# THERMODYNAMIC PROPERTIES OF TRILAURYLAMMONIUM BISULPHATE IN BENZENE

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#### ABSTRACT

We have studied the thermodynamic properties of trilaurylammonium bisulphate (TLAH<sub>2</sub>SO<sub>4</sub>) in benzene at several temperatures by vapour pressure osmometry (VPO). Values of the activity coefficients,  $\gamma_i$ , are given, which allows calculation of the excess thermodynamic functions,  $G^E$ ,  $S^E$  and  $H^E$ .

#### INTRODUCTION

In a preceding paper [1], the aggregation equilibria of trilaurylammonium bisulphate (TLAH<sub>2</sub>SO<sub>4</sub>) in benzene at several temperatures was studied. At the lowest ammonium salt concentrations, great deviation from ideal behaviour was found. On the other hand, the distribution diagrams of the aggregated species, (TLAH<sub>2</sub>SO<sub>4</sub>)<sub>n</sub>, at 25.0, 37.0 and 50.0°C showed a high temperature dependence since the trimer is the predominant species at 25.0°C, whilst at 50.0°C the dimer predominates. However, extension of the aggregation process does not depend in practice on temperature, i.e. the monomeric form of the ammonium salt is always the species in lower concentration. These facts can be applied in the back extraction processes using the TLAH<sub>2</sub>SO<sub>4</sub> as a metal stripping agent [2–5].

In order to find a better understanding of solute-solvent and solute-solute interactions, the excess functions of trilaurylammonium bisulphate in benzene at 25.0, 37.0 and 50.0°C were calculated.

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Benzene (Merck p.a.) was purified by standard procedures [6] and freshly distilled before use. Benzil (Merck p.a.) was purified by successive crystallizations in dried methanol. Benzil purity was checked by IR and DTA.

Trilaurylammonium bisulphate was prepared by shaking trilaurylamine (Merck p.a.), previously filtered in order to remove some carbonate impurities [7], with a cold aqueous solution of  $2M H_2SO_4$ . The precipitate formed was dissolved in dry diethylether and placed at 40°C. The resulting white crystalline solid was recrystallized six times. It was then heated at 40°C in order to remove traces of diethylether and stored in vacuum over anhydrous CaCl<sub>2</sub>.

Solutions of a desired (stoichiometric) molality, B (mole kg<sup>-1</sup>), were prepared from weighed amounts of the dried substances and freshly boiled redistilled benzene.

Measurements were carried out on a Knauer 1974 model vapour pressure osmometer. Calibration of the probe, containing two thermistors, was made using, as standard, benzene solutions of benzyl. The  $\Delta R$  values for both the standard and the ammonium salt were recorded on a Houston Recorder as a function of time. In all the samples 2–3 min were enough to attain constant resistance. At least three  $\Delta R$  values were measured for each solution and the mean value was taken. The drop size was kept as a constant as possible and equal in the two thermistors, so that the precision of the  $\Delta R$  values ranged between 0.5 and 1.00%.

## THEORY

A short theoretical justification of the equations used is given here.

Following the Gibbs-Duhem equation for a binary system at constant T and p

$$\sum n_i \mathrm{d}\mu_i = 0 \tag{1}$$

where  $\sum n_i$  is the total number of moles in the system and  $\mu_i$  is the chemical potential. For the solvent

$$\mu_1 = \mu_1^0(T, p) + RT\Phi_1 \ln x_1 \tag{2}$$

where  $\Phi_1$  is the osmotic coefficient of the solvent. Differentiating eqn. (2) and using its value in the Gibbs–Duhem equation gives

$$x_1 \ln x_1 d\Phi_1 + x_1 \Phi_1 d \ln x_1 + x_2 d \ln x_2 + x_2 d \ln \gamma_2 = 0$$
(3)

Differentiation of this equation with respect to  $x_2$  and taking into account that  $dx_1 + dx_2 = 0$  gives

$$x_{1} \ln x_{1} \left( \frac{d\Phi_{1}}{dx_{2}} \right) + x_{2} \left( \frac{d \ln \gamma_{2}}{dx_{2}} \right) - \Phi_{1} + 1 = 0$$
(4)

For dilute solutions, we can develop  $\ln x_1$  in series, and consequently  $\ln x_1 = \ln(1 - x_2) \approx -x_2$ , and

$$(1 - \Phi_1) - x_2 \left(\frac{\mathrm{d}\Phi_1}{\mathrm{d}x_2}\right) + x_2 \left(\frac{\mathrm{d}\ln\gamma_2}{\mathrm{d}x_2}\right) = 0 \tag{5}$$

Integrating from zero to  $X_2$ , we have

$$\ln \gamma_2 = (\Phi_1 - 1) + \int_0^{x_2} (\Phi_1 - 1) d \ln x_2$$
(6)

If we write the  $\Phi_i$  values in polynomial form

$$\Phi_i = 1 + \sum_{i=1}^J a_i m^i$$

where  $a_i$  is the coefficient of the polynomial which better adjusts to the previous equation and m is the theoretical molality. Introducing this value of the osmotic coefficient and integrating, we obtain

$$\ln \gamma_2 = \sum_{i=1}^{J} \left( \frac{i+1}{i} \right) a_i m^i \tag{7}$$

It is also possible to calculate the temperature dependence of the activity coefficient of the solute. Differentiating with respect to temperature at constant pressure, and employing the Gibbs-Helmholtz equation

$$\left(\frac{\partial \ln \gamma_2}{\partial T}\right)_{p,B} = \frac{h_2^{\infty} - h_2}{RT^2} = -\frac{\overline{L}_2}{RT^2}$$
(8)

where  $h_2$  and  $h_2^{\infty}$  are the partial molar enthalpy of the solute in the solution and the partial molar enthalpy of the solute at infinite dilution, respectively, and  $\overline{L}_2$  is the relative partial molar enthalpy of the solute.

The excess Gibbs function is defined as the difference between the Gibbs function for the solution and the Gibbs function for the solution assumed ideal

$$G^{\rm E} = G_{\rm real \, solution} - G_{\rm ideal \, solution} \tag{9}$$

These excess functions measure the deviation of a real from an ideal solution

$$G^{E} = \sum n_{i} \mu_{i} (\text{real}) - \sum n_{i} \mu_{i} (\text{ideal})$$
(10)

Employing eqn. (2) for the real and ideal solutions

$$G^{\rm E} = RT \sum x_i \ln \gamma_i \tag{11}$$

Knowing  $G^E$  values for different temperatures, it is possible to calculate the entropy and enthalpy excess functions

$$\left(\frac{\partial G^{\rm E}}{\partial T}\right)_{\rm p} = -S^{\rm E} \qquad H^{\rm E} = -T^2 \left( \left\{ \frac{\partial (G^{\rm E}/T)}{\partial T} \right\} \right)_{\rm p}$$
(12)

Finally, we can also determine the interaction solute-solvent parameter,  $\chi$ , from

$$G^{\rm E} = N\chi RT x_1 (1 - x_1) \tag{13}$$

where N is the total number of moles.

### DISCUSSION

Table 1 gives the values of the activity coefficient of solvent,  $\gamma_1$ , and solute,  $\gamma_2$ , as a function of molality and temperature. As can be seen, at the three temperatures studied the system shows a strong negative deviation from Raoult's law. This deviation increases with the molality of the system.

It is interesting to compare the behaviour of  $TLAH_2SO_4$  in solution with other salts of the same family. Thus, the osmotic coefficient,  $\Phi_2$ , was calculated at 25°C, for  $TLAH_2SO_4$  and for the trilaurylammonium chloride (TLAHCl), trilaurylammonium bromide (TLAHBr), trilaurylammonium iodide (TLAHI), trilaurylammonium nitrate (TLAHNO<sub>3</sub>) and trilaurylammonium perchlorate (TLAHClO<sub>4</sub>). As can be seen in Fig. 1, TLAH<sub>2</sub>SO<sub>4</sub> self-associates at very low concentrations and in a higher proportion than the other trilaurylamines. In these compounds the cation plays an important role in the thermodynamical behaviour in solution. Thus, it can be seen that as we go from TLAHCl to TLAH<sub>2</sub>SO<sub>4</sub> the deviation from ideality becomes greater.

This behaviour can be explained if we suppose that TLAH<sub>2</sub>SO<sub>4</sub> can form

Т	A	B	L	E	1

Values of  $\gamma_1$  and  $\gamma_2$  and their variation with the molality and temperature

$B_2 \times 10^2$ (mole kg <sup>-1</sup> )	$T = 25^{\circ}\mathrm{C}$		$T = 37^{\circ}\mathrm{C}$		$T = 50^{\circ} \mathrm{C}$	
	γ1	γ <sub>2</sub>	γ <sub>1</sub>	γ <sub>2</sub>	γ <sub>1</sub>	Ϋ2
2.253	0.99999	0.34751	1.00000	0.39333	1.00000	0.44707
3.072	0.99999	0.26719	0.99999	0.31067	0.99999	0.36338
4.209	0.99998	0.20256	0.99998	0.24138	0.99998	0.29016
4.667	0.99998	0.18581	0.99998	0.22282	0.99998	0.26988
5.904	0.99996	0.15630	0.99997	0.18908	0.99997	0.23193
6.780	0.99995	0.14440	0.99996	0.17478	0.99996	0.21519
8.323	0.99993	0.13325	0.99994	0.15977	0.99994	0.19763
9.741	0.99991	0.12794	0.99991	0.15283	0.99992	0.18844
10.602	0.99989	0.12481	0.99990	0.14867	0.999990	0.18383
11.023			0.99989	0.14638	0.99990	0.18145
12.477	0.99985	0.11317	0.99985	0.13554	0.99987	0.17098
12.951	0.99976	0.08907	0.99978	0.11044	0.99979	0.14707



Fig. 1. Osmotic coefficient,  $\Phi_2$ , as a function of the total concentration,  $B_{tot}$ , for different trilaurylammonium salts.

two hydrogen bonds.



These bonds are very strong as shown by the fact that they are stable even at  $50^{\circ}$ C. For the other salts, however, the self-association probably appears in the form



This interaction is weaker than the hydrogen bond.

On the other hand, as shown by Madariaga et al. [1], the predominant species in the phenomenon of self-association for the  $TLAH_2SO_4$ , at 25°C, is the trimer, while it is the dimer for the other salts. This fact, evidently, provokes a deviation from ideality. If we suppose that a third  $TLAH_2SO_4$  molecule incorporates with the dimer via dipole-dipole interaction, as shown in Fig. 2, it could be explained by considering that the bonds which stabilize the complex are of two different classes, dipole-dipole and hydrogen bonds. The former are more sensitive to temperature. This model could explain the results obtained by Madariaga et al. [1], who calculated the distribution of the different species as a function of temperature.

Another interesting application is to calculate the thermal variation of the activity coefficient of the solute. In Fig. 3  $(dln \gamma_2/dT)_p$  is plotted vs. molality,  $B_2$ . As the magnitude of B depends on the concentration of the



Fig. 2. Formation of a trimer molecule.



Fig. 3. Plot of (d ln  $\gamma_2/dT)_p$  as a function of the total concentration of TLAH<sub>2</sub>SO<sub>4</sub>.



Fig. 4. Excess functions  $S^{E}$ ,  $H^{E}$  and  $G^{E}$  as a function of solute molar fraction,  $x_{2}$ , at 298 K.

solution, the extrapolation of  $B_2$  to zero gives the standard partial molar enthalpy,  $h_2^{\infty}$ . The value of  $h_2^{\infty}$  was found to be -2.66 kJ mole<sup>-1</sup>. It is possible to calculate the excess Gibbs free energy,  $G^E$ , from eqn. (11).



Fig. 5. Excess functions,  $S^{E}$ ,  $H^{E}$  and  $G^{E}$  as a function of solute molar fraction,  $x_{2}$ , at 310 K.

If we know  $G^{E}$  values for different temperatures, the entropy and enthalpy excess functions can be obtained. Figures 4-6 give the values of  $G^{E}$ ,  $TS^{E}$ and  $H^{E}$  for all temperatures studied. Negative values of  $G^{E}$  indicate that



Fig. 6. Excess functions  $S^{E}$ ,  $H^{E}$  and  $G^{E}$  as a function of solute molar fraction,  $x_{2}$ , at 323 K.

there is a great compatibility between solute and solvent. This compatibility can be quantitatively calculated from the solute-solvent interaction parameter,  $\chi$ , which can be obtained from eqn. (13). Figure 7 shows the variation of



Fig. 7. Variation of the excess Gibbs free energy,  $G^{E}$ , as a function of  $x_1x_2$ .

 $G^{\rm E}$  as a function of  $x_1x_2$ , at several temperatures. From the slopes of the three straight lines the values obtained were -0.28 (298 K), -0.26 (310 K) and -0.23 (323 K). This indicates that as the temperature increases, the interaction between TLAH<sub>2</sub>SO<sub>4</sub> and benzene becomes less favoured. This is logical because as temperature increases the proportion of solvated trimers existing in the system decreases, which confirms the model proposed previously.

The splitting of  $\chi$  into the enthalpy and entropy terms is given by  $\chi = \chi_H + \chi_S$ 

where

$$\chi_{H} = -T \left( \frac{\partial \chi}{\partial T} \right)_{B}$$
$$= -\frac{\partial (T\chi)}{\partial T}$$

Generally, the entropic term,  $\chi_s$ , is independent of temperature. However, as can be seen in Fig. 8, the variation of  $\chi_s$  with temperature is not linear, i.e.  $\chi_s$  depends on *T*. These results can be explained if we take into account



Fig. 8. Variation of  $\chi_s$  and  $\chi_H$  with temperature.

that at 323 K, the dimer predominates, and it supposes a decrease in the order of the system, and therefore an increase in the entropic contribution according to experimental observations (Fig. 8).

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