

## TOPOLOGICAL ASPECTS OF THE EFFECT OF TEMPERATURE AND PRESSURE ON THE THERMODYNAMICS OF BINARY MIXTURES OF NON-ELECTROLYTES

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### ABSTRACT

An approach, employing the concept of molecular connectivity index of the third degree of graph theory, has been developed to evaluate molar excess enthalpy,  $H^E(T_1, x)$ , and molar excess volume  $V^E(T_1, x)$  of any kind of binary mixture (liquid as well as gaseous) of non-electrolytes, and the calculated  $H^E(T_1, x)$  or  $V^E(T_1, x)$  values agree well with their corresponding experimental values. This approach has also been extended to study the effect of temperature and pressure on  $H^E(T_1, x)$  and  $V^E(T_1, x)$  data of any kind of binary mixture of non-electrolytes, and the calculated  $H^E(T_2, x, P = 1 \text{ atm})$ ,  $H^E(T_2, x, P_2 \neq 1 \text{ atm})$ ,  $V^E(T_2, x, P_2 = 1 \text{ atm})$  and  $V^E(T_2, x, P_2 \neq 1 \text{ atm})$  values, obtained from  $H^E(T_1, x, P = 1 \text{ atm})$  or  $V^E(T_1, x, P = 1 \text{ atm})$  data, compare well with their corresponding experimental values. The approach has further been utilized to evaluate specific volumes  $v(T_1, x, P_2 \gg 1 \text{ atm})$  of pure compounds as well as their mixtures when  $v(T_1, P = 1 \text{ atm})$  or  $v(T_1, x, P = 1 \text{ atm})$  data are available; the calculated  $v(T_1, x)$  and  $v(T_1, x, P_2)$  values again compare well (within 5% at the worst) with their corresponding experimental values.

### INTRODUCTION

Although the thermodynamics of binary mixtures of non-electrolytes have attracted the attention of physical chemists for a considerable time [1-18], no satisfactory approach (theoretical or empirical) is available until now to evaluate reasonably well such thermodynamic properties as the molar excess enthalpy,  $H^E(T_1, x, P = 1 \text{ atm})$ , or the molar excess volume,  $V^E(T_1, x, P = 1 \text{ atm})$ , or to study the effect of temperature and pressure on  $H^E(T_1, x, P = 1 \text{ atm})$  or  $V^E(T_1, x, P = 1 \text{ atm})$  data of all kinds (liquid, associated or otherwise, or gaseous) of binary mixtures of non-electrolytes.

The situation is all the more acute for those binary mixtures where either one or both the components are associated or when their components undergo specific interactions between themselves; and while all the earlier attempts [11-19] for the latter class of binary mixtures have been concerned with evaluating equilibrium constants of the molecular complexation reaction and the enthalpy of formation of various postulated molecular species

in the complexation reaction, no approach is available to (a) analyze  $H^E(T_1, x, P = 1 \text{ atm})$  and  $V^E(T_1, x, P = 1 \text{ atm})$  data, and (b) study the effect of temperature or/and pressure on  $H^E(T_1, x, P = 1 \text{ atm})$  and  $V^E(T_1, x, P = 1 \text{ atm})$  data for the former class of binary mixtures. Singh et al. [20,21] have recently utilized the concept of molecular connectivity index of the third degree of graph theory to evaluate  $H^E(T_1, x, P = 1 \text{ atm})$  and  $V^E(T_1, x, P = 1 \text{ atm})$  data of those binary mixtures of non-electrolytes that are not characterized by specific interactions between their components. However, this approach would fail to differentiate  $H^E$  or  $V^E$  data at  $T_1$  of, for example,  $[(1-x) \text{ benzene} + x \text{ } n\text{-pentane}]$  from  $[(1-x) \text{ cyclohexane} + x \text{ } n\text{-pentane}]$ , or  $[(1-x) \text{ benzene} + x \text{ } n\text{-pentane}]$  from  $[(1-x) \text{ benzene} + x \text{ pent-1-ene}]$  mixtures. Further, this approach (henceforth called molecular connectivity approach) would not be conducive to evaluate  $H^E$  and/or  $V^E$  data of binary mixtures that contain hetero atoms in their molecular graph. Again no approach is available to evaluate specific volumes under high pressures,  $v(T_1, x, P \gg 1 \text{ atm})$ , of binary mixtures of non-electrolytes when  $v(T_1, x, P = 1 \text{ atm})$  data are available. The present work is concerned with (i) the evaluation of  $H^E(T_1, x, P = 1 \text{ atm})$  and  $V^E(T_1, x, P = 1 \text{ atm})$  data, (ii) the study of the effect of  $T$  and  $P$  on  $H^E(T_1, x, P = 1 \text{ atm})$  and  $V^E(T_1, x, P = 1 \text{ atm})$  data, and (iii) the evaluation of  $v(T_1, x, P \gg 1 \text{ atm})$  of all kinds of binary mixtures of non-electrolytes.

## CONCEPTUAL ASPECT OF THE APPROACH AND THE RESULTS

According to the mathematical discipline of graph theory [22–24] the molecular graph of, for example,  $n$ -pentane, symbolizing its C–C skeleton, would be



in which while the vertices at positions 2, 3 and 4 are of the degree two (reflecting the number of adjacent carbon atoms in its molecular graph), those at positions 1 and 5 are of the degree one. In order to further quantify the information contained in the molecular graph of a molecule, Kier et al. [25–29] suggested the use of molecular connectivity index,  $\xi$ , of the first, second and third degree of the molecule, defined by

$${}^1\xi = \sum_{l < m} (\delta_l \delta_m)^{-0.5} \quad (1)$$

$${}^2\xi = \sum_{l < m} \sum_{m < n} (\delta_l \delta_m \delta_n)^{-0.5} \quad (2)$$

$${}^3\xi = \sum_{l < m} \sum_{m < n} \sum_{n < o} (\delta_l \delta_m \delta_n \delta_o)^{-0.5} \quad (3)$$

where  $\delta_l$ ,  $\delta_m$  and  $\delta_n$  etc., denote the degrees of the  $l$ th,  $m$ th and  $n$ th etc., vertices of its molecular graph. Thus the  ${}^1\xi$ ,  ${}^2\xi$ ,  ${}^3\xi$  connectivity indices of

*n*-pentane would be

$${}^1\xi = 2.414 \quad (4)$$

$${}^2\xi = 1.354 \quad (5)$$

$${}^3\xi = 0.707 \quad (6)$$

Such a scheme of evaluating the molecular connectivity index,  $\xi$ , of a molecule utilizing only the degrees of the various vertices of the C–C skeleton of a molecule would fail to differentiate *n*-pentane from pent-1-ene or benzene from cyclohexane. Moreover, it would also be not conducive to quantify the information contained in the molecular graph of such molecules as alkanols, ethers, esters, pyridine, etc. In order to overcome this problem, Kier [30] advocated the use of  $\delta^v$  values reflecting explicitly the valency of the atoms forming the bonds ( $\delta^v = \text{valence } \delta$ ) to evaluate  ${}^1\xi$ , etc., indices of the molecular graph of a molecule. According to Kier [30],  $\delta^v$  of carbon in any C–H linkage should be evaluated from

$$\delta^v(\text{C}) = Z - h \quad (7)$$

where  $Z$  is the maximum valency of C (i.e. 4), and  $h$  is the number of hydrogen atoms linked to the carbon atom. Thus  $\delta^v$  of C in  $-\text{CH}_2$ ,  $-\text{CH}_3$  or  $-\text{CH}$  would be

$$\begin{aligned} \delta^v(\text{C}) \quad \text{in } -\text{CH}_2 &= 4 - 2 = 2 \\ &\text{in } -\text{CH}_3 &= 4 - 3 = 1 \\ &\text{in } -\text{CH} &= 4 - 1 = 3 \end{aligned}$$

and so the  ${}^1\xi$ ,  ${}^2\xi$  and  ${}^3\xi$  indices of *n*-pentane and pent-1-ene would be



*n*-pentane                      pent-1 ene

$${}^1\xi = 2.414 \quad {}^1\xi = 2.024$$

$${}^2\xi = 1.354 \quad {}^2\xi = 1.077$$

$${}^3\xi = 0.707 \quad {}^3\xi = 0.493$$

which now clearly differentiate them. For molecules containing heteroatoms like N and O, Kier [31] further suggested that  $\delta^v$  of N or O should also be evaluated from eqn. (7) where  $Z$  now denotes the maximum valency of N or O and  $h$  is the number of hydrogen atoms linked to N or O. Accordingly,  $\delta^v$  (N) in the  $-\text{NH}$  fragment of a molecule would be  $5 - 1 = 4$ . Similarly

$$\delta^v(\text{O}) \text{ in } \text{R}-\text{OH} = 6 - 1 = 5$$

and

$$\delta^v(\text{O}) \text{ in } \begin{array}{c} \text{R} \\ \diagup \\ \text{C}=\text{O} \\ \diagdown \\ \text{R} \end{array} = 6 - 0 = 6$$

It would thus be possible to quantify the information contained in the molecular graph of any kind of molecule.

Further, since the  $^1\xi$  index of a molecule depends on the degrees of the closest vertices of its molecular graph taken two at a time, it has been taken [20] to represent a measure of the oscillations of its bond length. On the other hand, while the  $^1\xi$  index of a molecule provides no information [32] about the effect of branching in a molecule, the  $^2\xi$  index of a molecule encodes some information [32] about the effect of branching in a molecule. According to Kier [33], more information about the effect of branching in a molecule is obtainable by computing its  $^3\xi$  index and it has actually been shown [20] that while an increase in branching in an isomeric compound increases its molar volume, its  $^3\xi$  index decreases. In other words, the molar volumes of isomeric compounds vary inversely as their  $^3\xi$ . Again,  $^{1/3}\xi$  of most of the molecules is less than unity, and as branching in an isomeric compound would allow only a part of this surface area to interact effectively with the corresponding surface areas of other molecules,  $^{1/3}\xi$  of a molecule has been taken [20] to represent a measure of the probability that its surface area interacts effectively with the surface areas of other molecules. If now the molar excess enthalpy,  $H^E$ , of a ( $x$  A +  $(1-x)$  B) mixture at  $T_1$  is due essentially to the replacement of like contacts in pure A and B by unlike contacts in the mixture, then it has been shown [21] that the molar excess enthalpy at  $T_1$ ,  $H^E(T_1, x)$ , of an [ $x$  A +  $(1-x)$  B] mixture is given by

$$H^E(T_1, x) = \frac{x(1-x)\chi_{AB}k_{AB}({}^3\xi_A/{}^3\xi_B)}{x + (1-x)k_{AB}({}^3\xi_A/{}^3\xi_B)} \quad (8)$$

where all the symbols have their usual meaning [20,21]. Equation (8) has been shown to describe very well  $H^E$  data of a very large number of binary mixtures of non-electrolytes that are not characterized by the presence of any specific interactions between their components, if  $H^E$  data for the mixture at two compositions close to  $x=0.5$  are known. This earlier approach [20,21], however, suggests that  $H^E$  for [ $x$ ] cyclohexane +  $(1-x)$   $n$ -pentane] and [ $x$  cyclohexane +  $(1-x)$  pent-1-ene] would be the same. However, this is not true. Moreover, this approach is also not conducive to evaluate  $H^E$  for binary mixtures in which either one or both the components contain hetero atoms in their molecular graph since their  $^3\xi$  index cannot be evaluated. If the  $^3\xi$  indices of molecules are evaluated by employing the  $\delta^v$  values, it appears that eqn. (8) should be able to describe  $H^E$  data of any class of binary mixtures of non-electrolytes if  $H^E$  data for the mixture at two compositions close to  $x=0.5$  are available. Such  $H^E$  values for a number of binary mixtures at  $x=0.3$  and  $0.7$  are recorded in Table 1 and are also compared with their corresponding experimental values [34–84].

Examination of Table 1 clearly shows that the  $H^E$  values calculated from eqn. (8) compare very well their corresponding experimental values even for

those mixtures which are known to be characterized by specific interactions between their components or when one of the components is associated. This would then mean that  $H^E$  of an  $[x A + (1 - x) B]$  mixture is due essentially to the interaction energy per contact,  $\chi_{AB}$ . Consequently, as the temperature is raised from  $T_1$  to  $T_2$ , the molecules A and B in this mixture at  $T_2$  would be able to interact less effectively compared to the case at  $T_1$ . This would then suggest that as the temperature is raised  $\chi_{AB}$  decreases or  $H^E$  for a binary mixture should decrease with the rise in temperature, and so if  $H^E(T_1, x)$  and  $H^E(T_2, x)$  denote the  $H^E$  of a binary mixture at  $T_1$  and  $T_2$  K, respectively, then

$$\frac{H^E(T_2, x)}{H^E(T_1, x)} = \frac{T_1}{T_2} \quad (9)$$

or

$$H^E(T_2, x) = \frac{T_1}{T_2} H^E(T_1, x) \quad (10)$$

Thus if  $H^E(T_1, x)$  data of a binary mixture at  $T_1$  are known or could be evaluated from eqn. (8) in the manner described earlier, it should be possible to evaluate  $H^E(T_2, x)$  for any class of binary mixture at  $T_2$ . Such  $H^E(T_2, x = 0.3, 0.7)$  data for some of the various binary mixtures listed in Table 1 are recorded in Table 2 and are also compared with their corresponding experimental values [34,35,37,38,58,59,62,64,65,68,75-77,79,83-85].

Examination of Table 2 again reveals that the  $H^E(T_2, x)$  data for the various binary mixtures evaluated from eqn (10) utilizing  $H^E(T_1, x = 0.3, 0.7)$  data evaluated from eqn. (8), compare very well with their corresponding experimental values even for those mixtures where one of the components is associated or where the components are known to undergo specific interactions. Table 2 also shows that expression (10) well describes the  $H^E(T_2, x = 0.3, 0.7, P = 101.3 \text{ k Pa})$  data [83-85] of even gaseous mixtures.

#### EFFECT OF PRESSURE ALONE ON THE $H^E(T_2, x, P = 1 \text{ ATM})$ DATA OF GASEOUS MIXTURES

When a binary gaseous mixture  $[x A + (1 - x) B]$  at  $T_2$  and  $P_2$  is subjected to an increase of pressure from  $P_2$  to  $P_2^1$ , the increased pressure would cause the gaseous components to interact more effectively at  $T_2$  and  $P_2^1$  as compared to that at  $T_2$  and  $P_2$ . This would then mean that as pressure on a mixture at a given  $T_2$  is increased, the interaction energy per unlike contact,  $\chi_{AB}$ , increases and so should its  $H^E(T_2, x, P_2^1)$ . Accordingly, if  $H^E(T_2, x, P_2^1)$  and  $H^E(T_2, x, P_2)$  denote the molar excess enthalpy of a binary mixture at  $P_2^1$  and  $P_2$  and at a given temperature  $T_2$ , then

$$H^E(T_2, x, P_2^1) \propto P_2^1 \quad (11)$$

TABLE I

Comparison of  $H^E$  ( $T_1, x$ ) values as calculated from eqn. (8) with their corresponding experimental values at  $x = 0.3, 0.7$  for various mixtures

Mixture	$T_1$	${}^3\xi_A$	${}^3\xi_B$	$\chi_{AB}$ (J mole $^{-1}$ )	$k_{AB}$	$x$	$H^E$ (J mole $^{-1}$ )		Ref.
							Calcd.	Exptl.	
<i>(a) Liquid mixtures</i>									
1. $x$ Methylene chloride + (1 - $x$ ) 2-propanone	273.15	1.0	1.0	-3312.9	1.2711	0.3	-743.3	-760.2	34
2. $x$ Methylene chloride (1 - $x$ ) methyl ethanoate	303.15	1.0	0.287	-2980.9	0.3311	0.3	-817.8	-820.5	35
3. $x$ Methylene chloride + (1 - $x$ ) oxane	303.15	1.0	1.076	-5123.1	1.2711	0.3	-652.0	-675.2	36
4. $x$ Methylene chloride + (1 - $x$ ) 1,4-dioxane	303.15	1.0	0.744	-3360.0	1.309	0.3	-1026	-1050	37
5. $x$ Chloroform + (1 - $x$ ) 1,4-dioxane	303.15	1.0	0.744	-5520.2	1.929	0.3	-967	-898	38
6. $x$ Chloroform + (1 - $x$ ) diethylether	298.15	1.0	0.408	-10422.9	0.444	0.3	-810.6	-795.0	39
7. $x$ Chloroform + (1 - $x$ ) pyridine	308.15	1.0	0.566	-5958.2	1.036	0.3	-1011.1	-965.0	40
8. $x$ Chloroform + (1 - $x$ ) $\alpha$ -picoline	308.15	1.0	0.814	-9165.5	1.342	0.3	-1421.1	-1423.2	41
9. $x$ Chloroform + (1 - $x$ ) $\gamma$ -picoline	308.15	1.0	0.847	-8102.3	1.384	0.3	-2033.8	-1990.5	42
10. $x$ Chloroform + (1 - $x$ ) di- <i>tert</i> -butyl ether	298.15	1.0	0.612	-5756.7	0.666	0.3	-2243.4	-2108.0	43
11. $x$ Chloroform + (1 - $x$ ) di-isopentyl ether	298.15	1.0	1.158	-5384.3	1.306	0.3	-2321.0	-2129.0	44
12. $x$ Carbon tetrachloride + (1 - $x$ ) diethyl ether	298.15	1.0	0.408	-2013.9	0.408	0.3	-1448	-1444	45
						0.7	-1833	-1859	46
						0.7	-2182	-2180	47
						0.7	-2657	-2540	48
						0.3	-1926	-1796	49
						0.7	-2336	-2180	50
						0.3	-1239	-1250	51
						0.7	-1282	-1254	52
						0.3	-1171	-1130	53
						0.7	-1229	-1240	54
						0.3	-422.9	-396.0	55
						0.7	-422.9	-400.6	56

13. x Carbon tetrachloride + (1 - x) oxane	303.15	1.0	1.076	-3286.5	0.856	0.3	-640.7	-645.1	44
14. x Carbon tetrachloride + (1 - x) di-isopentyl ether	298.15	1.0	1.158	-530.6	1.172	0.3	-584.8	-564.2	41
15. x Carbon tetrachloride + (1 - x) di.tert.butyl ether	298.15	1.0	0.612	199.8	0.902	0.3	-111.8	-118.0	41
						0.7	-112.4	-120.0	
						0.3	46.4	46.0	41
						0.7	54.1	56.0	
16. x Carbon tetrachloride + (1 - x) tetrahydrofuran	298.15	1.0	0.827	-2670	1.195	0.3	-617.9	-618.9	45
17. x Carbon tetrachloride + (1 - x) 1,3-dioxolane	298.15	1.0	0.539	-848.2	0.2846	0.3	-714.8	-707.2	45
18. x Carbon tetrachloride + (1 - x) oxane	298.15	1.0	1.076	-2658.9	1.1014	0.3	140.4	143.7	45
19. x Carbon tetrachloride + (1 - x) 1,3-dioxane	298.15	1.0	0.889	-248.7	22.464	0.3	109.6	111.1	45
20. x Ethane + (1 - x) ethanol (P = 6900 kPa)	298.15	1.0	1.0	-793.2	0.655	0.3	-627.0	-633.6	45
21. x Ethane + (1 - x) propan-1-ol (P = 6900 kPa)	298.15	1.0	1.0	-938.4	1.140	0.3	-585.9	-588.5	45
22. x Ethane + (1 - x) + butan-1-ol (P = 6900 kPa)	298.15	1.0	0.512	-972.2	0.809	0.3	-145.9	-135.3	45
23. x Ethane + (1 - x) pentan-1-ol (P = 6900 kPa)	298.15	1.0	0.762	-982.8	1.602	0.3	-73.0	-64.5	46
24. x Ethane + (1 - x) hexane-1-ol (P = 6900 kPa)	298.15	1.0	1.012	-942.3	2.842	0.3	-143.8	-132.4	46
25. x Ethane + (1 - x) octane-1-ol (P = 6900 kPa)	298.15	1.0	1.512	-740.3	21.29	0.3	-121.7	-192.8	46
26. x Ethane + (1 - x) decan-1-ol (P = 6900 kPa)	298.15	1.0	2.012	-531.2	-13.312	0.3	-204.6	-204.0	46
27. x Trimethylene oxide + (1 - x) benzene	298.15	0.577	0.667	-1471.4	1.426	0.3	-215.6	-192.8	46
28. x Methyl ethanoate + (1 - x) methanol	298.15	0.287	1.0	3356.1	5.258	0.3	-229.4	-227.6	46
						0.7	-274.8	-260.8	46
						0.3	-244.9	-244.3	46
						0.7	-326.0	-326.8	46
						0.3	-245.3	-250.0	46
						0.7	-360.2	-376.4	46
						0.3	-215.5	-217.6	46
						0.7	-444.6	-433.8	46
						0.3	-170.5	-165.7	46
						0.7	-574.4	-454.5	47
						0.3	-327.6	-316.0	47
						0.7	-356.2	-350.0	47
						0.3	784.2	790.2	48
						0.7	922.7	950.0	48

TABLE 1 (continued)

Mixture	$T_1$	${}^3\xi_A$	${}^3\xi_B$	$X_{AB}$ (J mole <sup>-1</sup> )	$k_{AB}$	$x$	$H^E$ (J mole <sup>-1</sup> )		Ref.
							Calcd.	Exptl.	
29. <i>x</i> Methyl ethanoate + (1 - <i>x</i> ) ethanol	298.15	0.287	1.0	4560.9	4.729	0.3	1034.4	1057.4	49
30. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) methanol	298.15	0.348	1.0	2880.3	5.129	0.7	1171.1	1233.5	50
31. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) ethanol	298.15	0.348	1.0	4444.8	3.903	0.7	832.2	891.0	51
32. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) propan-1-ol	298.15	0.348	1.0	5423.0	3.608	0.3	1213.0	1227.0	52
33. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) butan-1-ol	298.15	0.348	0.512	6104.6	1.749	0.7	1328.0	1365.0	53
34. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) <i>n</i> -hexane	298.15	0.348	0.957	5684.9	2.254	0.3	1346.0	1361.0	54
35. <i>x</i> Ethyl ethanoate + (1 - <i>x</i> ) cyclohexane	298.15	0.348	1.50	6495.8	2.862	0.7	1443.0	1485.0	55
36. <i>x</i> Butan-1-ol + (1 - <i>x</i> ) methanol	298.15	0.512	1.0	973.2	0.808	0.3	1120.0	1160.0	56
37. <i>x</i> Tetrahydrofuran + (1 - <i>x</i> ) benzene	298.15	0.827	0.667	-122.64	1.1781	0.7	1007.0	1048.0	45
38. <i>x</i> 1,3-Dioxane + (1 - <i>x</i> ) benzene	298.15	0.889	0.667	574.2	0.781	0.3	143.4	142.8	57
39. <i>x</i> 1,4-Dioxane + (1 - <i>x</i> ) benzene	298.15	0.744	0.667	-253.9	-0.180	0.7	102.6	105.0	58
40. <i>x</i> 1,4-Dioxane + (1 - <i>x</i> ) cyclohexane	298.15	0.744	1.5	6992.0	1.692	0.3	-175.6	-185.2	45
41. <i>x</i> Oxane + (1 - <i>x</i> ) benzene	298.15	1.076	0.667	-937.71	0.8837	0.7	-284.5	-296.1	59
							-330.5	-316.5	60
							-122.0	-117.0	
							-124.0	-117.0	
							-67.1	-48.3	
							-16.7	-5.1	
							1388	1398	
							1295	1320	
							-216.3	-205.9	
							-248.9	-217.1	



42. x	Butan-1-ol + (1 - x) ethanol	298.15	0.512	1.0	270.0	1.082	0.3	45.7	45.1	61
							0.7	36.3	36.4	
43. x	Butan-1-ol + (1 - x) propan-1-ol	298.15	0.512	1.0	15.2	4.888	0.3	3.9	4.8	61
							0.7	5.5	4.3	
44. x	Pyridine + (1 - x) benzene	298.15	0.566	0.667	92.12	0.2541	0.3	9.3	8.0	62
							0.7	5.5	5.4	
45. x	Pyridine + (1 - x) <i>N</i> -methyl piperidine	298.15	0.566	1.580	3029.5	2.030	0.3	571.7	551.0	63
							0.5041	633.0	634.0	
							0.7	503.6	501.0	
46. x	Piperidine + (1 - x) benzene	298.15	1.132	0.667	2001.4	0.6504	0.3	432.5	434.0	64
							0.4996	525.0	524.0	
							0.7	449.8	417.0	
47. x	Piperidine + (1 - x) toluene	298.15	1.132	0.940	2161.6	0.742	0.3	438.2	400.0	65
							0.5038	509.7	516.0	
							0.7	418.9	439.0	
48. x	Piperidine + (1 - x) cyclohexane	298.15	1.132	1.500	4298.8	0.828	0.3	765.1	777.0	66
							0.496	822.0	824.0	
							0.7	636.0	689.0	
49. x	Piperidine + (1 - x) methyl cyclohexane	298.15	1.132	1.894	4415.2	1.044	0.3	785.4	765.0	67
							0.4935	850.9	853.0	
							0.7	652.4	665.0	
50. x	Aniline + (1 - x) benzene	293.15	0.799	0.667	4890.8	0.472	0.3	834.6	807.7	68
							0.7	541.6	596.0	
51. x	Aniline + (1 - x) toluene	293.15	0.799	0.940	5126.9	0.7915	0.3	939.6	941.5	67
							0.7	803.2	813.7	
52. x	Aniline + (1 - x) <i>o</i> -xylene	293.15	0.799	1.426	6234.0	1.084	0.3	1096.2	1085.3	68
							0.7	900.9	872.9	
53. x	Aniline + (1 - x) <i>m</i> -xylene	293.15	0.799	1.174	6245.1	1.081	0.3	1183.6	1200.7	68
							0.7	1047.3	1102.1	
54. x	1-Hexanol + (1 - x) methanol	298.15	1.012	1.0	2133.3	0.281	0.3	255.3	256.0	69
							0.7	162.2	170.0	
55. x	1-Hexanol + (1 - x) ethanol	298.15	1.012	1.0	760.4	0.492	0.3	122.6	124.0	70
							0.7	93.6	96.1	

TABLE I (continued)

Mixture	$T_1$	${}^3\xi_A$	${}^3\xi_B$	$\chi_{AB}$ (J mole <sup>-1</sup> )	$k_{AB}$	$x$	$H^E$ (J mole <sup>-1</sup> )		Ref.
							Calcd.	Exptl.	
56. $x$ 1-Hexanol + (1 - $x$ ) propanol-1-ol	298.15	1.012	1.0	287.0	0.741	0.3	54.8	56.8	71
57. $x$ 1-Hexanol + (1 - $x$ ) butan-1-ol	298.15	1.012	0.512	135.4	0.3356	0.3	48.2	52.0	61
58. $x$ Methyl benzoate + (1 - $x$ ) <i>n</i> -hexane	298.15	1.136	0.957	6466.7	0.6124	0.3	24.7	24.2	61
59. $x$ Octane-1-ol + (1 - $x$ ) methanol	298.15	1.512	1.0	3691.8	0.148	0.7	21.0	21.5	72
60. $x$ Octan-1-ol + (1 - $x$ ) ethanol	298.15	1.512	1.0	1512.46	0.267	0.3	1220.5	7230.1	72
61. $x$ 2-Methyl pyridine + (1 - $x$ ) hexafluorobenzene	318.15	0.814	0.667	-5048.2	0.219	0.3	1075.2	1080.3	73
62. $x$ <i>N</i> -Methyl piperidine + (1 - $x$ ) benzene	298.15	1.580	0.667	1114.0	0.2225	0.3	378.0	375.2	73
63. $x$ <i>N</i> -Methyl piperidine + (1 - $x$ ) cyclohexane	298.15	1.580	1.500	689.6	0.766	0.7	226.2	224.3	61
64. $x$ <i>N</i> -Methyl piperidine + (1 - $x$ ) toluene	298.15	1.580	0.940	205.0	0.5666	0.7	156.2	156.0	74
65. $x$ 3,5-Dimethylpyridine + (1 - $x$ ) hexafluorobenzene	318.15	0.788	0.667	-4460.4	0.2477	0.3	-581.6	-556.9	74
66. $x$ Di- <i>n</i> -Butylether + (1 - $x$ ) benzene	298.15	0.931	0.667	2260.3	0.2824	0.3	-363.1	-340.8	75
67. $x$ Ethyl benzoate + (1 - $x$ ) <i>n</i> -hexane	298.15	1.213	0.957	5781.6	0.486	0.3	184.3	180.0	75
68. $x$ Ethyl benzoate + (1 - $x$ ) benzene	298.15	1.217	0.667	408.7	0.057	0.7	192.1	193.0	75
69. $x$ Octan-1-ol + (1 - $x$ ) methanol	298.15	1.512	1.0	3691.8	0.148	0.7	143.7	129.0	76
						0.5012	135.1	121.0	76
						0.7	124.1	117.0	77
						0.3	42.4	36.0	77
						0.7	41.6	35.0	78
						0.3	-543.0	-525.0	78
						0.7	-347.9	-289.4	79
						0.3	324.9	326.2	79
						0.7	228.7	226.7	80
						0.3	1023	1035	80
						0.7	846	862	81
						0.3	23.9	27.4	81
						0.7	12.2	6.0	81
						0.3	378.0	375.2	81
						0.7	226.2	224.3	81

70. x Octan-1-ol+(1-x) ethanol	318.15	1.512	1.0	1512.5	0.267	0.3	220.1	220.0	61
71. x Octan-1-ol+(1-x) propan-1-ol	298.15	1.512	1.0	776.4	0.4324	0.3	156.2	156.0	61
72. x Octan-1-ol+(1-x) butan-1-ol	298.15	1.512	0.512	482.9	0.2553	0.3	140.7	141.2	61
						0.7	119.0	125.6	
73. x Octan-1-ol+(1-x) hexanol	318.15	1.512	1.012	92.4	2.862	0.3	92.4	92.8	61
						0.7	85.5	84.7	
74. x Decan-1-ol+(1-x) methanol	318.15	2.012	1.0	4153.8	0.1176	0.3	20.8	22.1	61
						0.7	23.0	21.2	
75. x Decan-1-ol+(1-x) ethanol	318.15	2.012	1.0	1507.9	0.2015	0.3	443.3	452.0	70
						0.7	267.7	254.2	
76. x Decan-1-ol+(1-x) propan-1-ol	298.15	2.012	1.0	1284.8	0.321	0.3	219.9	217.0	70
						0.7	156.3	156.0	
77. x Decan-1-ol+(1-x) butan-1-ol	298.15	2.012	0.512	910.2	0.2012	0.3	231.7	233.8	70
						0.7	195.0	192.2	
78. x Decan-1-ol+(1-x) hexan-1-ol	318.15	2.012	1.012	415.8	0.4283	0.3	177.1	180.2	61
						0.7	161.3	166.0	
79. x Decan-1-ol+(1-x) octan-1-ol	318.15	2.012	1.512	89.54	0.7728	0.3	83.1	85.2	71
						0.7	77.8	78.4	
80. x Tri- <i>n</i> -butylamine + (1-x) benzene	303.15	2.168	0.667	5418.4	0.1233	0.3	19.5	19.2	61
						0.7	19.0	18.2	
(b) Gaseous mixtures						0.3	785.5	800.9	82
81. x Water(g)+(1-x) nitrogen(g)	373.15	1.0	1.0	179.5	1.507	0.5	555.9	590.1	
82. x Water(g)+(1-x) <i>n</i> -heptane (v)	373.15	1.0	1.207	649.5	1.2936	0.5	54.0	53.5	83
						0.610	53.7	50.7	
$P = 101.325$ kPa						0.587	168.1	169.6	83
83. x 2-Propanone(g)+(1-x) chloroform (v)	323.3	1.0	1.0	-2013.5	0.1315	0.392	164.0	169.9	
						0.570	-133.7	-123.8	84
$P = 44$ kPa						0.625	-103.6	-107.0	
$P = 101.3$ kPa						0.350	-92.0	-113.6	84
						0.474	-99.5	-103.0	
						0.675	-112.8	-112.6	
							-105.1	-97.9	

TABLE 2

Comparison of  $H^E(T_2, x)$  values [evaluated from  $H^E(T_1, x)$  values by means of eqn. (10)] with their corresponding experimental values for various mixtures

Mixture	$T_1$ (K)	$T_2$ (K)	$x$	$H^E(T_2, x)$ (J mole <sup>-1</sup> )		Ref.					
				Calcd.	Exptl.						
<i>(a) Liquid mixtures</i>											
1. $x$ Methylene chloride + (1 - $x$ ) 2-propanone	273.15	288.15	0.3	-704.6	-727.2	34					
			0.7	-775.2	-783.2						
			303.15	318.15	0.3	-669.7	-735.5	34			
					0.7	-736.9	-740.4				
					318.15	318.15	0.3	-638.2	-700.3	34	
							0.7	-702.1	-747.2		
2. $x$ Methylene chloride + (1 - $x$ ) methyl ethanoate	303.15	318.15	0.3	-621.3	-624.6	35					
			0.7	-657.8	-647.5						
3. $x$ Methylene chloride + (1 - $x$ ) 1,4-dioxane	303.15	318.15	0.3	-772.4	-760.5	37					
			0.7	-963.4	-945.3						
4. $x$ Chloroform + (1 - $x$ ) 1,4-dioxane	303.15	318.15	0.3	-1354.1	-1360.2	38					
			0.7	-1937.9	-1863.3						
5. $x$ 1,4-Dioxane + (1 - $x$ ) benzene	298.15	288.15	0.3	-69.4	-57.5	58					
			0.7	-17.3	-6.9						
6. $x$ 1,4-Dioxane + (1 - $x$ ) cyclohexane	298.15	288.15	0.3	1436.6	1360	59					
			0.7	1339.0	1345						
			318.15	318.15	0.3	1301.0	1280	59			
					0.7	1213.0	1260				
					333.15	333.15	0.3	1243.0	1220	59	
							0.7	1159.0	1220		
					7. $x$ Aniline + (1 - $x$ ) benzene	293.15	298.15	0.3	820.5	743.4	68
								0.7	532.5	573.7	
303.15	303.15	0.3	807.1	701.7				68			
		0.7	523.7	551.2							
		308.15	308.15	0.3				794.0	678.0	68	
				0.7				515.2	499.5		
8. $x$ Aniline + (1 - $x$ ) toluene	293.15	298.15	0.3	923.8	935.3	68					
			0.7	789.7	781.4						
			303.15	303.15	0.3	908.6	866.1	68			
					0.7	776.7	726.8				
					308.15	308.15	0.3	893.9	820.0	68	
							0.7	764.1	675.4		
9. $x$ Aniline + (1 - $x$ ) <i>o</i> -xylene	293.15	298.15	0.3	1077.8	1034.2	68					
			0.7	885.8	838.6						
			303.15	303.15	0.3	1060.0	942.2	68			
					0.7	871.2	759.6				
					308.15	308.15	0.3	1042.8	859.5	68	
							0.7	857.0	720.0		

TABLE 2 (continued)

Mixture	$T_1$ (K)	$T_2$ (K)	$x$	$H^E(T_2, x)$ (J mole <sup>-1</sup> )		Ref.	
				Calcd.	Exptl.		
10. $x$ Aniline + (1 - $x$ ) $m$ -xylene	293.15	298.15	0.3	1163.8	1149.3	68	
			0.7	1029.7	967.4		
		303.15	0.3	1144.6	1081.4	68	
			0.7	1012.8	956.7		
			0.3	1126.0	1008.2		68
0.7	996.0	840.3					
11. $x$ Pyridine + (1 - $x$ ) benzene	298.15	313.15	0.3	8.9	25.5	62	
			0.7	5.2	17.0		
		333.15	0.3	8.3	47.3	62	
			0.7	4.9	32.0		
12. $x$ Piperidine + (1 - $x$ ) benzene	298.15	283.15	0.4996	552.8	608.0	64	
13. $x$ Piperidine + (1 - $x$ ) toluene	298.15	283.15	0.5038	536.8	590.0	65	
14. $x$ $N$ -Methyl piperidine + (1 - $x$ ) cyclohexane	298.15	283.15	0.5215	161.0	161.0	76	
15. $x$ $N$ -Methyl piperidine + (1 - $x$ ) benzene	298.15	283.15	0.5012	202.2	205.0	75	
16. $x$ $N$ -Methyl piperidine + (1 - $x$ ) toluene	298.15	283.15	0.5038	536.8	590.0	77	
17. $x$ Di- $n$ -butylether + (1 - $x$ ) benzene	298.15	308.15	0.3	314.4	309.8	79	
			0.7	221.3	217.8		
<i>(b) Gaseous mixtures</i>							
18. $x$ Water + (1 - $x$ ) nitrogen $P = 101.325$ kPa	373.15	380.15	0.5	53.0	48.4	83	
		390.15	0.5	51.6	42.9		
		400.15	0.5	50.4	38.0		
		410.15	0.5	49.1	34.9		
		423.15	0.5	47.6	30.6		
19. $x$ Water + (1 - $x$ ) $n$ -heptane $P = 101.325$ kPa	373.15	398.15	0.5	157.5	132.6	83	
		423.15	0.5	148.2	105.6		
20. $x$ 2-Propanone + (1 - $x$ ) chloroform $P = 101.325$ kPa	353.3	363.2	0.35	-96.5	-81.2	84	
			0.675	-101.9	-81.4		
		373.2	0.35	-93.9	-64.3	84	
			0.675	-99.2	-62.5		
		343.2, $P = 101.3$ kPa	343.2, $P = 35.0$ kPa	0.474	-40.1	-47.2	84
				0.474	-52.8	-64.5	
	343.2, $P = 46.1$ kPa	0.474	-77.0	-95.1			
	343.2, $P = 67.2$ kPa						

TABLE 2 (continued)

Mixture	$T_1$ (K)	$T_2$ (K)	$x$	$H^E(T_2, x)$ (J mole <sup>-1</sup> )		Ref.
				Calcd.	Exptl.	
		343.2, $P = 88.5$ kPa	0.474	-101.4	-126.7	
		343.2, $P = 104.5$ kPa	0.474	-119.8	-150.4	
	338.2, $P = 101.3$ kPa	323.3, $P = 43.1$ kPa	0.474	-54.7	-120.2	84
		327.8, $P = 60.8$ kPa	0.474	-75.1	-90.6	
		338.2, $P = 87.8$ kPa	0.474	-102.1	-139.4	

and

$$H^E(T_2, x, P_2) \propto P_2 \quad (12)$$

or

$$H^E(T_2, x, P_2^1) = \frac{P_2^1}{P_2} H^E(T_2, x, P_2) \quad (13)$$

Thus, if the  $H^E(T_2, x, P_2)$  data of a gaseous mixture are known or can be evaluated from eqn. (10) utilizing the  $H^E(T_1, x, P_2)$  data computed from eqn. (8) in the manner described above, it should be possible to evaluate  $H^E(T_2, x, P_2^1)$  data for the gaseous mixture at any pressure  $P_2^1$ .

Doyle et al. [84] have recently made measurements on the molar excess enthalpy of a gaseous [ $x$  acetone +  $(1 - x)$  chloroform] mixture as a function of temperature and pressure, and it would be interesting to see how eqn. (13) describes the  $H^E(T_2, x, P_2^1)$  data of this gaseous mixture. For this purpose,  $H^E(T_1 = 353.2 \text{ K}, x = 0.474, P_2 = 101.3 \text{ kPa})$  data for this mixture were first evaluated from eqn. (8) utilizing  $H^E(T_1 = 353.2, P_2 = 101.3 \text{ kPa})$  data at two compositions. Such  $H^E(T_1 = 353.2 \text{ K}, x = 0.474, P_2 = 101.3 \text{ kPa})$  data were next utilized to estimate  $H^E(T_2 = 343.2 \text{ and } 338.2 \text{ K}, x = 0.474, P_2 = 101.3 \text{ kPa})$  values by means of eqn. (10) which was then employed to evaluate  $H^E(T_2 = 343.2 \text{ and } 338.2 \text{ K}, x = 0.474, P_2^1 = 35.0, 46.1, 67.2, 88.5, \text{ and } 104.5 \text{ kPa})$  for this mixture. Such  $H^E(T_2, x, P_2^1)$  values for this mixture are recorded in Table 2 and are also compared with their corresponding experimental values [84]; the calculated  $H^E(T_2, x = 0.474, P_2^1)$  data compare reasonably well with their corresponding experimental values [84].

EFFECT OF TEMPERATURE AND PRESSURE ON THE  $H^E$  DATA OF A GASEOUS MIXTURE

If  $H^E(T_1, x, P_2)$  data for a gaseous mixture are known, then from eqns. (10) and (13),  $H^E(T_2, x, P_2^1)$  data for the mixture can be readily evaluated from

$$H^E(T_2, x, P_2^1) = \frac{P_2^1}{P_2} \cdot \frac{T_1}{T_2} H^E(T_1, x, P_2) \quad (14)$$

In order to check eqn. (14),  $H^E(T_1 = 353.2 \text{ K}, x = 0.474, P_2 = 101.3 \text{ kPa})$  data for a gaseous [ $x$  acetone +  $(1 - x)$  chloroform] mixture evaluated from eqn. (8) were employed to evaluate  $H^E(T_2 = 327.8 \text{ K}, x = 0.474, P_2^1 = 60.8 \text{ kPa})$  and  $H^E(T_2 = 323.3 \text{ K}, x = 0.474, P_2^1 = 43.1 \text{ kPa})$ . Such  $H^E(T_2, x, P_2^1)$  values for an [ $x$  acetone +  $(1 - x)$  chloroform] mixture are recorded in Table 2 and are also compared with their corresponding experimental values [84]; and bearing in mind the overall simplicity of this approach these compare well with each other.

Further, in view of the use of  $\delta^v$  to evaluate the  ${}^3\xi$  molecular connectivity index of a molecule, it appears that it should also be possible to evaluate  $V^E$  data for any kind of binary mixtures of non-electrolytes. It has already been shown [20] that the molar volume,  $V$ , for a wide range of non-electrolytes is well described by

$$V = \alpha/{}^3\xi + \beta({}^1\xi) + \gamma \quad (15)$$

where  $\alpha$ ,  $\beta$  and  $\gamma$  are constants. Consequently, for a binary [ $x$  A +  $(1 - x)$  B] mixture while

$$V_A = \alpha_A/{}^3\xi_A + \beta_A({}^1\xi_A) + \gamma_A \quad (16)$$

$$V_B = \alpha_B/{}^3\xi_B + \beta_B({}^1\xi_B) + \gamma_B \quad (17)$$

the ideal molar volume for the mixture would be given by

$$V_m(\text{id}) = xV_A + (1 - x)V_B \quad (18)$$

$$= x[\alpha_A/{}^3\xi_A + \beta_A({}^1\xi_A) + \gamma_A] + (1 - x)[\alpha_B/{}^3\xi_B + \beta_B({}^1\xi_B) + \gamma_B] \quad (19)$$

The molar volume,  $V_m$ , of the mixture should also be expressible by an expression analogous to eqn. (15) so that

$$V_m = \alpha_m/{}^3\xi_m + \beta_m({}^1\xi_m) + \gamma_m \quad (20)$$

If it is assumed that

$${}^3\xi_m = x({}^3\xi_A) + (1 - x)({}^3\xi_B) \quad (21)$$

$$\beta_m({}^1\xi_m) = x\beta_A({}^1\xi_A) + (1 - x)\beta_B({}^1\xi_B) \quad (22)$$

$$\gamma_m = x\gamma_A + (1 - x)\gamma_B \quad (23)$$

TABLE 3

Comparison of  $V^F(T_1, x)$  values calculated from eqn. (24) with their corresponding experimental values at  $x_A = 0.3$  and  $0.7$  for the various mixtures

Mixture	$T_1$ (K)	${}^3\xi_A$	${}^3\xi_B$	$\alpha_{AB}$	$x_A$	$V^F$ (cm <sup>3</sup> mole <sup>-1</sup> )		Ref.
						Calcd.	Exptl.	
1. Water (A) + propanoic acid (B)	298.15	1.0	0.303	1.852	0.3	-1.2177	-0.9358	85
2. Water (A) + butanoic acid(B)	298.15	1.0	0.474	4.793	0.3	-0.7884	-1.0067	85
3. Methylene chloride(A) + methyl ethanoate(B)	298.15	1.0	0.287	-0.446	0.3	-0.9299	-0.764	85
4. Methylene chloride(A) + aniline (B)	298.15	1.0	0.799	9.108	0.7	-0.6980	-0.820	35
5. Methylene chloride (A) + <i>o</i> -toluidine (B)	298.15	1.0	1.188	12.65	0.3	0.331	0.250	35
6. Ethylenediamine(A) + isopropanol(B)	303.15	0.167	1.0	0.4308	0.3	0.211	0.263	86
7. Ethylenediamine(A) + isobutanol(B)	303.15	0.167	0.365	1.684	0.3	-0.113	-0.090	86
8. Ethylenediamine(A) + isopentanol(B)	303.15	0.167	0.707	0.478	0.3	-0.103	-0.120	86
9. Ethylenediamine(A) + benzene(B)	303.15	0.167	0.667	-0.2787	0.3	-0.070	-0.056	86
10. Ethylenediamine(A) + toluene(B)	303.15	0.167	0.940	-0.240	0.3	-0.075	-0.092	87
11. Ethylenediamine(A) + <i>o</i> -xylene(B)	303.15	0.167	1.426	-0.313	0.3	-0.501	-0.812	87
12. Ethylenediamine(A) + <i>m</i> -xylene	303.15	0.167	1.174	-0.347	0.3	-0.902	-0.528	87
					0.7	-0.744	-1.036	87
					0.7	-1.005	-0.673	87
					0.3	-0.455	-0.772	87
					0.7	-0.754	-0.413	88
					0.3	0.254	0.361	88
					0.7	0.414	0.271	88
					0.3	0.271	0.441	88
					0.7	0.481	0.287	88
					0.3	0.417	0.616	88
					0.7	0.803	0.486	88
					0.3	0.433	0.486	88
					0.7	0.804	0.639	88



TABLE 3 (continued)

Mixture	$T_1$ (K)	${}^3\xi_A$	${}^3\xi_B$	$\alpha_{AB}$	$x_A$	$V^E$ (cm <sup>3</sup> mole <sup>-1</sup> )		Ref.
						Calcd.	Exptl.	
13. Ethylenediamine(A)+ <i>p</i> -xylene(B)	303.15	0.167	1.217	-0.2944	0.3	0.372	0.537	88
14. Chloroform(A) + Diethyl- ether(B)	303.15	1.0	0.408	4.377	0.7	0.696	0.416	39
15. Bromoform(A) + benzene(B)	303.15	1.0	0.667	0.3008	0.7	-1.348	-1.160	89
16. Chloroform(A) + pyridine (B)	303.15	1.0	0.566	1.2423	0.7	-0.959	-1.021	89
17. Chloroform(A) + di. <i>tert.</i> butylether(B)	298.15	1.0	0.612	15.715	0.3	-0.014	-0.009	89
18. Carbon tetrachloride(A) + diethylether (B)	298.15	1.0	0.408	2.3374	0.7	-0.012	-0.014	89
19. Carbon tetrachloride(A) + di. <i>tert</i> butylether(B)	298.15	1.0	0.612	1.0459	0.7	-0.125	-0.115	42
20. Carbon tetrachloride(A) + di. <i>n</i> -butylether(B)	298.15	1.0	0.931	124.31	0.3	-0.099	-0.148	43
21. Carbon tetrachloride(A) + di-isopentylether(B)	298.15	1.0	1.158	8.088	0.7	-0.919	-0.995	42
22. Trimethylene oxide(A) + benzene (B)	298.15	0.577	0.667	37.77	0.3	-0.720	-0.637	42
23. 1,4-Dioxane(A) + benzene (B)	298.15	0.744	0.667	16.33	0.7	-0.513	-0.559	42
24. 1,4-Dioxane(A) + cyclo- hexane(B)	298.15	0.744	1.500	-8.3265	0.3	-0.0742	-0.0693	90
25. 1,3-Dioxane(A) + benzene(B)	298.15	0.889	0.667	7.2112	0.7	-0.0611	-0.0663	79
					0.3	-0.1363	-0.1354	42
					0.7	-0.1403	-0.1370	91
					0.3	-0.033	-0.137	92
					0.7	-0.028	-0.039	92
					0.3	-0.260	-0.255	93
					0.7	-0.279	-0.277	
					0.3	-0.058	-0.075	
					0.7	-0.042	-0.037	
					0.3	0.703	0.703	
					0.7	0.923	0.756	
					0.3	-0.172	-0.168	
					0.7	-0.153	-0.150	

TABLE 3 (continued)

Mixture	$T_1$ (K)	${}^3\xi_A$	${}^3\xi_B$	$\alpha_{AB}$	$x_A$	$V^E$ (cm <sup>3</sup> mole <sup>-1</sup> )		Ref.
						Calcd.	Exptl.	
26. <i>n</i> -Butylamine(A)+ <i>n</i> -propano(B)	303.15	0.558	1.0	8.695	0.3	-0.737	-0.820	94
27. <i>n</i> -Butylamine(A)+ <i>n</i> -butanol(B)	303.15	0.558	0.512	274.36	0.3	-0.926	-0.809	94
28. <i>n</i> -Butylamine(A)+ <i>n</i> -pentanol(B)	303.15	0.558	0.762	24.788	0.3	-0.787	-0.761	94
29. <i>n</i> -Butylamine(A)+ <i>n</i> -hexanol(B)	303.15	0.558	1.012	7.897	0.3	-0.727	-0.773	94
30. Butanol(A)+methanol(B)	298.15	0.512	1.0	-0.4813	0.3	-0.823	-0.747	94
31. Butanol(A)+ethanol(B)	298.15	0.512	1.0	-0.078	0.3	-0.691	-0.753	95
32. Butanol(A)+propan-1-ol (B)	298.15	0.512	1.0	0.0124	0.3	0.055	0.079	95
33. Oxane(A)+benzene(B)	298.15	1.076	0.667	2.409	0.3	0.071	0.051	96
34. Hexanol(A)+methanol(B)	298.15	1.012	1.0	-3252.2	0.3	0.009	0.013	96
35. Hexanol(A)+ethanol(B)	298.15	1.012	1.0	-1018.07	0.3	0.012	0.008	96
36. Hexanol(A)+propan-1-ol (B)	298.15	1.012	1.0	-528.83	0.3	-0.0014	-0.0014	96
37. Hexanol(A)+butan-1-ol(B)	298.15	1.012	0.512	-0.073	0.3	-0.0018	-0.0012	97
38. Pyridine(A)+benzene(B)	303.15	0.566	0.667	18.2526	0.3	-0.149	-0.133	97
39. Aniline(A)+benzene(B)	293.15	0.799	0.667	20.895	0.3	-0.124	-0.141	97
					0.7	0.097	0.141	98
					0.7	0.093	0.066	71
					0.3	0.030	0.043	71
					0.7	0.030	0.022	70
					0.3	0.016	0.018	70
					0.7	0.016	0.013	99
					0.3	0.012	0.011	99
					0.7	0.0085	0.0090	89
					0.3	-0.163	-0.162	89
					0.7	-0.174	-0.180	68
					0.3	-0.203	-0.195	68
					0.7	-0.189	-0.176	

40. Aniline(A) + toluene(B)	293.15	0.799	0.940	-14.716	0.3	-0.091	-0.081	68
					0.7	-0.092	-0.094	
41. Aniline(A) + <i>o</i> -xylene(B)	293.15	0.799	1.426	-2.309	0.3	0.134	0.184	68
					0.7	0.169	0.124	
42. Aniline(A) + <i>m</i> -xylene(B)	293.15	0.799	1.174	-1.632	0.3	0.048	0.088	68
					0.7	0.056	0.027	
43. Cyclohexylamine(A) + Butan-1-ol(B)	303.15	1.496	0.512	3.933	0.3	-1.293	-1.046	100
					0.7	-0.870	-0.987	
44. Cyclohexylamine(A) + butan-2-ol(B)	303.15	1.496	0.498	2.249	0.3	-0.792	-0.661	100
					0.7	-0.528	-0.599	
45. Cyclohexylamine(A) + pentan-1-ol(B)	303.15	1.496	0.762	10.673	0.3	-1.079	-0.958	100
					0.7	-0.830	-0.864	
46. Cyclohexylamine(A) + hexan-1-ol(B)	303.15	1.496	1.012	31.12	0.3	-0.874	-0.821	100
					0.7	-0.749	-0.736	
47. Cyclohexylamine(A) + heptan-1-ol(B)	303.15	1.496	1.085	44.145	0.3	-0.799	-0.790	100
					0.7	-0.703	-0.736	
48. Octan-1-ol(A) + methanol(B)	298.15	1.512	1.0	-4.494	0.3	0.142	0.196	101
					0.7	0.120	0.110	
49. Octan-1-ol(A) + ethanol(B)	298.15	1.512	1.0	-1.739	0.3	0.055	0.070	96
					0.7	0.0045	0.040	
50. Octan-1-ol(A) + propan-1-ol (B)	298.15	1.512	1.0	-1.487	0.3	0.0469	0.0492	61
					0.7	0.0400	0.0382	
51. Octan-1-ol(A) + butan-1-ol(B)	298.15	1.512	0.512	-0.1294	0.3	0.0432	0.0372	61
					0.7	0.0291	0.0328	
52. Octan-1-ol(A) + hexan-1-ol(B)	298.15	1.512	1.012	-0.303	0.3	0.0089	0.0090	61
					0.7	0.0076	0.0076	
53. Di- <i>n</i> -butylether(A) + benzene(B)	298.15	0.931	0.667	-3.696	0.3	0.1167	0.0874	79
					0.7	0.1024	0.1400	
54. Decan-1-ol(A) + methanol(B)	298.15	0.937	1.00	-1.361	0.3	0.112	0.142	102
					0.7	0.085	0.070	
55. Decan-1-ol(A) + ethanol(B)	298.15	2.012	1.0	-1.0533	0.3	0.086	0.102	71
					0.7	0.066	0.060	
56. Decan-1-ol(A) + propan-1-ol (B)	298.15	2.012	1.0	-1.052	0.3	0.0863	0.0842	71
					0.7	0.0658	0.0692	

TABLE 3 (continued)

Mixture	$T_1$ (K)	${}^3\xi_A$	${}^3\xi_B$	$\alpha_{AB}$	$x_A$	$V^E$ (cm <sup>3</sup> mole <sup>-1</sup> )		Ref.
						Calcd.	Exptl.	
57. Decan-1-ol(A) + butan-1-ol (B)	298.15	2.012	0.512	-0.180	0.3	0.0858	0.0712	96
58. Decan-1-ol(A) + <i>n</i> -pentane(B)	298.15	2.012	0.707	4.561	0.7	0.0529	0.0630	103
					0.00076	-0.0058	-0.0016	
					0.00139	-0.0107	-0.0029	
					0.3	-1.044	-0.946	
					0.7	-0.708	-0.746	
59. Decan-1-ol(A) + <i>n</i> -hexane(B)	298.15	2.012	0.957	5.938	0.97573	-0.0653	-0.0768	103
					0.00178	-0.0064	0.0018	
					0.00547	-0.0194	0.0037	
					0.3	-0.5662	-0.5216	
					0.7	-0.4251	-0.4568	
60. Decan-1-ol(A) + hexan-1-ol(B)	298.15	2.012	1.012	-0.462	0.98453	-0.0261	-0.0329	96
					0.3	0.0363	0.0324	
					0.7	0.0278	0.0322	
					0.3	0.0068	0.0066	
					0.7	0.0060	0.0065	
61. Decan-1-ol(A) + octan-1-ol(B)	298.15	2.012	1.512	-0.652	0.00083	-0.0007	0.0034	103
					0.0052	-0.0046	0.0182	
					0.3	-0.1696	-0.1283	
					0.7	-0.1492	-0.1828	
					0.99688	-0.0020	-0.0028	
62. Decan-1-ol(A) + <i>n</i> -octane (B)	298.15	2.012	1.457	12.4800	0.99768	-0.0020	-0.0021	103
					0.00145	0.0014	0.0087	
					0.00787	0.0076	0.0422	
					0.03356	0.1541	0.1202	
					0.3	0.2325	0.2862	
63. Decan-1-ol(A) + <i>n</i> -hexadecane(B)	298.15	2.012	3.457	-11.1494	0.7	0.2874	0.2432	103
					0.97209	0.0442	0.0320	
					0.99314	0.0103	0.0083	

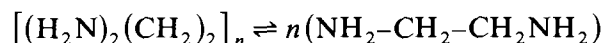
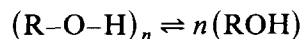
then the molar excess volume for this mixture is given by

$$V^E = \alpha_{AB} \left[ \frac{1}{x_A({}^3\xi_A) + (1-x)({}^3\xi_B)} - \frac{x}{{}^3\xi_A} - \frac{(1-x)}{{}^3\xi_B} \right] \quad (24)$$

$$\alpha_{AB} = \alpha_m = \alpha_A = \alpha_B$$

Evaluation of  $V^E$  from eqn. (24) requires a knowledge of  $\alpha_{AB}$  for the mixture and this was evaluated by fitting  $V^E(T_1, x = 0.5)$  data to eqn. (24). This value of  $\alpha_{AB}$  was next employed to evaluate  $V^E(T_1, x = 0.3, 0.7)$  data for the mixture. Such  $V^E(T_1, x)$  data for various binary mixtures are recorded in Table 3 and are also compared with their corresponding experimental values [35,39,42,43,61,68,70,71,79,85-103].

Examination of Table 3 reveals that the  $V^E(T_1, x = 0.3, 0.7)$  data so obtained for the various mixtures compare well with their experimental values even for mixtures where either one or both the components are associated, or where the components are known to undergo specific interaction between themselves, the quantitative agreement between the theoretical and experimental  $V^E(T_1, x)$  values for binary mixtures containing ethylenediamine, cyclohexylamine and water is not good. For  $x$  ethylenediamine +  $(1-x)$  isopropanol,  $+(1-x)$  isobutanol and  $+(1-x)$  isopentanol mixtures while  $\{V_{\text{calcd.}}^E(T_1, x = 0.3) - V_{\text{exptl.}}^E(T_1, x = 0.3)\} = 0.3 \text{ cm}^3 \text{ mole}^{-1}$ ,  $\{V_{\text{calcd.}}^E(T_1, x = 0.7) - V_{\text{exptl.}}^E(T_1, x = 0.7)\} = -0.35 \text{ cm}^3 \text{ mole}^{-1}$ . This is understandable since both ethylenediamine and alkanols are associated in the pure state through hydrogen bonding [87 and refs. cited therein] so that their  $V^E$  data are due essentially to (i) mutual breaking up of  $\text{O-H} \cdots \text{O}$  and  $\text{N-H} \cdots \text{N}$  bonds represented by



in the self-associated alkanols as well as ethylenediamine; and (ii) the formation of an  $\text{O-H} \cdots \text{N}$  bond between unlike molecules.

Consequently, for these mixtures when  $x = 0.3$ , while all these alkanols remain practically as  $(\text{ROH})_n$ , the ethylenediamine undergoes almost complete depolymerization and its monomers undergo  $\text{N} \cdots \text{H-O}$  bond formation with alkanols. Since ethylenediamine is a strong bidentate ligand, effects due to (ii) outweigh those due to effect (i) so that the  $V_{\text{calcd.}}^E(T_1, x)$  values [calculated on the basis that there are no effects like (i) and (ii) as in the present case] would be more positive than the  $V_{\text{exptl.}}^E(T_1, x)$  values, and  $\{V_{\text{calcd.}}^E(T_1, x = 0.3) - V_{\text{exptl.}}^E(T_1, x = 0.3)\}$  would have the same value for all these mixtures. An opposite effect will characterize these mixtures for  $x = 0.7$ .

For  $x$  ethylenediamine +  $(1-x)$  benzene,  $+(1-x)$  toluene,  $+(1-x)$  *o*-xylene,  $+(1-x)$  *p*-xylene and  $+(1-x)$  *m*-xylene mixtures at  $x = 0.3$ , while ethylenediamine undergoes almost complete depolymerization, the

ability of the aromatics to interact with these ethylenediamine monomers through N–H  $\cdots \pi$  interaction would be governed by the ability of the aromatic hydrocarbons to donate their  $\pi$ -electrons. Now while this ability to donate  $\pi$ -electrons increases in the order *o*-xylene  $\geq$  *m*-xylene  $>$  *p*-xylene  $>$  toluene  $>$  benzene, the steric repulsion increases in the same order so that if the effects due to steric repulsion between ethylenediamine monomers and the aromatic hydrocarbons do not outweigh those due to specific N–H  $\cdots \pi$  interactions between them, the  $\{V_{\text{calcd}}^E(T_1, x = 0.3)\}$  [as calculated on the basis that there are no effects like (i) and (ii) in the present case]  $- V_{\text{exptl}}^E(T_1, x = 0.3)\}$  value would be negative and would vary with the nature of the aromatic hydrocarbon as has indeed been observed; it varies in the order *m*-xylene  $>$  benzene  $>$  toluene  $\approx$  *p*-xylene  $>$  *o*-xylene. An opposite effect would characterize these mixtures for  $x = 0.7$ . *x* Cyclohexylamine +  $(1 - x)$  butan-1-ol,  $+(1 - x)$  butan-2-ol,  $+(1 - x)$  pentan-1-ol,  $+(1 - x)$  hexan-1-ol and  $+(1 - x)$  heptan-1-ol mixtures may also be characterized by similar effects if it is assumed that while cyclohexylamine undergoes depolymerization [100], the alkanol remains as (ROH) $_n$ . A similar situation may also characterize binary mixtures containing water.

The very fact that the present approach describes very well  $V^E(T_1, x)$  data for  $(x \text{ alkanol} + (1 - x) \text{ Alkanol})$  mixtures suggests that the depolymerization of alkanol is governed primarily by the other component in the mixture and that for the present case they behave as normal molecules and do not undergo depolymerization.

#### EFFECT OF TEMPERATURE ON $V^E(T_1, x)$ DATA OF A BINARY MIXTURE

Since the molar volume,  $V$ , of a fluid varies almost directly as its  $T$ , it follows that

$$V_A(T_1) \propto T_1 \quad (25)$$

and

$$V_A(T_2) \propto T_2 \quad (26)$$

or

$$V_A(T_2) = \frac{T_2}{T_1} V_A(T_1) = \frac{T_2}{T_1} [\alpha_A / {}^3\xi_A + \beta_A ({}^1\xi_A) + \gamma_A] \quad (27)$$

so that  $V^E(T_2, x)$  for an  $[x \text{ A} + (1 - x) \text{ B}]$  mixture would be given by

$$V^E(T_2, x) = \frac{T_2}{T_1} V^E(T_1, x) \quad (28)$$

Thus, if  $V^E(T_1, x)$  data for a binary mixture are known or can be evaluated from eqn. (27) from the  $V^E(T_1, x = 0.5)$  data, it should be possible to evaluate  $V^E(T_2, x)$  data for the mixture. Such  $V^E(T_2, x)$  data for some

TABLE 4

Comparison of  $V^E(T_2, x)$  values evaluated from  $V^E(T_1, x)$  values by means of eqn. (28) utilizing  $V^E(T_1, x, = 0.5)$  data alone with their corresponding experimental values for various mixtures

Mixture	$T_1$	$T_2$	$x$	$V^E(T_2, x)$ ( $\text{cm}^3 \text{mole}^{-1}$ )		Ref.
				Calcd.	Exptl.	
1. $x$ Methylene chloride + ( $1-x$ ) methyl ethanoate	298.15	308.15	0.3	0.337	0.261	35
			0.7	0.215	0.271	
2. $x$ Methylene chloride + ( $1-x$ ) aniline	298.15	308.15	0.3	-0.117	-0.113	86
			0.7	-0.107	-0.186	
3. $x$ Methylene chloride + ( $1-x$ ) <i>o</i> -toluidine	298.15	308.15	0.3	-0.072	-0.083	86
			0.7	-0.078	-0.130	
4. $x$ Chloroform + ( $1-x$ ) pyridine	303.15	308.15	0.3	-0.127	-0.114	89
			0.7	-0.102	-0.150	
5. $x$ Bromoform + ( $1-x$ ) benzene	303.15	308.15	0.3	-0.013	-0.018	89
			0.7	-0.012	-0.019	
6. $x$ Carbon tetrachloride + ( $1-x$ ) di- <i>n</i> -butylether	298.15	308.15	0.3	-0.1409	-0.1317	79
			0.7	-0.1450	-0.1319	
7. $x$ 1,4-Dioxane + ( $1-x$ ) benzene	298.15	288.15	0.3	-0.056	-0.066	91
			0.7	-0.041	-0.025	
		308.15	0.3	-0.062	-0.087	91
			0.7	-0.044	-0.054	
8. $x$ 1,4-Dioxane + ( $1-x$ ) cyclohexane	298.15	288.7	0.3	0.679	0.845	92
			0.7	0.892	0.723	
		318.15	0.3	0.750	0.944	92
			0.7	0.985	0.799	
9. $x$ <i>n</i> -Butylamine + ( $1-x$ ) propan-1-ol	303.15	313.15	0.3	-0.761	-0.890	94
			0.7	-0.957	-0.919	
10. $x$ <i>n</i> -Butylamine + ( $1-x$ ) butan-1-ol	303.15	313.15	0.3	-0.842	-0.888	94
			0.7	-0.813	-0.819	
11. $x$ <i>n</i> -Butylamine + ( $1-x$ ) pentan-1-ol	303.15	313.15	0.3	-0.751	-0.843	94
			0.7	-0.850	-0.834	
12. $x$ <i>n</i> -Butylamine + ( $1-x$ ) hexan-1-ol	303.15	313.15	0.3	-0.714	-0.921	94
			0.7	-0.901	-0.829	
13. $x$ Pyridine + ( $1-x$ ) benzene	303.15	308.15	0.3	-0.165	-0.168	89
			0.7	-0.177	-0.160	
14. $x$ Aniline + ( $1-x$ ) benzene	293.15	298.15	0.3	-0.204	-0.208	68
			0.7	-0.192	-0.179	
		303.15	0.3	-0.210	-0.224	68
			0.7	-0.195	-0.192	
		308.15	0.3	-0.213	-0.239	68
			0.7	-0.199	-0.205	
15. $x$ Aniline + ( $1-x$ ) toluene	293.15	298.15	0.3	-0.093	-0.090	68
			0.7	-0.094	-0.095	
		303.15	0.3	-0.094	-0.096	68
			0.7	-0.095	-0.098	
		308.15	0.3	-0.096	-0.099	68
			0.7	-0.097	-0.112	

TABLE 4 (continued)

Mixture	$T_1$	$T_2$	$x$	$V^E(T_2, x)$ ( $\text{cm}^3 \text{ mole}^{-1}$ )		Ref.
				Calcd.	Exptl.	
16. $x$ Aniline + ( $1-x$ ) <i>o</i> -xylene	293.15	298.15	0.3	0.136	0.188	68
			0.7	0.172	0.131	
		303.15	0.3	0.139	0.199	68
			0.7	0.175	0.142	
		308.15	0.3	0.141	0.207	68
			0.7	0.178	0.146	
17. $x$ Aniline + ( $1-x$ ) <i>m</i> -xylene	293.15	298.15	0.3	0.049	0.096	68
			0.7	0.057	0.036	
		303.15	0.3	0.050	0.098	68
			0.7	0.058	0.042	
		308.15	0.3	0.051	0.101	68
			0.7	0.059	0.050	
18. $x$ Di- <i>n</i> -butylether + ( $1-x$ ) benzene	298.15	308.15	0.3	0.1206	0.0882	79
			0.7	0.1057	0.1375	

binary mixtures (listed in Table 3) are recorded in Table 4 and are also compared with their corresponding experimental values [35,68,79,86,89,91,92,94].

Examination of Table 4 reveals that  $V^E(T_2, x = 0.3, 0.7)$  values so calculated compare reasonably well with the corresponding experimental values even for those mixtures which are known to be characterized by specific interaction between their components or when one of the compounds is even associated.

#### EFFECT OF PRESSURE ON $V^E(T_1, x)$ DATA OF A BINARY MIXTURE

An increase of pressure on a fluid at a given temperature,  $T_1$  would reduce its molar volume, and the extent to which its molar volume is decreased by an increase of pressure would be determined by its isothermal compressibility and the applied pressure. Thus, if  $V_A(T, P)$  and  $V_A^1(T, P^1)$  denote the molar volume of A at a given  $T$  and pressures  $P$  and  $P^1$ , respectively, and if  $K_T(P)$  is the isothermal compressibility of A at  $P$ , then

$$V_A^1(T, P^1) = V_A(T, P)[1 - K_T(P)(P^1 - P)] \quad (29)$$

Further, according to Wilhelm (see Takagi [104]),  $K_T$  of a liquid varies with pressure as

$$(\partial K_T / \partial P)_T = -CK_T^2 \quad (30)$$



where  $C$  is a constant with a very small or zero temperature dependence and has a value of approximately 10 for most of the common organic liquids. Integration of eqn. (30) yields

$$1/K_T(P') \approx \frac{1}{K_T(P = 1 \text{ atm})} + CP' \quad (31)$$

where  $K_T(P')$  and  $K_T(P = 1 \text{ atm})$  denote the isothermal compressibility of a liquid at pressure  $P'$  and atmospheric pressure, respectively. Accordingly

$$V_A^1(T_1, P^1) = V_A(T_1, P = 1 \text{ atm}) \left\{ 1 - \frac{K_T(P = 1 \text{ atm})(P^1 - 1)}{1 + K_T(P = 1 \text{ atm})CP^1} \right\} \quad (32)$$

where

$$K_T(P = 1 \text{ atm}) = (1 + T\alpha^2 U^2 / C_p) / (U^2)_{P=1 \text{ atm}} \quad (33)$$

and  $\alpha$ ,  $U$  and  $C_p$  represent the expansivity, ultrasonic speed in  $\text{m s}^{-1}$  and molar heat capacity of A at the thermodynamic temperature  $T_1$  and  $P = 1 \text{ atm}$ . Thus, if ultrasonic speed  $U$  in a fluid at a given temperature  $T_1$  and  $P = 1 \text{ atm}$  are known, eqn. (32) would express the molar volume of A at  $T$  and pressure  $P^1$ . Takagi [104] has determined the density of benzene, *m*-xylene, *p*-xylene, chlorobenzene, aniline and benzene + *m*-xylene, + *p*-xylene, + aniline and chlorobenzene + aniline mixtures from the pressure dependence of ultrasonic speed in the pure components as well the mixtures. Table 5 clearly shows that  $V_A^1(T_1, P^1 = 100, 200, 300, 400, 500 \text{ atm, etc.})$  values of benzene, *m*-xylene, *p*-xylene chlorobenzene and aniline evaluated from eqn. (32) utilizing the  $V_A(T_1, P = 1 \text{ atm})$  values [104] compare very well with the corresponding  $V_A^1(T_1, P^1)$  values [104] obtained from the pressure dependence of ultrasonic speeds at  $T_1$  in them.

TABLE 5

Comparison of molar volumes  $V'$  ( $T_1 = 303.15, P^1$ ), data of pure compounds evaluated from eqn. (32) employing their  $V(T_1 = 303.15, P = 1 \text{ atm})$  data with their corresponding experimental values for various compounds

$P^1$ (atm)	$V(T_1, P^1)$ ( $\text{cm}^3 \text{ mole}^{-1}$ )									
	Benzene		<i>m</i> -Xylene		<i>p</i> -Xylene		Chloroform		Aniline	
	Calcd.	Exptl. [104]	Calcd.	Exptl. [104]	Calcd.	Exptl. [104]	Calcd.	Exptl. [105]	Calcd.	Exptl. [105]
100	89.19	88.98	123.04	122.78	123.54	123.30				
200	88.64	88.21	122.32	121.81	122.80	122.30				
400	87.73	86.84	121.11	120.07	121.58	120.40				
500	87.35	86.24	120.61	119.6	121.06	119.76				
552.6	87.17	85.51					99.67	98.74	89.81	89.32
1035.2							98.31	96.52	88.82	87.84
1517.8							97.36	94.54	88.05	86.59

This would then mean that for an  $[x \text{ A} + (1 - x) \text{ B}]$  mixture

$$V_A^1(T_1, P^1) = V_A(T_1, P = 1 \text{ atm}) \left[ 1 - \frac{K_{T_A}(P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_A}(P = 1 \text{ atm})CP^1} \right] \quad (34)$$

and

$$V_B^1(T_1, P^1) = V_B(T_1, P = 1 \text{ atm}) \left[ 1 - \frac{K_{T_B}(P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_B}(P = 1 \text{ atm})CP^1} \right] \quad (35)$$

so that  $V^E(T_1, x, P^1)$  would be given by

$$\begin{aligned} V^E(T_1, x, P^1) = \alpha_{AB} & \left[ \left( 1 - \frac{K_{T_m}(P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_m}(P = 1 \text{ atm})CP^1} \right) \left( \frac{1}{x^3 \xi_A + (1-x)^3 \xi_B} \right) \right. \\ & - \frac{x}{^3 \xi_A} \left( 1 - \frac{K_{T_A}(P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_A}(P = 1 \text{ atm})CP^1} \right) - \frac{(1-x)}{^3 \xi_B} \\ & \left. \times \left( 1 - \frac{K_{T_B}(P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_B}(P = 1 \text{ atm})CP^1} \right) \right] \quad (36) \end{aligned}$$

We now consider two cases

case (i) when

$$\begin{aligned} K_{T_m}(T_1, P = 1 \text{ atm}) &= xK_{T_A}(T_1, P = 1 \text{ atm}) + (1-x)K_{T_B}(T_1, P = 1 \text{ atm}) \\ &\approx K_{T_A}(T_1, P = 1 \text{ atm}) \approx K_{T_B}(T_1, P = 1 \text{ atm}) \end{aligned}$$

so that eqn. (36) yields

$$V^E(T_1, x, P^1) = V^E(T_1, x, P = 1 \text{ atm}) \left[ 1 - \frac{K_{T_m}(T_1, P = 1 \text{ atm})(P^1 - 1)}{1 + K_{T_m}(T_1, P = 1 \text{ atm})CP^1} \right] \quad (37)$$

case (ii) when

$$\begin{aligned} K_{T_m}(T_1, P = 1 \text{ atm}) &= xK_{T_A}(T_1, P = 1 \text{ atm}) + (1-x)K_{T_B}(T_1, P = 1 \text{ atm}) \\ &\neq K_{T_A}(T_1, P = 1 \text{ atm}) \neq K_{T_B}(T_1, P = 1 \text{ atm}) \end{aligned}$$

so that  $V^E(T_1, x, P^1)$  of an  $[x \text{ A} + (1 - x) \text{ B}]$  mixture is given by

$$\begin{aligned} V^E(T_1, x, P^1) &= V^E(T_1, x, P = 1 \text{ atm}) \\ & - \alpha_{AB}(P^1 - 1) \left\{ \frac{K_{T_m}(T_1, P = 1 \text{ atm})}{[1 + K_{T_m}(T_1, P = 1 \text{ atm})][x(^3 \xi_A) + (1-x)(^3 \xi_B)]} \right. \\ & \left. - \frac{xK_{T_A}(T_1, P = 1 \text{ atm})}{[1 + K_{T_A}(T_1, P = 1 \text{ atm})(^3 \xi_A)]} - \frac{(1-x)K_{T_B}(T_1, P = 1 \text{ atm})}{[1 + K_{T_B}(T_1, P = 1 \text{ atm})(^3 \xi_B)]} \right\} \quad (38) \end{aligned}$$

Takagi [104] has determined the density of [ $x$  benzene +  $(1 - x)$   $m$ -xylene] and [ $x$  benzene +  $(1 - x)$   $p$ -xylene] mixtures at  $T_1 = 303.15$  K from the pressure dependence of ultrasonic speeds in these mixtures at normal as well as high pressures. Since  $K_{T_m}(T_1, P = 1 \text{ atm}) = x K_{T_{\text{benzene}}}(T_1, P = 1 \text{ atm}) + (1 - x) K_{T_m}^{m- \text{ or } p\text{-xylene}}(T_1, P = 1 \text{ atm}) \approx K_{T_{\text{benzene}}}(T_1, P = 1 \text{ atm}) \approx K_{T_m}^{m- \text{ or } p\text{-xylene}}(T_1, P = 1 \text{ atm})$ ,  $V^E(T_1, x, P^1)$  data at  $P^1 = 100, 200, 300, 400$  atm, etc., for these mixtures should be well described by eqn. (37) when the corresponding  $V^E(T_1, x, P = 1 \text{ atm})$  data for these mixtures are known or can be evaluated from eqn. (24) utilizing  $V^E(T_1, x = 0.5, P = 1 \text{ atm})$  data alone. Such  $V^E(T_1, x, P^1)$  data for these mixtures at  $x = 0.2, 0.4, 0.6$  and  $0.8$  are recorded in Table 6 and are also compared with their corresponding experimental  $V^E(T_1, x, P^1)$  data [104] obtained from the pressure of ultrasonic speeds in these mixtures as also in the pure components at  $T_1$ . Examination of Table 6 shows that eqn. (37) well describes the  $V^E(T_1, x, P^1)$  data of these mixtures.

Takagi [105] has also determined the densities of [ $(1 - x)$  benzene +  $x$  aniline] and [ $(1 - x)$  chlorobenzene +  $x$  aniline] mixtures at  $T_1 = 298.15$  K from the pressure dependence of ultrasonic speeds in them at  $P^1 = 1, 552.6, 1032.6, 1517.8$  and  $2069.4$  atm. For these mixtures at  $T_1 = 298.15$  K,  $K_{T_m}(T_1, P = 1 \text{ atm}) \neq K_{T_\lambda}(T_1, P = 1 \text{ atm})$  so that the  $V^E(T_1, x, P^1)$  of these mixtures could be evaluated from eqn. (38) if  $V^E(T_1, x, P = 1 \text{ atm})$  data for these mixtures are known. Examination of Table 5, however, suggests that eqn. (32) well describes the molar volume data of chlorobenzene and aniline at  $P^1 = 552.6$  atm only; at pressures higher than  $552.6$  atm, the molar volume data of these mixtures differ substantially from their corresponding experimental values. Consequently, only  $V^E(T_1 = 298.15 \text{ K}, x, P = 552.6)$  data for these mixtures were evaluated from eqn. (38) and are also recorded in Table 6. These are also compared with their corresponding  $V^E(T_1 = 298.15, x, P^1 = 552.6 \text{ atm})$  data [105] in Table 6. It is evident that while the  $V^E(T_1 = 298.15 \text{ K}, x, P^1 = 552.6 \text{ atm})$  values calculated from eqn. (38) for these mixtures have the same sign as the corresponding experimental  $V^E(T_1, x, P^1)$  values, the quantitative agreement is not good; the calculated  $V^E(T_1, x, P^1)$  values are consistently smaller than the corresponding experimental values and while the discrepancy between the experimental and theoretical  $V^E(T_1, x, P^1)$  values for [ $(1 - x)$  benzene +  $x$  aniline] mixtures is more acute for  $x > 0.5$ , the theoretical  $V^E(T_1, x, P^1 = 552.6 \text{ atm})$  values for [ $(1 - x)$  chlorobenzene +  $x$  aniline] mixtures are consistently smaller than the corresponding experimental values by about  $0.06 \text{ cm}^3 \text{ mole}^{-1}$ .

This is understandable since benzene (A) + aniline  $B_n$  ( $n = 2, 3 \dots$ ) mixtures are assumed [106] to be characterized by the presence of AB,  $AB_2$ ,  $A_2B_2$  molecular species in equilibrium with A and  $B_n$  according to the reaction.

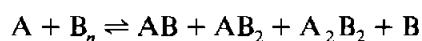


TABLE 6

Comparison of  $V^E(T_1, x, P^1)$  values evaluated from eqn. (37) or (38) (see text) employing  $V^E(T_1, x, P = 1 \text{ atm})$  data with their corresponding experimental values at various  $P^1$  for some binary mixtures

Mixture	$T_1$ (K)	$x$	$V^E(T_1, x, P^1)$ (cm <sup>3</sup> mole <sup>-1</sup> )			
			$P^1 = 100 \text{ atm}$		$P^1 = 200 \text{ atm}$	
			Calcd.	Exptl. [104]	Calcd.	Exptl. [104]
(1 - $x$ ) Benzene + $x$ <i>p</i> -xylene	303.15	0.2	0.1176	0.1560	0.1080	0.1156
		0.4	0.1365	0.1284	0.1255	0.1101
		0.6	0.2231	0.2270	0.2053	0.2139
		0.8	0.0609	0.0651	0.0561	0.0516
(1 - $x$ ) Benzene + $x$ <i>m</i> -xylene	303.15	0.2	0.1521	0.1635	0.1398	0.1599
		0.4	0.2746	0.2867	0.2527	0.2868
		0.6	0.2629	0.2818	0.2422	0.2742
		0.8	0.1819	0.1960	0.1677	0.1934
(1 - $x$ ) Benzene + $x$ aniline	298.15	0.1537				
		0.3074				
		0.4611				
		0.5916				
		0.7221				
(1 - $x$ ) Chloro- benzene + $x$ aniline	298.15	0.2852				
		0.4150				
		0.5467				
		0.6917				
		0.8218				

and as  $V^E(T_1, x, P = 1 \text{ atm})$  for this mixture is negative, an increase of pressure would cause the reaction to proceed more towards the right.  $K_{T_n}(T_1, x, P = 1 \text{ atm})$  values for this mixture should therefore be  $> \{ (K_{T_A}^E(T_1, x, P = 1 \text{ atm}) x_A + (1 - x_A) K_{T_B}^E(T_1, x, P = 1 \text{ atm})) \}$  since AB, etc., species are less compressible than A or B so that  $V^E(T_1, x, P^1)$  values evaluated from eqn (37) on the assumption that there are no molecular species in this solution would be smaller than the  $V^E(T_1, x, P^1)$  values, as has indeed been observed. Further,  $\{V_{\text{calcd.}}^E(T_1, x, P^1) - V_{\text{exptl.}}^E(T_1, x, P^1)\}$  value for this mixture would vary with  $x$  and would be maximum corresponding to  $x$  at which maximum amounts of the less compressible species are produced in this mixture. Similar arguments would also apply to chlorobenzene (A) + aniline ( $B_n, n = 2, 3 \dots$ ) mixtures if it is assumed that this mixture is characterized by the reaction  $A + B_n \rightleftharpoons AB_n$  so that the  $\{V_{\text{calcd.}}^E(T_1, x, P^1) - V_{\text{exptl.}}^E(T_1, x, P^1)\}$  value for this mixture will be almost

$P^1 = 300 \text{ atm}$		$P^1 = 400 \text{ atm}$		$P^1 = 500 \text{ atm}$		$P^1 = 552.6 \text{ atm}$	
Calcd.	Exptl. [104]	Calcd.	Exptl. [104]	Calcd.	Exptl. [104]	Calcd.	Exptl. [105]
0.985	0.0972	0.0889	0.0900	0.0794	0.0931		
0.1145	0.0980	0.1036	0.0811	0.0926	0.0750		
0.1875	0.1975	0.1697	0.1850	0.1519	0.1783		
0.512	0.0365	0.0464	0.0350	0.0416	0.0330		
0.1275	0.1618	0.1153	0.1589	0.1030	0.1592		
0.2308	0.2833	0.2089	0.1955	0.1870	0.2143		
0.2215	0.2663	0.2008	0.2656	0.1801	0.2625		
0.1536	0.1942	0.1395	0.1857	0.1253	0.1805		
						-0.2811	-0.0028
						-0.2910	-0.0316
						-0.4948	-0.0366
						-0.2387	-0.0921
						-0.1608	-0.1066
						-0.1660	-0.0965
						0.0302	0.0844
						0.0315	0.1126
						0.0670	0.1305
						0.0635	0.1283
						0.0272	0.0851

constant with  $x$ , as has been observed. Alternatively, when the isothermal compressibility data at  $T_1$  and  $P = 1 \text{ atm}$  for the pure components as well as their mixtures are not available, it may still be possible to study the effect of pressure on the molar or the specific volume of binary mixtures as well as their pure components.

As pressure on a liquid is increased, its molar or specific volume should decrease. In other words, the molar or specific volume of a liquid at a given  $T_1$  should vary as some inverse function of the applied pressure so that if  $V_A(T_1, P_1)$  and  $v_A(T_1, P_1)$  represent the molar and specific volume, respectively, of A at  $T_1$  and  $P_1$ , then

$$V_A(T_1, P_1) \propto f(1/P_1) \quad (39)$$

or

$$v_A(T_1, P_1) \propto f(1/P_1) \quad (40)$$

TABLE 7

Comparison of specific volume  $\nu(T_1, P_2)$  values evaluated from eqn (46) utilizing  $\nu(T_1, P_1)$  values at various  $T$  and  $P_2$  with their corresponding experimental values for some compounds and their mixtures

Compound	$T_1$ (K)	$\nu(T_1, P_2)$ ( $\text{cm}^{-3} \text{g}^{-1}$ )				
		$P_2 = 99 \text{ atm}$		$P_2 = 393 \text{ atm}$		
		Calcd.	Exptl.	Calcd.	Exptl.	
Chlorobenzene [108]	298.15	0.85748	0.90175	0.84283	0.88495	
	318.15	0.87470	0.91900	0.85976	0.89992	
	338.15	0.89280	0.93699	0.87755	0.91528	
Bromobenzene [108]	298.15	0.63412	0.66737	0.62329	0.65613	
	318.15	0.64587	0.67921	0.63484	0.66654	
	338.15	0.65814	0.69150	0.64690	0.67720	
Nitrobenzene [108]	298.15	0.78792	0.83051	0.77446	0.81959	
	318.15	0.80118	0.84404	0.78749	0.83186	
	338.15	0.81490	0.85799	0.80099	0.84436	
Aniline [108]	298.15	0.92802	0.97851	0.91218	0.96679	
	318.15	0.94413	0.99499	0.92801	0.98148	
	338.15	0.96089	1.01206	0.94448	0.99688	
Methylcyclopentane [107]	298.2	1.2699	1.330	1.2482	1.292	
	323.2	1.31240	1.372	1.29000	1.324	
Ethanol [107]	298.2	1.28659	1.179	1.10716	1.146	
	323.2	1.15000	1.203	1.13036	1.165	
	348.2	1.17171	1.124	1.15171	1.182	
<i>n</i> -Heptane [107]	298.2	1.38982	1.454	1.36609	1.409	
	323.2	1.43136	1.493	1.40692	1.441	
	348.2	1.48518	1.542	1.45982	1.476	
(1 - $x$ ) Ethanol + $x$ methylcyclopentane [107]	298.2	0.0985	1.21798	1.276	1.19718	1.242
		0.1857	1.22836	1.286	1.20739	1.251
		0.4880	1.25291	1.311	1.23152	1.273
		0.5426	1.25480	1.312	1.2337	1.273
		0.6992	1.26330	1.323	1.24173	1.284
		0.8495	1.26802	1.328	1.24637	1.291
	323.2	0.0985	1.25480	1.311	1.23337	1.270
		0.1857	1.26708	1.321	1.24544	1.281
		0.4880	1.29634	1.352	1.27421	1.307
		0.5426	1.29729	1.353	1.27514	1.308
		0.6992	1.30480	1.362	1.28256	1.317
		0.8495	1.31240	1.371	1.28999	1.324
	348.2	0.0985	1.30012	1.350	1.27792	1.302
		0.1857	1.30484	1.363	1.28256	1.313
		0.4880	1.34450	1.398	1.32154	1.340

$P_2 = 687 \text{ atm}$		$P_2 = 1178 \text{ atm}$		$P_2 = 1962 \text{ atm}$	
Calcd.	Exptl.	Calcd.	Exptl.	Calcd.	Exptl.
0.83697	0.87090	0.83189	0.85381	0.82606	0.82784
0.85378	0.88428	0.84859	0.86549	0.84265	0.83745
0.87145	0.89786	0.86615	0.87726	0.86009	0.84704
0.61896	0.64659	0.61520	0.63479	0.61089	0.61661
0.63043	0.65597	0.62659	0.64306	0.62221	0.62349
0.64241	0.66548	0.63850	0.65138	0.63403	0.63033
0.76908	0.81001	0.76440	0.79780	0.75905	0.77831
0.78202	0.82130	0.77726	0.80799	0.77182	0.78700
0.79542	0.83270	0.79058	0.81817	0.78505	0.79559
0.90584	0.95581	0.90031	0.94213	0.89402	0.92009
0.92156	0.96967	0.91595	0.95468	0.90954	0.93085
0.93792	0.98378	0.93221	0.96734	0.92569	0.94158
1.23954	1.263	1.2320	1.2790	1.22338	1.184
1.28102	1.290	1.27322	1.2490	1.26431	1.204
1.09946	1.127				
1.12250	1.145				
1.14370	1.158				
1.35659	1.374	1.34747	1.330	1.33890	1.284
1.39714	1.401	1.38774	1.353	1.37892	1.300
1.44967	1.431	1.43992	1.378	1.43077	1.320
1.18886	1.215	1.18086	1.180	1.17336	1.141
1.19899	1.224	1.19093	1.196	1.18336	1.148
1.22296	1.245	1.21473	1.196	1.20701	1.167
1.22480	1.246	1.21656	1.199	1.20883	1.168
1.23309	1.255	1.22480	1.210	1.21702	1.181
1.23770	1.262	1.22938	1.214	1.22156	1.186
1.22480	1.241	1.21656	1.204	1.20883	1.161
1.23678	1.249	1.22846	1.211	1.22065	1.166
1.26535	1.273	1.25684	1.231	1.24885	1.185
1.26627	1.274	1.25776	1.235	1.24976	1.188
1.27629	1.283	1.26508	1.242	1.25704	1.199
1.28367	1.290	1.27240	1.248	1.26431	1.203
1.26904	1.267	1.26050	1.225	1.25249	1.179
1.27364	1.276	1.26508	1.233	1.25704	1.183
1.31235	1.302	1.30353	1.255	1.29524	1.202

TABLE 7 (continued)

Compound	$T_1$ (K)	$\nu(T_1, P_2)$ ( $\text{cm}^{-3} \text{g}^{-1}$ )				
		$P_2 = 99 \text{ atm}$		$P_2 = 393 \text{ atm}$		
		Calcd.	Exptl.	Calcd.	Exptl.	
$(1-x)$ <i>n</i> -Heptane + $x$ ethanol [107]	298.2	0.3047	1.36433	1.425	1.34103	1.381
		0.5732	1.32467	1.387	1.30205	1.345
		0.8190	1.26896	1.327	1.24730	1.290
	323.2	0.3047	1.40587	1.465	1.38186	1.412
		0.5732	1.36716	1.424	1.34381	1.373
		0.8190	1.31145	1.370	1.28906	1.325
	348.2	0.5732	1.41625	1.470	1.39207	1.407
		0.8190	1.35488	1.411	1.33175	1.356
$(1-x)$ Methyl- cyclopentane + $x$ <i>n</i> -heptane [107]	298.2	0.1191	1.28690	1.348	1.26493	1.310
		0.3837	1.32278	1.384	1.30019	1.343
		0.5025	1.33694	1.398	1.31411	1.357
		0.6472	1.35394	1.415	1.33082	1.372
		0.8317	1.37377	1.436	1.35031	1.392
		0.1191	1.32561	1.385	1.30298	1.426
	323.2	0.3837	1.36527	1.426	1.34196	1.375
		0.5025	1.37943	1.439	1.35588	1.389
		0.6472	1.39832	1.457	1.37444	1.405
		0.8317	1.41720	1.478	1.39300	1.425
		0.5025	1.42853	1.483	1.40414	1.424
		0.6472	1.44741	1.502	1.42270	1.439
	348.2	0.8317	1.46724	1.524	1.44219	1.458
	$T_1$ (K)	$x$	$P_2 = 1.0 \text{ atm}$		$P_2 = 1032.6 \text{ atm}$	
			Calcd.	Exptl.	Calcd.	Exptl.
$(1-x)$ Benzene + $x$ aniline [105]	298.15	0.1537	1.16007	1.11380	1.06368	1.04505
		0.3074	1.13500	1.08652	1.04070	1.02453
		0.4611	1.11149	1.06023	1.01914	1.00518
		0.5916	1.09207	1.03933	1.00133	1.98885
		0.7211	1.07404	1.01983	1.98480	1.97375
		0.8269	1.01024	1.00516	1.97215	1.896670
$(1-x)$ Chloroben- zene + $x$ aniline [105]	298.15	0.2852	0.97287	0.92770	0.89204	0.88006
		0.4150	0.97493	0.93693	0.90231	0.89097
		0.5467	0.99590	0.94670	0.91315	0.90245
		0.6917	0.93277	0.95779	0.92552	0.91563
		0.8218	0.94415	0.96811	0.93681	0.94449



$P_2 = 687 \text{ atm}$		$P_2 = 1178 \text{ atm}$		$P_2 = 1962 \text{ atm}$	
Calcd.	Exptl.	Calcd.	Exptl.	Calcd.	Exptl.
1.33170	1.347	1.32275	1.305	1.31434	1.260
1.29300	1.315	1.28430	1.275	1.27614	
1.23862	1.262	1.23030	1.226	1.22247	1.185
1.37225	1.372	1.36303	1.323	1.35436	1.276
1.33447	1.336	1.32550	1.291	1.31707	
1.28010	1.292	1.27149	1.250	1.26340	1.203
1.38239	1.363	1.37310	1.310	1.36437	
1.32249	1.319	1.31360	1.273	1.30524	1.220
1.25613	1.279	1.24769	1.200	1.23975	1.200
1.29115	1.312	1.28247	1.273	1.27432	1.229
1.30498	1.326	1.29620	1.287	1.28796	1.242
1.32157	1.341	1.31268	1.300	1.30434	1.255
1.34092	1.361	1.33190	1.319	1.32344	1.274
1.29392	1.303	1.28522	1.260	1.27705	
1.33263	1.340	1.32367	1.295	1.31525	
1.34645	1.352	1.33740	1.308	1.32889	
1.36488	1.369	1.35570	1.323	1.34709	
1.38331	1.387	1.37401	1.341	1.36528	
1.39437	1.381	1.38500	1.331	1.37619	1.276
1.41280	1.397	1.40331	1.345	1.39438	1.290
1.43216	1.414	1.42253	1.360	1.41348	1.304

$P_2 = 1517.8 \text{ atm}$		$P_2 = 2069.4 \text{ atm}$	
Calcd.	Exptl.	Calcd.	Exptl.
1.03568	1.00503		
1.01423	0.98732	1.01031	0.97035
1.99650	0.97210	0.99266	0.95607
1.98005	0.95814	0.97627	0.94284
1.96746	0.94414	0.46373	0.93091
0.88774	0.86479	0.88431	0.85009
0.89796	0.87593	0.89449	0.86159
0.90875	0.88774	0.90524	0.87409
0.92105	0.90140	0.91750	0.88766
0.93229	0.93091	0.92869	

similarly

$$V_A(T_1, P_2) \propto f(1/P_2) \quad (41)$$

or

$$v_A(T_1, P_2) \propto f(1/P_2) \quad (42)$$

$$\frac{V_A(T_1, P_2)}{V_A(T_1, P_1)} = \frac{v_A(T_1, P_2)}{v_A(T_1, P_1)} = f\left(\frac{P_1}{P_2}\right) \quad (43)$$

or

$$v_A(T_1, P_2) = v_A(T_1, P_1) f(P_1/P_2) \quad (44)$$

or

$$V_A(T_1, P_2) = V_A(T_1, P_1) f(P_1/P_2) \quad (45)$$

Ozawa et al. [107] and Gibson and Loeffler [108] have determined the specific volume  $v_A(T, P)$  of ethanol, methyl, cyclopentane, *n*-heptane, chlorobenzene, bromobenzene, nitrobenzene and aniline as a function of temperature and pressure. It was found that the specific volumes  $v(T_1, P_2)$  of these compounds satisfy the relation (see Table 6)

$$\frac{v(T_1, P_2)}{v(T_1, P_1)} = \left(\frac{P_1}{P_2}\right)^{0.0125} \quad (46)$$

where  $P_1$  and  $P_2$  are expressed in atm, and while  $P_1 = 1$  atm,  $P_2$  had the values 99, 393, 687, 1118 and 1962 atm. The  $v(T_1, P_2)$  data for chlorobenzene, bromobenzene, nitrobenzene and aniline were computed from the various parameters given by Gibson and Loeffler [108] for these compounds while those of the remaining compounds were taken from the literature [107].

If expression (46) is assumed to hold even for binary mixtures it should be possible to determine the molar or specific volume  $V(T_1, x, P_2)$  or  $v(T_1, x, P_2)$  of a binary mixture when  $V(T_1, x, P = 1 \text{ atm})$  or  $v(T_1, x, P = 1 \text{ atm})$  data are available.

Ozawa et al. [107] have determined the specific volumes  $v(T, x, P)$  of [(1 - *x*) ethanol + *x* methylcyclopentane], [(1-*x*) *n*-heptane + *x* ethanol] and [(1 - *x*) methylcyclopentane + *x* *n*-heptane mixtures as a function of *T* and *P*. If  $v(T, x, P = 1 \text{ atm})$  data for these mixtures are taken from the literature [106], then from eqn. (46)

$$v(T, x, P_2) = v(T, x, P = 1 \text{ atm}) \left[ (1/P_2)^{0.0125} \right] \quad (47)$$

Such  $v(T, x, P_2)$  values at  $T = 298.2, 323.2$  and  $348.2$  K and  $P_2 = 99, 393, 687, 1178$  and  $1962$  atm are recorded in Table 7 and are also compared with their corresponding experimental values [107,108]. It is quite evident that the calculated  $v(T, x, P_2)$  values compare very well with the corresponding experimental values; the maximum difference being 5%.

Takagi [105] has determined the density at 298.15 K of [(1 - *x*) benzene +

$x$  aniline] and  $[(1 - x)$  chlorobenzene +  $x$  aniline] mixtures from the pressure dependence of ultrasonic speeds in them. It would now be interesting to see how eqn. (46) describes the  $v(T = 298.15 \text{ K}, P_2)$  data of these mixtures when  $v(T = 298.15 \text{ K}, P_1 = 552.6 \text{ atm})$  data are known. Such  $v(T = 298.15, P_2 = 1, 1032.6, 1517.8$  and  $2069.4 \text{ atm})$  values are recorded in Table 7 and are also compared with their corresponding experimental values; again the agreement is good [maximum difference between the calculated and the experimental  $v(T, x, P_2)$  values [105] is about 5%].

The present approach thus provides a convenient means to (i) evaluate  $H^E(T_1, x)$  or  $V^E(T_1, x)$  data, (ii) study the effect of temperature and pressure on  $H^E(T_1, x)$  or  $V^E(T_1, x)$  for any kind of binary mixture of non-electrolytes when  $H^E(T_1, x)$  or  $V^E(T_1, x)$  data for the mixture at two compositions at  $T_1$  are available. This approach also enables the evaluation of specific volumes  $v(T_1, x, P_2)$  of pure components as well their binary mixtures when  $v(T_1, x, P_1)$  data are available.

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