

THERMAL DECOMPOSITION KINETICS. XIII. EFFECT OF SAMPLE MASS ON THE THERMAL DECOMPOSITION KINETICS OF $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$ FROM ISOTHERMAL MASS-LOSS DATA

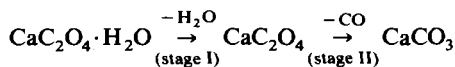
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ABSTRACT

The kinetic parameters for the first two stages of the thermal decomposition of calcium oxalate monohydrate



have been established from isothermal mass-change studies. For the decomposition of calcium oxalate to carbonate, the kinetic parameters are not appreciably affected by the sample mass in the ranges studied. For the dehydration of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$, they show a systematic decrease with increase in sample mass, and the curves of E or $\log A$ vs. sample mass can be best fitted as parabolae following an equation of the type

$$E(\text{ or } \log A) = \text{constant} - (\text{constant}) \times (\text{mass}) + (\text{constant}) \times (\text{mass})^2$$

SYMBOLS USED

- A = pre-exponential factor (s^{-1});
- α = fraction decomposed;
- E = energy of activation (kJ mol^{-1});
- m = sample mass (mg);
- n = order parameter;
- r = correlation coefficient;
- T = temperature (K).

INTRODUCTION

In an earlier publication [1], the kinetic parameters (E , A and n) for the dehydration of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$ and the decomposition of the resultant CaC_2O_4 to CaCO_3 and CO were evaluated from TG curves using three mechanism-non-invoking kinetic equations. The studies were carried out at seven different heating rates with a fixed sample mass and with seven different sample

masses at a fixed heating rate. It was observed that the kinetic parameters were not appreciably affected for the decomposition of CaC_2O_4 , whereas for the dehydration reaction, they showed a systematic decrease with increase in either heating rate or sample mass. Mathematical correlations of high reliability between the kinetic parameters and procedural factors were also evolved for the dehydration step.

Non-isothermal kinetic methods have always been a subject of controversy and criticism [2–5]. So, it was considered worthwhile to extend the studies on calcium oxalate monohydrate, using isothermal methods as well, to see whether the kinetic parameters obtained from isothermal methods are subject to the fluctuations and trends, observed in the case of the results from non-isothermal methods. In the non-isothermal experiments, seven different heating rates and seven different sample masses were used. Obviously, the only variable in isothermal experiments is the sample mass, and therefore, we have studied the effect of the seven sample masses on the isothermal kinetic parameters from the first two stages of the thermal decomposition of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$, carried out in a nitrogen atmosphere. Correlations between kinetic parameters and sample mass have been reported [6] from isothermal mass-loss studies of CaCO_3 . So, it is attempted here to evolve mathematical correlations between sample mass and kinetic parameters from this study.

EXPERIMENTAL

Sample

Calcium oxalate monohydrate powder of 99.9% purity and 5 μm average particle size from the same lot was used in the entire study.

Instruments

The isothermal mass-loss curves were recorded on a DuPont 990 thermal analyser (2 pen) in conjunction with a 951 thermogravimetric analyser. Computational work was done with an IBM-360 computer using a FORTRAN IV program.

Procedure

All the measurements were done in an atmosphere of dry nitrogen purged at a rate of $50 \text{ cm}^3 \text{ min}^{-1}$. The mass loss was recorded on the y -axis and the temperature on the y' -axis. The temperature was always steady for the entire span of the experiment, or at least the fluctuations were too small to be revealed on the recorder, which gave a perfect straight line.

The furnace was initially stabilised at the required temperature for about 30 min before introducing the sample. Even though the temperature programme was pre-set to a gap of 10 K for successive experiments, the actual sample temperature, as recorded by the thermocouple, sometimes rose above or dipped below the set point. The temperatures given in the tables in this communication are those recorded by the thermocouple.

As the set temperature was increased to higher values, it was observed that the sample underwent some reaction during the initial lag period, when it was raised to the furnace temperature. This is an inherent disadvantage of isothermal techniques [7]. So, the isothermal mass-loss curves could be recorded only at 4–6 different temperatures in the range 380–430 K for stage I, and 690–750 K for stage II. Mass suppression controls were used to expand the mass loss, recorded on the y -axis.

Time was recorded on the x -axis and the chart speed was adjusted to obtain an amplified recorder output for the two stages of decomposition. The initial time, t_0 , was noted by extrapolation to the zero mass-loss point on the y -axis. In each experiment, as soon as the dehydration reaction was over, the furnace temperature was raised to the value required for the stage II reaction, and the recording was continued until a well-defined plateau was obtained.

Seven sample masses (1.1, 2.5, 5.0, 7.5, 10, 15 and 20 mg) were employed in this study. Sample loading was done carefully to obtain the actual masses ± 0.1 mg of these nominal values. A total of 67 mass-loss curves were recorded for the two stages of decomposition (33 for stage I and 34 for stage II).

RESULTS AND DISCUSSION

The kinetic analysis of the mass-loss data was carried out with the general mechanism-non-invoking isothermal equation, the integral form of which can be given as

$$\frac{1 - (1 - \alpha)^{1-n}}{1 - n} = kt$$

In an earlier publication [1], the values of n were established as 0.65 for stage I and 0.50 for stage II. Using these values of n , the rate constants were calculated by plotting the left-hand side of the above equation against time, t . The values of the rate constants and the corresponding correlation coefficients at different temperatures and for different sample masses for the dehydration of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$ are given in Table 1. Similar values for the decomposition of the resultant CaC_2O_4 to CaCO_3 and CO are given in Table

TABLE 1

Rate constants at different temperatures and for different sample masses for dehydration of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$ (T in K and k in s^{-1})

| 1.1 mg | | | 2.5 mg | | |
|--------|-------------------------|--------|--------|-------------------------|--------|
| T | k | r | T | k | r |
| 383 | 0.1827×10^{-3} | 0.9995 | 403 | 0.8002×10^{-3} | 0.9986 |
| 393 | 0.4907×10^{-3} | 0.9777 | 412 | 0.2229×10^{-2} | 0.9975 |
| 402 | 0.1826×10^{-2} | 0.9917 | 423 | 0.7939×10^{-2} | 0.9885 |
| 412 | 0.4062×10^{-2} | 0.9851 | 433 | 0.1147×10^{-1} | 0.9820 |
| 418 | 0.7363×10^{-2} | 0.9830 | 437 | 0.2255×10^{-1} | 0.9863 |
| 5.0 mg | | | 7.5 mg | | |
| T | k | r | T | k | r |
| 381 | 0.1213×10^{-3} | 0.9929 | 388 | 0.1643×10^{-3} | 0.9994 |
| 389 | 0.2077×10^{-3} | 0.9960 | 402 | 0.5062×10^{-3} | 0.9961 |
| 399 | 0.8279×10^{-3} | 0.9936 | 417 | 0.1997×10^{-2} | 0.9920 |
| 408 | 0.1500×10^{-2} | 0.9884 | 424 | 0.2705×10^{-2} | 0.9881 |
| 420 | 0.3393×10^{-2} | 0.9916 | 434 | 0.7008×10^{-2} | 0.9873 |
| 10 mg | | | 15 mg | | |
| T | k | r | T | k | r |
| 391 | 0.2380×10^{-3} | 0.9934 | 392 | 0.1647×10^{-3} | 0.9998 |
| 413 | 0.1247×10^{-2} | 0.9958 | 412 | 0.6206×10^{-3} | 0.9977 |
| 423 | 0.2029×10^{-2} | 0.9928 | 422 | 0.1176×10^{-2} | 0.9948 |
| 430 | 0.3877×10^{-2} | 0.9901 | 442 | 0.3842×10^{-2} | 0.9866 |
| 20 mg | | | | | |
| T | k | r | | | |
| 392 | 0.2658×10^{-3} | 0.9938 | | | |
| 408 | 0.8933×10^{-3} | 0.9922 | | | |
| 412 | 0.7425×10^{-3} | 0.9974 | | | |
| 418 | 0.1182×10^{-2} | 0.9923 | | | |
| 431 | 0.2789×10^{-2} | 0.9924 | | | |

2. From these tables it can be seen that the correlation coefficients are close to unity in almost all cases, indicating near-perfect fits.

Using each set of values of T and k , given in Tables 1 and 2, linear plots of $\ln k$ vs. $1/T$ were drawn and E and A were calculated from the slope and intercept, respectively. The values of E and A along with the corresponding

correlation coefficients are given in Tables 3 and 4. Table 3 gives the kinetic parameters for different sample masses for the dehydration reaction and Table 4 gives similar values for the decomposition of CaC_2O_4 . The correlation coefficients are also near unity in these cases.

TABLE 2

Rate constants at different temperatures and for different sample masses, for decomposition of CaC_2O_4 (T in K and k in s^{-1})

| 1.1 mg | | | 2.5 mg | | |
|--------|-------------------------|--------|--------|-------------------------|--------|
| T | k | r | T | k | r |
| 693 | 0.1157×10^{-2} | 0.9991 | 694 | 0.3551×10^{-3} | 0.9955 |
| 701 | 0.2013×10^{-2} | 0.9989 | 706 | 0.4910×10^{-3} | 0.9971 |
| 708 | 0.2465×10^{-2} | 0.9989 | 716 | 0.9960×10^{-3} | 0.9975 |
| 722 | 0.5924×10^{-2} | 0.9873 | 725 | 0.2006×10^{-2} | 0.9991 |
| | | | 735 | 0.2622×10^{-2} | 0.9986 |
| | | | 750 | 0.5371×10^{-2} | 0.9997 |
| 5.0 mg | | | 7.5 mg | | |
| T | k | r | T | k | r |
| 695 | 0.2708×10^{-3} | 0.9967 | 690 | 0.1981×10^{-3} | 0.9997 |
| 706 | 0.5254×10^{-3} | 0.9995 | 701 | 0.4053×10^{-3} | 0.9993 |
| 713 | 0.6858×10^{-3} | 0.9998 | 710 | 0.6765×10^{-3} | 0.9992 |
| 725 | 0.1288×10^{-2} | 0.9996 | 721 | 0.1325×10^{-2} | 0.9995 |
| 736 | 0.2904×10^{-2} | 0.9997 | 731 | 0.2267×10^{-2} | 0.9994 |
| 750 | 0.4682×10^{-2} | 0.9984 | | | |
| 10 mg | | | 15 mg | | |
| T | k | r | T | k | r |
| 690 | 0.1615×10^{-3} | 0.9994 | 708 | 0.5844×10^{-3} | 0.9991 |
| 703 | 0.5249×10^{-3} | 0.9990 | 719 | 0.8969×10^{-3} | 0.9994 |
| 721 | 0.1153×10^{-2} | 0.9993 | 728 | 0.1562×10^{-2} | 0.9986 |
| 723 | 0.1114×10^{-2} | 0.9985 | 732 | 0.1787×10^{-2} | 0.9997 |
| | | | 744 | 0.2811×10^{-2} | 0.9984 |
| 20 mg | | | | | |
| T | k | r | | | |
| 703 | 0.3281×10^{-3} | 0.9967 | | | |
| 712 | 0.6139×10^{-3} | 0.9989 | | | |
| 722 | 0.1025×10^{-2} | 0.9990 | | | |
| 749 | 0.4757×10^{-2} | 0.9993 | | | |

TABLE 3

Kinetic parameters for different sample masses for dehydration of $\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$

| Sample mass (mg) | E (kJ mol^{-1}) | A (s^{-1}) | r |
|------------------|------------------------------|-------------------------|--------|
| 1.1 | 142.7 | 5.125×10^{15} | 0.9966 |
| 2.5 | 136.7 | 4.662×10^{14} | 0.9891 |
| 5.0 | 118.3 | 1.985×10^{12} | 0.9916 |
| 7.5 | 113.2 | 2.724×10^{11} | 0.9978 |
| 10.0 | 97.37 | 2.431×10^9 | 0.9972 |
| 15.0 | 90.78 | 2.035×10^8 | 1.0000 |
| 20.0 | 82.02 | 2.272×10^7 | 0.9826 |

E and A for stage II

From Table 4, it can be observed that the kinetic parameters for stage II are not appreciably affected by sample mass. The values of E and A are in the range 197–252 kJ mol^{-1} and 2×10^{11} to $2 \times 10^{15} \text{ s}^{-1}$, respectively. The variations are irregular in nature. It is interesting to note that these values are in the same range as those obtained in our non-isothermal studies [1].

E and A for stage I

From Table 3 it can be observed that the values of E and A for the dehydration reaction are strongly dependent on sample mass: they show a systematic decrease with increase in sample mass. Here again, the trend is similar to the one observed for non-isothermal kinetics [1].

Figure 1 shows the curves of E and $\log A$ vs. sample mass. Using a computer, different types of curve fittings (e.g., exponential, parabola and rectangular hyperbola) were worked out and it was found that the curves of

TABLE 4

Kinetic parameters for different sample masses for decomposition of CaC_2O_4

| Original sample mass (mg) | E (kJ mol^{-1}) | A (s^{-1}) | r |
|---------------------------|------------------------------|-------------------------|--------|
| 1.1 | 222.0 | 6.441×10^{13} | 0.9938 |
| 2.5 | 220.8 | 1.332×10^{13} | 0.9903 |
| 5.0 | 229.9 | 5.116×10^{13} | 0.9962 |
| 7.5 | 249.4 | 1.516×10^{15} | 0.9998 |
| 10.0 | 239.0 | 2.335×10^{14} | 0.9793 |
| 15.0 | 196.9 | 1.953×10^{11} | 0.9955 |
| 20.0 | 251.8 | 1.741×10^{15} | 0.9995 |

E or $\log A$ vs. sample mass could best be fitted as parabolae, using the following equations

$$E = 149.9 - 4.806 m + 0.1567 m^2$$

$$\log A = 16.69 - 0.9243 m + 0.02313 m^2$$

The reliability of these equations was assessed by the F test [8] and the Fisher constants for the two worked out to be 142.4 and 232.2, respectively, corresponding to a confidence level of above 99% in both cases. (The critical value of the Fisher constant [8] for the system at 99% confidence level is 18.) It is interesting to note that similar equations correlating kinetic parameters with sample mass were obtained in the case of the non-isothermal method also [1].

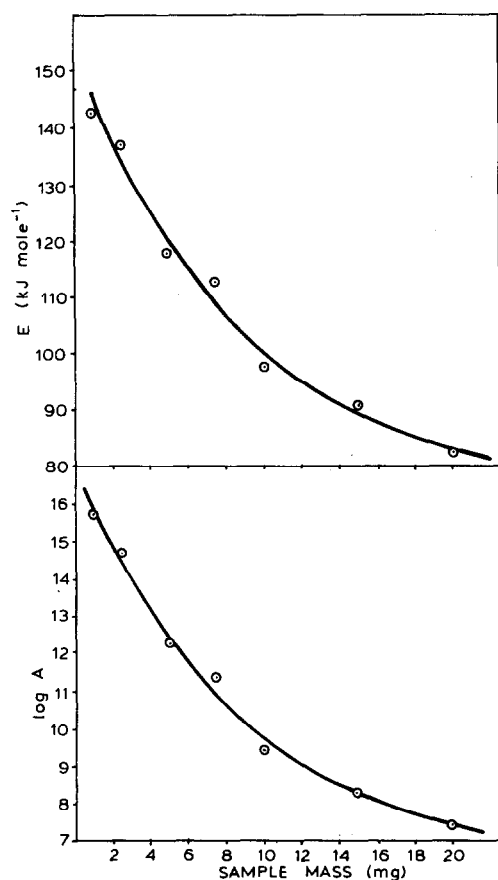


Fig. 1. Plots of $E/\log A$ vs. sample mass.

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