plot of  $\log \Delta T$  vs.  $1/T$  used for the Piloyan et al.'s [3] evaluation.

The rate of reaction is given by the usual relationships

$$\frac{d\alpha}{dt} = KC^\eta \quad (1)$$

or

$$\frac{d\alpha}{dt} = \frac{KC^\eta}{\beta} \quad (1a)$$

where  $C$  is the concentration, generally expressed in terms of the fraction remaining unreacted ( $1 - \alpha$ ),  $d\alpha/dt$  or  $d\alpha/dT$  is the reaction rate,  $K$  is the specific reaction rate constant,  $\beta$  is the heating rate, and  $\eta$  is the order of reaction.

Substituting  $K = Ze^{-E/RT}$  (Arrhenius equation) in eqn. (1a) and taking logarithms, this relation becomes

$$\log \frac{d\alpha}{dT} = \log \frac{Z}{\beta} - \frac{E}{2.303RT} + \eta \log(1 - \alpha) \quad (2)$$

where  $Z$  is the frequency factor,  $E$  the activation energy, and  $T$  the temperature (K).

Differentiating eqn. (1a) with respect to  $T$

$$\frac{d^2\alpha}{dT^2} = \frac{Z}{\beta} e^{-E/RT}(1-\alpha)^{\eta-1} \left[ -\eta \frac{d\alpha}{dT} + \frac{E}{RT^2} (1-\alpha) \right] \quad (3)$$

At the point of inflexion,  $d^2\alpha/dT^2 = 0$  and hence

$$E = \frac{\eta RT_{\max}^2}{(1-\alpha)_{\max}} \frac{(d\alpha)}{(dt)_{\max}} \quad (4)$$

Substituting eqn. (4) into eqn. (2) gives

$$\log \frac{d\alpha}{dT} = \log \frac{Z}{\beta} - \eta \left[ \frac{T_{\max}^2}{(1-\alpha)_{\max}} \frac{(d\alpha/dT)_{\max}}{2.303T} - \log(1-\alpha) \right] \quad (5)$$

Experimentally, it is observed that  $T_{\max}^2(d\alpha/dT)_{\max}/[(1-\alpha)_{\max} 2.303T] \gg \log(1-\alpha)$  (Table 1) and hence omitting  $\log(1-\alpha)$  in the equation

$$\log \frac{d\alpha}{dT} = \log \frac{Z}{\beta} - \frac{\eta T_{\max}^2 (d\alpha/dT)_{\max}}{(1-\alpha)_{\max} 2.303T} \quad (6)$$

$\log Z/\beta$  is a constant for all practical purposes.

The plot of  $\log(d\alpha/dT)$  vs.  $T_{\max}^2(d\alpha/dT)_{\max}/[(1-\alpha)_{\max} 2.303T]$  gives a straight line, the slope of which gives the order of reaction,  $\eta$ , and the intercept gives  $\log Z/\beta$ . The plot of  $\log(d\alpha/dT)$  vs.  $1/T$  also gives a straight line.

This slope, if divided by  $T_{\max}^2(d\alpha/dT)_{\max}/[(1-\alpha)_{\max}]$ , gives  $\eta$ , the order of reaction.

The plot of  $\log T$  vs.  $1/T$  is suggested by Piloyan et al. [3] for the evaluation of the activation energy from a DTA curve. The same plot, if used with

TABLE 1

Comparison of  $\frac{T_{\max}^2(d\alpha/dt)_{\max}}{(1-\alpha)_{\max} 2.303T}$   
and  $\log(1-\alpha)$  for  $\text{CdCO}_3$  decomposition

$\frac{T_{\max}^2(d\alpha/dT)_{\max}}{(1-\alpha)_{\max} 2.303T}$	$-\log(1-\alpha)$
54.39	0.0019
53.50	0.0075
52.57	0.0180
51.58	0.0356
50.51	0.0631
49.80	0.1073
48.99	0.1801
48.20	0.3032
47.39	0.5219
46.59	1.0342
46.34	1.9322

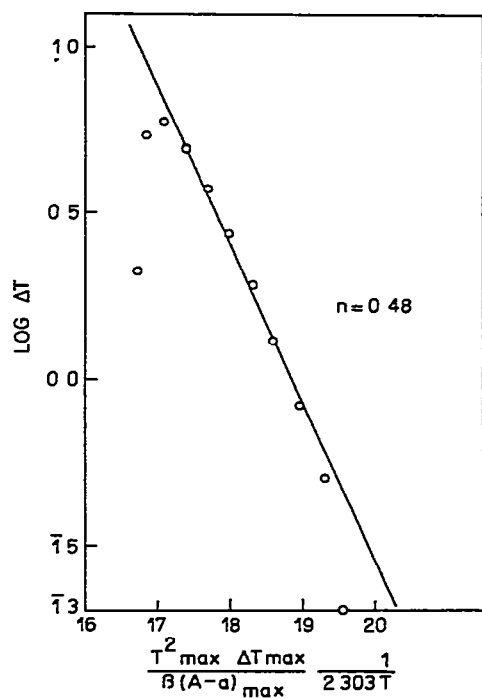


Fig. 1. Plot of  $\log \Delta T$  vs.  $T_{\max}^2 \Delta T_{\max} / [\beta(A-a)_{\max} 2.303T]$ .

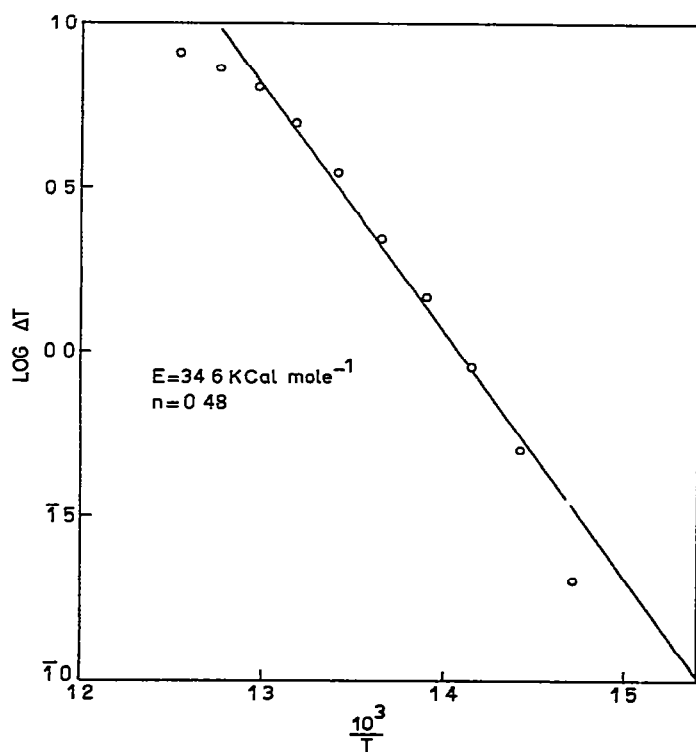


Fig. 2. Piloyan et al.'s method [3] plot for the decomposition of  $\text{CdCO}_3$ .

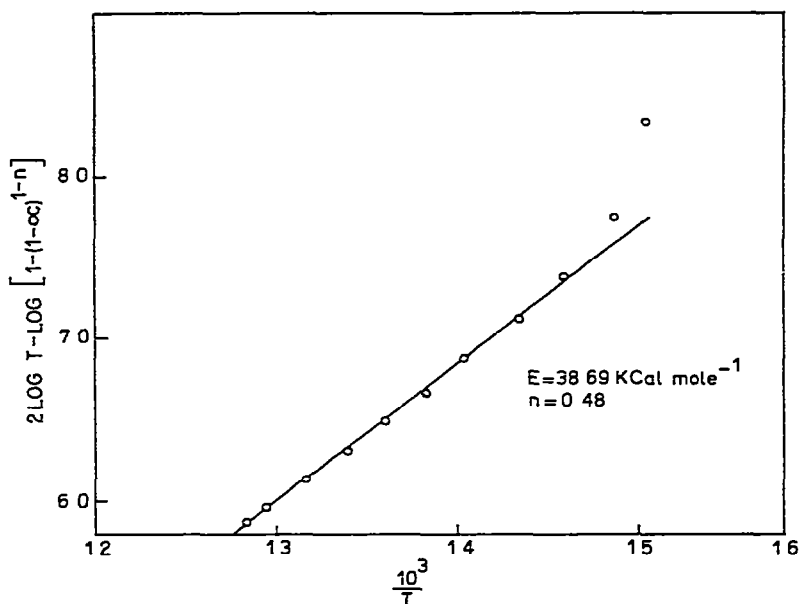


Fig. 3. Coats and Redfern's method plot [4] for the decomposition of  $\text{CdCO}_3$ .

proper multiplying factors, gives the activation energy and order of reaction simultaneously.

The rate of reaction  $d\alpha/dt$  or  $da/dt$  obtained from DTA curves where  $a$  is the area under the DTA peak (total area  $A$ ) is equivalent to  $\Delta T$  and the relation  $\Delta T = da/dt$  or  $A(d\alpha/dt)$  holds good.

Substituting this relation in eqn. (6) and replacing  $\alpha = a/A$ , where  $a$  is the area under the DTA peak at a particular point,  $A$  gives the relation

$$\log \Delta T = \log ZA - \frac{\eta T_{\max}^2 \Delta T_{\max}}{\beta (A - a)_{\max} 2.303T} \quad (7)$$

where  $\beta$  is the heating rate.

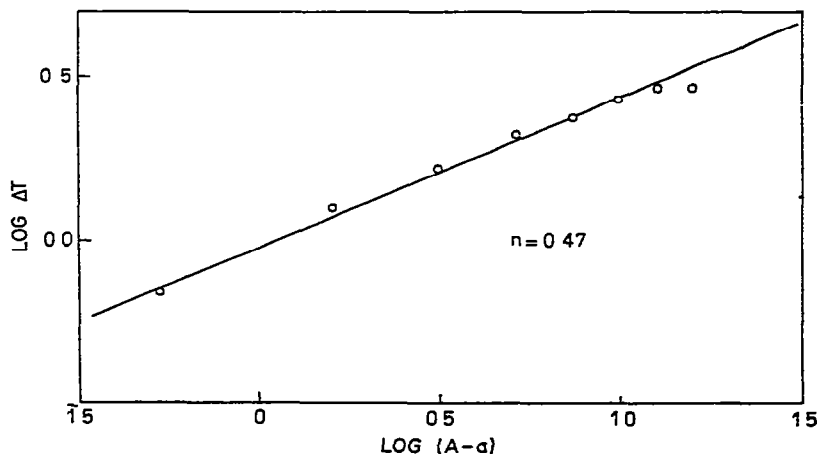


Fig. 4.  $\log \Delta T$  vs.  $\log(A - a)$  plot for the isothermal decomposition of  $\text{CdCO}_3$  at  $703 \pm 1$  K.

TABLE 2

Order of reaction values calculated from different methods for  $\text{CdCO}_3 \rightarrow \text{CdO} + \text{CO}_2$ 

Kissinger's method	0.48
Isothermal method	0.47
This method	0.48

A plot of  $\log \Delta T$  vs.  $T_{\max}^2 \Delta T_{\max} / [\beta(A - a)_{\max} 2.303T]$  (Fig. 1) gives a straight line, the slope of which will be  $\eta$ , the order of reaction. The plot of  $\log \Delta T$  vs.  $1/T$  also gives a straight line, the slope of which if divided by  $T_{\max}^2 \Delta T_{\max} / [\beta(A - a)_{\max} 2.303T]$  (whose  $\Delta T$  is expressed in temperature scale) will give the order of reaction (Fig. 2).

This relation was tested for the decomposition  $\text{CdCO}_3 \rightarrow \text{CdO} + \text{CO}_2$  and the order of reaction was found to be 0.48. The value determined from Kissinger's slope index method [1] was 0.48. Using this reaction order value, the activation energy value calculated by Coats and Redfern's method [4] for 0.5 order was found to be  $38.69 \text{ kcal mole}^{-1}$  (Fig. 3), which is comparable with the value calculated by the method of Piloyan et al. [3] (Fig. 2) and also by the conventional isothermal method (Fig. 4; Table 2).

It is evident from this that the method is very simple, convenient and easily applicable to solid state reactions.

## REFERENCES

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