

## CHEMICAL THERMODYNAMIC PROPERTIES OF TOLUENE, *o*-, *m*- AND *p*-XYLENES

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### ABSTRACT

Employing recent molecular, spectroscopic and thermal constants, the ideal gas thermodynamic properties [ $C_p^0$ ,  $S^0$ ,  $H^0(T) - H^0(0)$ ,  $\Delta H_f^0$  and  $\Delta G_f^0$ ] of toluene, *o*-xylene, *m*-xylene and *p*-xylene in the temperature range 0–3000 K are calculated by the statistical mechanical method. A potential function, formed by summation of internal rotational energy levels, is used for evaluating the internal rotational contributions to the thermodynamic properties caused by the presence of each  $\text{CH}_3$  rotor in these molecules. The internal rotational energy levels for each rotor are calculated by solving the wave equation using the adopted internal rotational constant and potential function for the given rotor. The heat capacities and entropies obtained agree with the experimental values. The sources of molecular data and method of calculation are described in detail.

### INTRODUCTION

The thermodynamic properties of toluene (methylbenzene,  $\text{C}_7\text{H}_8$ ), *o*-xylene (1,2-dimethylbenzene,  $\text{C}_8\text{H}_{10}$ ), *m*-xylene (1,3-dimethylbenzene,  $\text{C}_8\text{H}_{10}$ ) and *p*-xylene (1,4-dimethylbenzene,  $\text{C}_8\text{H}_{10}$ ) in the ideal gaseous state have been calculated by Pitzer and Scott [1], Taylor et al. [2], Scott et al. [3] and Draeger and Scott [4] using the molecular constants then available. Recently, new data on molecular structure, vibrational assignments and internal rotation potential barrier heights for the  $\text{CH}_3$  rotor have been reported for these compounds. Therefore, we have employed the best values of the recent molecular, spectroscopic and thermal constants to recalculate the ideal gas thermodynamic properties of these alkyl benzenes. In these calculations, a standard statistical mechanical method based upon a rigid-rotor and a harmonic-oscillator molecular model was adopted.

For computing the contributions to the thermodynamic properties caused by internal rotation of the methyl groups ( $-\text{CH}_3$ ) in the molecules of the above compounds, we employed an internal rotation potential function formed by summation of internal rotational energy levels for each  $\text{CH}_3$  rotor. These energy levels were obtained from the solutions of the torsional wave-equation for a molecule with  $n$ -fold symmetry

$$\left[ -F \frac{\gamma^2}{\gamma \phi^2} + \frac{V_n}{2} (1 - \cos n\phi) \right] \psi(\phi) = E\psi(\phi) \quad (1)$$

where  $F$  = internal rotation constant for the given rotor,  $\phi$  = internal rotational angle,  $V_n$  = internal rotation barrier height and  $E$  = the required internal rotational energy levels. For the toluene molecule  $n = 6$  and for the other alkyl benzene molecules  $n = 3$ . The method suggested by Lewis et al. [5] was adopted for generating the internal rotational energy levels using eqn. (1).

Each xylene molecule has two methyl ( $-\text{CH}_3$ ) rotors. The two  $\text{CH}_3$  groups in the *o*-xylene molecule attach to two adjacent carbon atoms in the benzene ring. Because of steric effects, the internal rotation of these two rotors in this molecule is hindered, i.e., the potential barrier is high for each rotor. However, the two  $\text{CH}_3$  groups in the *m*- and *p*-xylene molecules are not so close to each other and consequently their potential barriers for internal rotation are much lower.

We estimated the  $\text{CH}_3$  barrier height of the *m*- and *p*-xylene molecules to be comparable to that of the toluene molecule. In the statistical mechanical calculations for the thermodynamic properties of the three isomeric xylenes we assumed that the two  $\text{CH}_3$  rotors are identical and independent; in other words, there was no interaction between these two rotors in each molecule. In all calculations the recent fundamental constants [6] and the 1975 Atomic Weights [7],  $C = 12.011$  and  $H = 1.0079$ , were employed.

## TOLUENE

The molecular structure of gaseous toluene was determined by electron diffraction by Keidel and Bauer [8]. Later, Rudolph et al. [9] investigated the microwave rotational spectrum of toluene in the region 8–23 GHz. They determined the rotational constants and derived the three principal moments of inertia as  $I_a = 88.23570 \text{ u}\text{\AA}^2$ ,  $I_b = 200.8198 \text{ u}\text{\AA}^2$  and  $I_c = 289.06118 \text{ u}\text{\AA}^2$ . From analysis of the spectral lines, they also obtained the internal rotation barrier height  $V_6 = (13.94 \pm 0.1) \text{ cal mol}^{-1}$  or  $(58.32 \pm 0.42) \text{ J mol}^{-1}$  for the  $\text{CH}_3$  rotor in this molecule. The internal rotation constant ( $F$ ) was reported to be  $166.72646 \text{ GHz}$  or  $5.561 \text{ cm}^{-1}$ . These values were adopted for

TABLE 1

Molecular constants for toluene, *o*-, *m*- and *p*-xylenes

	Toluene	<i>o</i> -Xylene	<i>m</i> -Xylene	<i>p</i> -Xylene
Molecular weight	92.1402	106.1670	106.1670	106.1670
Point group and total symmetry number	$C_{2v}$ , 6	$C_{2v}$ , 18	$C_{2v}$ , 18	$D_{2h}$ , 36
Ground-state configuration	$A_1$	$A_1$	$A_1$	$A_g$
Product of the three principal moments of inertia ( $\text{g}^3 \text{cm}^6$ )	$23446.4 \times 10^{-117}$	$66790.9 \times 10^{-117}$	$77362 \times 10^{-117}$	$66870 \times 10^{-117}$
Internal rotation of $\text{CH}_3$ rotor:				
Internal rotational constant, $F(\text{cm}^{-1})$	5.561	5.381	5.350	5.309
potential barrier height ( $\text{J mol}^{-1}$ )	$(58.32 \pm 0.42)$	6234	65.0	65.0
torsional wavenumber ( $0 \rightarrow 1$ ) ( $\text{cm}^{-1}$ )	51.28	162.0	48.21	47.85
Vibrational wavenumber ( $\text{cm}^{-1}$ )	3063, 3055, 3003, 2921, ... <sup>a</sup>	3080, 3062, 2950, 1680, ... <sup>a</sup>	3062, 3047, 3046, 2950, ... <sup>a</sup>	3050, 2950, 1616, 1578, ... <sup>a</sup>
Enthalpy of formation at 298.15 K ( $\text{kJ mol}^{-1}$ )	50.17	19.08	17.32	18.03

<sup>a</sup> See text for more information.

TABLE 2

Ideal gas thermodynamic properties

$T$ (K)	$C_p^0$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$S^0$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$H^0(T) - H^0(0)$ (J mol <sup>-1</sup> )	$\Delta H_f^0$ (kJ mol <sup>-1</sup> )	$\Delta G_f^0$ (kJ mol <sup>-1</sup> )
Toluene <sup>a</sup>					
0	0	0	0	73.22	73.22
50	38.10	220.3	1876.0	66.63	73.15
100	44.57	248.3	3917.0	64.01	80.66
150	56.00	268.4	6414.0	60.86	89.64
200	70.72	286.5	9570.0	57.30	99.79
273.15	96.06	312.2	15650.0	51.92	116.2
298.15	105.2	321.0	18170.0	50.17	122.2
300	105.8	321.6	18360.0	50.04	122.6
400	141.2	357.0	30740.0	43.56	147.8
500	171.7	391.9	46430.0	38.22	174.5
600	196.9	425.5	64910.0	33.93	202.2
700	217.6	457.5	85670.0	30.53	230.5
800	234.8	487.7	108300.0	27.89	259.3
900	249.3	516.2	132500.0	25.95	288.4
1000	261.6	543.1	158100.0	24.70	317.8
1100	272.0	568.6	184800.0	23.98	346.7
1200	281.0	592.6	212400.0	23.60	376.4
1300	288.7	615.4	240900.0	23.51	405.7
1400	295.4	637.1	270200.0	23.67	435.4
1500	301.1	657.6	300000.0	24.03	464.7
1750	312.5	705.0	376800.0	25.55	537.5
2000	320.7	747.2	456000.0	27.58	610.6
2250	326.7	785.4	536900.0	29.81	683.7
2500	331.3	820.1	619200.0	32.07	755.6
2750	334.8	851.8	702500.0	35.41	827.5
3000	337.5	881.0	786500.0	38.89	899.0
<i>o</i> -Xylene <sup>b</sup>					
0	0	0	0	46.43	46.43
50	40.58	220.7	1740.0	37.59	48.47
100	61.32	255.4	4302.0	34.37	60.60
150	78.99	283.7	7816.0	30.91	74.45
200	96.27	308.8	12200.0	27.05	89.56
273.15	122.9	342.7	20200.0	21.07	113.3
298.15	132.3	353.8	23390.0	19.08	121.9
300	133.0	354.6	23640.0	18.93	122.6
400	170.5	398.1	38820.0	11.32	158.3
500	204.3	439.8	57600.0	4.81	195.8
600	233.2	479.7	79520.0	-0.53	234.5
700	257.6	517.6	104100.0	-4.83	274.1
800	278.3	553.4	130900.0	-8.17	314.2
900	296.0	587.2	159700.0	-10.50	354.6
1000	311.1	619.2	190000.0	-12.16	395.5
1100	324.0	649.4	221800.0	-13.02	435.8

TABLE 2 (continued)

$T$ (K)	$C_p^0$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$S^0$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$H^0(T) - H^0(0)$ (J mol <sup>-1</sup> )	$\Delta H_f^0$ (kJ mol <sup>-1</sup> )	$\Delta G_f^0$ (kJ mol <sup>-1</sup> )
1200	335.2	678.1	254800.0	-13.41	477.0
1300	344.8	705.3	288800.0	-13.41	517.8
1400	353.0	731.2	323700.0	-13.07	559.0
1500	360.2	755.8	359400.0	-12.46	599.7
1750	374.3	812.5	451300.0	-10.07	701.0
2000	384.4	863.1	546200.0	-6.98	802.5
2250	391.8	908.9	643300.0	-3.60	903.8
2500	397.3	950.4	741900.0	-0.19	1004.0
2750	401.5	988.5	841800.0	4.46	1104.0
3000	404.7	1024.0	942600.0	9.23	1203.0
<i>m</i> -Xylene <sup>b</sup>					
0	0	0	0	45.94	45.94
50	43.30	234.9	2092.0	37.46	47.62
100	55.77	268.4	4541.0	34.12	59.06
150	71.14	293.8	7709.0	30.31	72.33
200	87.94	316.6	11680.0	26.04	87.00
273.15	115.7	348.0	19110.0	19.49	110.3
298.15	125.7	358.5	22120.0	17.32	118.8
300	126.5	359.3	22360.0	17.16	119.4
400	166.3	401.2	37010.0	9.02	154.8
500	201.8	442.2	55460.0	2.18	192.0
600	231.6	481.8	77180.0	-3.37	230.5
700	256.6	519.4	101600.0	-7.80	269.8
800	277.4	555.0	128400.0	-11.22	309.8
900	295.2	588.8	157000.0	-13.74	350.1
1000	310.3	620.7	187300.0	-15.37	390.8
1100	323.2	650.9	219000.0	-16.31	431.0
1200	334.3	679.5	251900.0	-16.78	472.0
1300	343.9	706.6	285800.0	-16.86	512.7
1400	352.1	732.4	320600.0	-16.62	553.7
1500	359.3	757.0	356200.0	-16.10	594.3
1750	373.3	813.5	447900.0	-13.96	695.4
2000	383.5	864.0	542600.0	-11.10	796.6
2250	391.0	909.6	639400.0	-7.94	897.7
2500	396.6	951.2	737900.0	-4.72	997.5
2750	400.9	989.2	837600.0	-0.22	1097.1
3000	404.3	1024.2	938300.0	4.43	1196.2
<i>p</i> -Xylene <sup>b</sup>					
0	0	0	0	46.76	46.76
50	44.67	229.2	2116.0	38.30	48.75
100	54.98	263.0	4582.0	34.98	60.46
150	69.79	288.0	7690.0	31.11	74.00
200	87.00	310.4	11600.0	26.78	88.97
273.15	115.7	341.7	18990.0	20.20	112.7
298.15	126.0	352.2	22010.0	18.03	121.4

TABLE 2 (continued)

$T$ (K)	$C_p^0$ ( $J K^{-1}$ $mol^{-1}$ )	$S^0$ ( $J K^{-1}$ $mol^{-1}$ )	$H^0(T) - H^0(0)$ ( $J mol^{-1}$ )	$\Delta H_f^0$ ( $kJ mol^{-1}$ )	$\Delta G_f^0$ ( $kJ mol^{-1}$ )
300	126.8	353.0	22250.0	17.87	122.0
400	167.4	395.1	36980.0	9.81	158.0
500	203.3	436.5	55570.0	3.11	195.8
600	233.2	476.2	77440.0	-2.28	234.9
700	258.1	514.1	102000.0	-6.56	274.8
800	278.9	550.0	128900.0	-9.84	315.2
900	296.4	583.9	157700.0	-12.22	356.0
1000	311.4	615.9	188100.0	-13.74	397.2
1100	324.2	646.2	219900.0	-14.57	437.9
1200	335.2	674.9	252900.0	-14.95	479.4
1300	344.7	702.1	286900.0	-14.95	520.5
1400	352.8	728.0	321800.0	-14.63	562.0
1500	359.9	752.5	357400.0	-14.05	603.0
1750	373.8	809.1	449300.0	-11.76	705.2
2000	383.9	859.7	544000.0	-8.79	807.5
2250	391.3	905.4	641000.0	-5.54	909.7
2500	396.9	946.9	739500.0	-2.24	1011.0
2750	401.2	985.0	839300.0	2.33	1111.0
3000	404.6	1020.0	940100.0	7.06	1211.0

<sup>a</sup>  $7 C(c, \text{graphite}) + 4 H_2(g) = C_7H_8(g)$ .

<sup>b</sup>  $8 C(c, \text{graphite}) + 5 H_2(g) = C_8H_{10}(g)$ .

calculating the rotational and internal rotational contributions to the thermodynamic properties of gaseous toluene.

It is interesting to note that to obtain calculated heat capacities of gaseous toluene consistent with experimental values, Pitzer and Scott [1] found that the internal rotation of the methyl group in the molecule was relatively free, i.e.,  $V_6 = 500 \text{ cal mol}^{-1}$ . Taylor et al. [2] selected  $V_6 = 750 \text{ cal mol}^{-1}$  and Kovner [19] adopted  $V_6 = 873 \text{ cal mol}^{-1}$  as an empirical parameter for the potential barrier, on the basis of the entropy and heat capacity data. Scott et al. [3] treated the  $CH_3$  group as a free rotor for calculation of the ideal gas thermodynamic properties of toluene by the statistical mechanical method. We adopted the experimental value  $V_6 = 13.94 \text{ cal mol}^{-1}$  [9] for the statistical calculations.

The vibrational spectra of toluene have been observed by numerous researchers [10–17]. Based upon the reported Raman and IR spectra, Pitzer and Scott [1] and Scott et al. [3] made a complete set of vibrational assignments for toluene. Recently, Sverdlov et al. [18] analyzed the reported spectral data and assigned the complete fundamental vibrational frequencies

for gaseous toluene. We adopted their values for evaluating the vibrational contributions to thermodynamic properties of this compound, because the use of their frequencies yielded  $C_p^0$  and  $S^0$  in better agreement with the experimental values.

Table 1 lists the molecular constants which we employ for calculating the heat capacity ( $C_p^0$ ), entropy ( $S^0$ ), enthalpy ( $H^0(T) - H^0(0)$ ), enthalpy of formation ( $\Delta H_f^0$ ) and Gibbs energy of formation ( $\Delta G_f^0$ ) in the temperature range 0–3000 K and at atmospheric pressure (101.325 kPa) for gaseous toluene. The results appear in Table 2.

A value of  $\Delta H_f^0(\text{g}, 298.15 \text{ K}) = 50.17 \text{ kJ mol}^{-1}$  [20–22] was selected for calculation of the  $\Delta H_f^0$  and  $\Delta G_f^0$  at the given temperatures. The required auxiliary data on  $H^0(T) - H^0(0)$  and  $(G^0(T) - H^0(0))/T$  for the elements C (graphite) and gaseous  $\text{H}_2$  were taken from the TRC Hydrocarbon Project Tables [22].

#### *o*-XYLENE

Rudolph et al. [23] measured the microwave ground-state spectra of this compound and determined its molecular structure. They reported the three principal moments of inertia as  $I_a = 2.65245 \times 10^{-38} \text{ g cm}^2$ ,  $I_b = 3.90320 \times 10^{-38} \text{ g cm}^2$  and  $I_c = 6.45133 \times 10^{-38} \text{ g cm}^2$ . This was the only source of data on the molecular structure of *o*-xylene. Their results were adopted for calculating  $I_a I_b I_c$  in this work.

Based upon the observed vibrational spectra, Pitzer and Scott [1] assigned a complete set of fundamental vibrational frequencies for gaseous *o*-xylene. Kovner and Bogomolov [25] and Bogomolov [26] calculated the fundamental frequencies theoretically for the *o*-xylene molecule, to interpret its vibrational spectrum. For computing the vibrational contributions to thermodynamic properties of gaseous *o*-xylene, we selected the vibrational assignments of Pitzer and Scott [1] as the best values.

Determination of the internal rotation barrier height of the two  $\text{CH}_3$  rotors in the *o*-xylene molecule has occupied researchers for many years. From the low-temperature heat capacity measurements, Wulff [27] evaluated the value  $V_3 = (1850 \pm 75) \text{ cal mol}^{-1}$ . Haupt and Muller-Warmuth [28] studied the temperature dependence of the proton-spin relaxation times of crystalline *o*-xylene at low temperatures and derived  $V_3 = (2200 \pm 100) \text{ cal mol}^{-1}$  for the  $\text{CH}_3$  rotor.

By inelastic neutron scattering and using a two-dimensional Fourier series to describe the potential energy interactions of the two methyl groups, Livingston et al. [29] obtained  $V_3 = (2400 \pm 130) \text{ cal mol}^{-1}$  and  $V_{33} = (-540 \pm 80) \text{ cal mol}^{-1}$  for the  $\text{CH}_3$  top in crystalline *o*-xylene. The potential function they employed was  $V(\phi_1, \phi_2) = V_3 (1 - \cos 3\phi_1) + V_3 (1 - \cos 3\phi_2) + V_{33} (1 - \cos 3\phi_1 \cos 3\phi_2) + V_{33} (1 - \sin 3\phi_1 \sin 3\phi_2)$ .

Pitzer and Scott [1] chose  $V_3 = 2000 \text{ cal mol}^{-1}$  for producing the calculated  $C_p^0$  and  $S^0$  of gaseous *o*-xylene consistent with the third-law entropy at 298.15 K and the vapor heat capacity measurements in the temperature range 393–463 K. Taylor et al. [2] selected the value  $2100 \text{ cal mol}^{-1}$  for  $V_3$ . Rush [30] reported  $V_3 = (1.96 \pm 0.14) \text{ kcal mol}^{-1}$  for this compound. Ingham and Strickler [31] investigated the UV absorption spectrum of *o*-xylene and assigned a barrier of internal rotation of  $(700 \pm 50) \text{ cm}^{-1}$  or  $(2.00 \pm 0.14) \text{ kcal mol}^{-1}$  in the ground state assuming the two  $\text{CH}_3$  groups in the molecule were independent oscillators.

Rudolph et al. [23] derived  $V_3 = (1490 \pm 50) \text{ cal mol}^{-1}$  or  $(6.234 \pm 0.209) \text{ kJ mol}^{-1}$  for the  $\text{CH}_3$  rotor of the *o*-xylene molecule, neglecting the top-top coupling and the higher than three-fold barrier terms. They determined the reduced moment of inertia ( $I_r$ ) and internal rotational constant ( $F$ ) of the  $\text{CH}_3$  rotor as  $5.203 \times 10^{-40} \text{ g cm}^2$  and  $5.381 \text{ cm}^{-1}$ , respectively. Their results were the best values and were adopted. Based upon the adopted  $F$  and  $V_3$ , we generated 108 internal rotational energy levels ( $0\text{--}15\,300 \text{ cm}^{-1}$ ) for each of the two  $\text{CH}_3$  rotors, which were used to calculate the internal rotational contributions to the thermodynamic properties of this compound. We calculated the  $\text{CH}_3$  torsional frequency ( $0 \rightarrow 1$ ) to be  $162 \text{ cm}^{-1}$  which agreed with the value  $162 \pm 5 \text{ cm}^{-1}$  observed from the far IR spectrum of gaseous *o*-xylene by Pardoe et al. [24].

The enthalpy of formation at 298.15 K, as given in Table 1, was derived from the enthalpy of combustion of liquid *o*-xylene determined by Prosen et al. [20] and the enthalpy of vaporization measured by Osborne and Ginnings [21]. The calculated results are listed in Table 2.

### *m*-XYLENE

The molecular structure of *m*-xylene has never been determined experimentally. Based upon an estimated molecular structure, Pitzer and Scott [1] calculated the three principal moments of inertia and the reduced moment of the  $\text{CH}_3$  rotor of the molecule as  $I_a = 2.61 \times 10^{-38} \text{ g cm}^2$ ,  $I_b = 3.88 \times 10^{-38} \text{ g cm}^2$ ,  $I_c = 6.39 \times 10^{-38} \text{ g cm}^2$ , and  $I_r = 5.23 \times 10^{-40} \text{ g cm}^2$ , respectively. These values were adopted tentatively in this work.

For evaluation of the internal rotational contributions of the two  $\text{CH}_3$  rotors in the *m*-xylene molecule to the thermodynamic properties of this substance, we employed  $F = 5.35 \text{ cm}^{-1}$ , which was derived from the adopted  $I_r$ , and  $V_3 = 65 \text{ J mol}^{-1}$  [32] for generating 108 internal rotational energy levels for each rotor.

To produce the calculated  $C_p^0$  and  $S^0$  for gaseous *m*-xylene in agreement with the experimental values, Pitzer and Scott [1] selected  $V_3 = 500 \text{ cal mol}^{-1}$  and Taylor et al. [2] chose  $V_3 = 750 \text{ cal mol}^{-1}$ . Using recent molecular constants for statistical calculations, we found that a value of  $V_3 = 65 \text{ J}$



TABLE 3

Comparison of experimental and calculated  $C_p^0$  and  $S^0$  (1 cal = 4.184 J)

$T$ (K)	$C_p^0/(\text{cal K}^{-1} \text{mol}^{-1})$			$S^0/(\text{cal K}^{-1} \text{mol}^{-1})$		
	Expt.	Calc.	$\Delta$	Expt.	Calc.	$\Delta$
<b>Toluene</b>						
298.15				$76.77 \pm 0.15^a$	76.72	-0.05
341.27				$80.39 \pm 0.15^a$	80.36	-0.03
361.06				$82.04 \pm 0.15^a$	82.04	0.00
371.20	$31.09^a$	31.40	0.31			
383.77				$83.92 \pm 0.15^a$	83.96	0.04
390	$33.5^b$	32.94	-0.56			
393	$32.8 \pm 0.3^c$	33.18	0.38			
396.20	$33.19^a$	33.44	0.25			
410	$35.0^b$	34.53	-0.47			
410.11				$86.08 \pm 0.15^a$	86.16	0.08
427.20	$35.65^a$	35.86	0.21			
428	$35.7 \pm 0.4^c$	35.92	0.22			
462.20	$38.32^a$	38.44	0.12			
463	$38.0 \pm 0.4^{c*}$	38.50	0.50			
500.20	$40.98^a$	41.06	0.08			
<b><i>o</i>-Xylene</b>						
298.15				$84.50 \pm 0.3^c$	84.57	0.07
393	$40.2 \pm 0.4^c$	40.13	-0.07			
428	$43.5 \pm 0.4^c$	43.12	-0.38			
463	$46.0 \pm 0.5^c$	45.98	-0.02			
<b><i>m</i>-Xylene</b>						
298.15				$85.60 \pm 0.3^c$	85.69	0.09
393	$39.1 \pm 0.4^c$	39.10	0.00			
428	$42.4 \pm 0.4^c$	42.25	-0.15			
463	$45.4 \pm 0.4^c$	45.24	-0.16			
<b><i>p</i>-Xylene</b>						
298.15				$84.27 \pm 0.3^c$	84.19	-0.08
393	$39.0 \pm 0.4^c$	39.37	0.37			
398.15	$39.80^d$	39.85	0.05			
423.15	$42.02^d$	42.13	0.11			
428	$42.6 \pm 0.4^c$	42.56	-0.04			
448.15	$44.31^d$	44.33	0.02			
463	$45.2 \pm 0.4^c$	45.59	0.39			
473.15	$46.41^d$	46.43	0.02			
498.15	$48.50^d$	48.44	-0.06			
523.15	$50.45^d$	50.37	-0.08			

<sup>a</sup> Ref. 3.<sup>b</sup> Ref. 38.<sup>c</sup> Ref. 1.<sup>d</sup> Ref. 4.

$\text{mol}^{-1}$  provided  $C_p^0$  and  $S^0$  values in better agreement with the experimental data, as shown in Table 3.

The vibrational assignments of Pitzer and Scott [1] were adopted for calculating the vibrational contributions to the thermodynamic properties of this substance. Fundamental frequencies and characteristic vibrations of *m*-xylene were calculated by Kovner and Bogomolov [33] and Bogomolov [35], respectively, using the force constants of the benzene ring [34].

Prosen et al. [20] measured the enthalpy of combustion of liquid *m*-xylene. The enthalpy of vaporization of this compound was determined by Osborne and Ginnings [21]. From their results we calculated the value  $\Delta H_f(\text{g}, 298.15 \text{ K}) = 17.32 \text{ kJ mol}^{-1}$ , as indicated in Table 1, for computing the  $\Delta H_f^0$  and  $\Delta G_f^0$  at the given temperatures. The calculated ideal gas thermodynamic properties for *m*-xylene are presented in Table 2.

#### *p*-XYLENE

The thermodynamic properties of gaseous *p*-xylene have been reported by Pitzer and Scott [1] and Taylor et al. [2]. Recently, Draeger and Scott [4] employed new molecular data and recalculated the thermodynamic properties of this compound. In their recent calculations, Draeger and Scott assumed that the two methyl groups in the *p*-xylene molecule were free rotors and utilized a semi-empirical method [36,37] for estimating the anharmonicity corrections such that the calculated thermodynamic functions like  $C_p^0$  and  $S^0$  agreed with the experimental values.

As mentioned previously, we considered that the two  $\text{CH}_3$  groups in the *p*-xylene molecule were not free rotors and that the potential barrier to internal rotation of each rotor was similar to the internal rotation potential barrier of the  $\text{CH}_3$  rotor in the toluene molecule. We employed  $V_3 = 65.0 \text{ J mol}^{-1}$  and  $F = 5.309 \text{ cm}^{-1}$  [3] for generating 180 internal rotational energy levels for each  $\text{CH}_3$  rotor, which were used for evaluation of the internal rotational contributions to thermodynamic properties of gaseous *p*-xylene.

The molecular structure of gaseous *p*-xylene has not been thoroughly investigated. The product of the three principal moments of inertia and the fundamental vibrational assignments reported by Draeger and Scott [4] were adopted for calculating the rotational and vibrational contributions to thermodynamic properties of gaseous *p*-xylene, respectively. To produce  $C_p^0$  and  $S^0$  of *p*-xylene in better agreement with the experimentally measured vapor heat capacity and third-law entropy values, we changed two vibrational wavenumbers from 972 and  $700 \text{ cm}^{-1}$  to 936 and  $680 \text{ cm}^{-1}$ , respectively. The calculated thermodynamic properties appear in Table 2.

## DISCUSSION

The statistically calculated heat capacities and entropies of gaseous toluene, *o*-, *m*- and *p*-xylenes are compared with the experimental data in Table 3. The agreement in  $C_p^0$  and  $S^0$  between the calculated and experimental values indicates that our selected molecular constants and method of calculation are appropriate and reasonable.

In calculation of ideal gas thermodynamic properties of toluene and *p*-xylene, Scott et al. [3] and Draeger and Scott [4] employed a molecular model in which the methyl groups in these two molecules were treated as free rotors. They adopted a semi-empirical method for evaluation of the anharmonicity corrections to make the statistically calculated  $C_p^0$  and  $S^0$  agree with the experimental values. In our statistical mechanical calculations we treated the methyl groups in the alkyl benzene molecules as hindered rotors. For evaluation of internal rotational contributions to thermodynamic properties we adopted an internal rotation partition function formed by summation of internal rotational energy levels.

Due to the difference in the method of calculation, there are some differences in our calculated property values and those reported by Scott and his coworkers. For example, the  $C_p$  of *p*-xylene was reported to be  $316.1 \text{ J K}^{-1} \text{ mol}^{-1}$  at 1000 K by Draeger and Scott [4] while our value is  $311.4 \text{ J K}^{-1} \text{ mol}^{-1}$ . The values reported by Pitzer and Scott [1] and Taylor et al. [2] were 310.0 and  $309.7 \text{ J K}^{-1} \text{ mol}^{-1}$ , respectively. The  $C_p^0$  of *p*-xylene at 1000 K is estimated to be  $311.7 \text{ J K}^{-1} \text{ mol}^{-1}$  using the methylene increment method, which is based upon the following formula:  $C_p^0(p\text{-xylene, g, 1000 K}) = C_p^0(\text{toluene, g, 1000 K}) + [C_p^0(\text{toluene, g, 1000 K}) - C_p^0(\text{benzene, g, 1000 K})]$ , where  $C_p^0(\text{benzene, g, 1000 K}) = 211.41 \text{ J K}^{-1} \text{ mol}^{-1}$ .

Because of the approximations involved in our molecular model for calculating the thermodynamic properties of these four alkyl benzenes, the property values evaluated at high temperatures, e.g., above 1000 K, may not be as accurate as those calculated at lower temperatures; however, they are still useful for approximate calculations.

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