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1. Introduction

Differential thermal analyses (DTA) are often used to determine heats of reaction/transformation, and to investigate reaction/transformation kinetics quantitatively as function of the heating/cooling rate [1,2]. To this end the DTA facility used first has to be calibrated with respect to the values of the heat capacity and the temperature. Moreover, and in particular for the analysis of reaction/transformation kinetics, the measurement signal has to be desmeared, since the measurement signal is smeared due to thermal lag [3], which affects the peak position and the peak shape.

Usually the heat-capacity calibration of isochronal (i.e. applying a constant heating/cooling rate) DTA is performed by calculating the apparent molar heat capacity of a sample, as follows. The temperature difference of a piece of calibration material with a well-known heat capacity and a reference cell is measured and it is assumed that this temperature difference is proportional to the heat capacity of the calibration specimen. In this method the smearing of the measurement signal over time is neglected [3]; because of this the determined heat capacity is an "apparent" heat capacity. The effect of smearing plays a significant role when the heat capacity changes drastically with temperature as for example around the Curie temperature.

ABSTRACT

[A previously re](http://www.sciencedirect.com/science/journal/00406031)ported calibration and desmearing method for a differential thermal a ratus applicable to heating and cooling was successfully modified to be used in the region (up to 1570 K). The method requires knowledge of parameters, which have a p the heat-flux model appropriate for the DTA apparatus. Values for these physical para mined by calibration. As calibration materials Mo (exhibiting a smooth variation of temperature) and Co (non-monotonic change of specific heat upon the ferro- to param and vice versa) were employed. Experimental measures to improve the reproducibility © 2008 Elsevier B.V.

> Common practice for the temperature calibrat involves the melting of pure materials $[4-6]$. The determined melting of pure ing temperatures are equated to the literature values temperature calibration has been performed. No ture calibration has to be performed for each hea

> A standard technique to desmear a DTA meas to use a temperature filter with parameters whi ical meaning $[8-10]$. Desmearing procedures wh mode of operation and the experimental setup of typically very complex and in addition they are isochronal *heating* modes [3,11].

The present work is based on previous work [3], where a combined temperature and heat-call and desmearing method was developed for DT. applicable to heating and cooling experiments. heat-flux model of the DTA with parameters wh dent of the heating/cooling rate applied. This mod applied successfully up to maximally $1100K[3]$ particular, the ferro- to paramagnetic transitio determination of the model parameters. A ferrotransition, occurring at the Curie temperature, ⁷ the combined calibration and desmearing meth a tra[nsition](#page-4-0) is non-monotonic (i.e. the heat capacity ity at the Curie temperature) and consequently stra In the present work the model was further developed for application cation to higher tempera[ture](#page-4-0)s of up to 1570 K, by to paramagnetic transition of cobalt ($T_{\rm C}^{\rm Co}=1396$

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of iron ($T_{\rm C}^{\rm Fe}$ = 1043 K). Thereby, the quantitative investigation of reaction/transformation kinetics and the quantitative determination of heats of reaction/transformation have become possible in the high-temperature region.

2. Basis of the method

2.1. Heat flux model

A DTA apparatus measures the temperature difference between a sample and reference cell upon heating/cooling. The experimental setup of the sample measurement cell is shown in Fig. 1. The sample and the reference cells are identical and are placed symmetrically with respect to each other in the furnace; the reference cell is empty (see Fig. 1). From the furnace wall the heat is transported to the components of the sample measurement cell and the reference cell, and, depending on the heat capa[citie](#page-4-0)s and the thermal resistances of the single components, heat transport also occurs between neighbouring components.

All components of the measurement cell are metallic (i.e. they have a small thermal resistance) except for the inner [samp](#page-4-0)le pan. The inner sample pan normally consists of inert, ceramic material (here Y_2O_3) to avoid chemical reactions between the outer sample pan (here Pt) and the sample at elevated temperatures.

The heat-transport characteristics of the sample measurement cell, s, and the reference cell, r, can be described using a heat-flux model of the DTA apparatus which consists of a limited number of heat resistances *R* and heat capacities *C* (cf. Fig. 2 in Ref. [3]). The heat, q , fluxes to the elements, t_r (thermocouple reference cell), r (reference cell), t_s (thermocouple sample cell) and s (sample measurement cell) (cf. Fig. 2 in Ref. [3]), can be described by the following equations [3]:

$$
\frac{dq_{t,r}}{dt} = \frac{T_f - T_{t,r}}{R_t} - \frac{T_{t,r} - T_r}{R_s} = C_{p,t} \frac{dT_{t,r}}{dt}
$$
(1)

$$
\frac{\mathrm{d}q_{\mathrm{r}}}{\mathrm{d}t} = \frac{T_{\mathrm{t},\mathrm{r}} - T_{\mathrm{r}}}{R_{\mathrm{s}}} = C_{p,\mathrm{r}} \frac{\mathrm{d}T_{\mathrm{r}}}{\mathrm{d}t} \tag{2}
$$

$$
\frac{\mathrm{d}q_{t,s}}{\mathrm{d}t} = \frac{T_f - T_{t,s}}{R_t} - \frac{T_{t,s} - T_s}{R_s} = C_{p,t} \frac{\mathrm{d}T_{t,s}}{\mathrm{d}t}
$$
(3)

$$
\frac{dq_s}{dt} = \frac{T_{t,s} - T_s}{R_s} = (C_{p,s} + C_{p,r}) \frac{dT_s}{dt}
$$
 (4)

where T_f denotes the temperature of the furnace wall. T_s and T_r are the temperatures of the sample cell, s, and the reference cell, r (cf. Fig. 2 in Ref. [3]), respectively. $T_{t,s}$ and $T_{t,r}$ atures of the thermocouples of the sample ce cell, t_r , respectively. $C_{p,s}$, $C_{p,r}$ and $C_{p,t}$ are the h sample, of the reference cell and of the thermo surroundings; t is the time. The measured variables perature of the thermocouple of the referene temperature difference of the thermocouples and the sample cell: $\Delta T_{t,s}$ = $T_{t,s}$ – $T_{t,r}$. The ident t_r and t_s are not calibrated for absolute temp tion. Hence, a temperature deviation of the the which is taken temperature and heating rate be incorporated in the analysis.

The DTA facility can thus be described by fi cooling-rate independent physical parameters tance, R_t , between the furnace and the thermod capacity of the thermocouple and its direct sur the heat capacity of the reference cell, $C_{p,r}$; (iv) between sample [measu](#page-4-0)rement/reference cell R_s ; and (v) the thermocouple temperature shi Ref. [3]).

According to Kempen et al. [3] these five DT. determined by measuring two calibration mate

Fig. 2. Consecutive runs with empty sample measureme the conventional experimental setup (6 runs) and (ii) aft fused onto the sample stage (2 runs); heating/cooling rate

perature hysteresis [13,14] (no mass transport involved), so that the Curie temperature is heating- and cooling-rate independent [15].

The determination of the instrumental DTA parameters was done on the basis of literature data for the temperature dependent molar heat capacity of molybdenum, C_{p,Mo}, (cf. Section 2.2) and for the Curie temperature of Co (cf. Section 2.3) as follows (for details of the fit procedure, see Ref. [3]). Using literature data for *Cp*,Mo as well as the DTA data recorded from the Mo measurements, first the temperature dependent parameter R_t was calculated (for each heating and cooling rate). Next, applying Eqs. (3) and ([4\),](#page-4-0) [th](#page-4-0)e calculated (temperature dependent) parameter *R*^t (averaged over all heating/cooling rates) and the recorded DTA data from the Co measurements, the molar heat capacity of Co, C_{p,Co}, was calculated. This calculation of C_{p,C_0} is based on a complex fit procedure during which the fit parameters $C_{p,t}$, $C_{p,r}$ and R_s are varied according to a simplex procedure [16], such that the $C_{p,Co}$ curves for different heating/cooling rates coincide. Finally, $\Delta T_{\rm tc}$ was calculated as the difference of the calculated value and the literature value of the Curie temperature of cobalt. The thus obtained model description of the DTA apparatus can be validated by comparing the desmeared molar heat capacity of cobalt, $C_{p,Co}$, as function of temperature with literature data (cf. Section 2.3).

2.2. Cp of molybdenum

Molybdenum has a molar heat capacity [that ch](#page-1-0)anges smoothly, monotonically with temperature. Temperature dependent values for [the](#page-4-0) [m](#page-4-0)olar heat capacity of molybdenum C_{p,Mo} were adopted as given in Ref.[17]. The uncertainties in the heat-capacity values were estimated not to exceed ± 1.0 %. The discrete values for $C_{p,Mo}$ from Ref. [17] can be d[escribed](#page-1-0) [by](#page-1-0) [a](#page-1-0) continuous [fifth-o](#page-1-0)rder polynomial. The difference between the data points and the polynomial curve does not exceed $\pm 0.1\%$ and consequently can be neglected. It thus was obtained:

$$
C_{p,Mo} = A_0 + A_1 T + A_2 T^2 + A_3 T^3 + A_4 T^4 + A_5 T^5
$$

for 273.15 K $\leq T \leq$ 1750 K (5)

with $A_0 = 17.1694 \text{ J} \text{ mol}^{-1} \text{ K}^{-1}$ $A_0 = 17.1694 \text{ J} \text{ mol}^{-1} \text{ K}^{-1}$ $A_0 = 17.1694 \text{ J} \text{ mol}^{-1} \text{ K}^{-1}$, $A_1 = 0.03515 \text{ J} \text{ mol}^{-1} \text{ K}^{-2}$, $A_2 =$ [−]5.35826 [×] ¹⁰−⁵ J mol−¹ ^K−3, *^A*³ = 4.40757 [×] ¹⁰−⁸ J mol−¹ ^K−4, *^A*⁴ ⁼ -1.70917×10^{-11} J mol⁻¹ K⁻⁵, $A_5 = 2.64523 \times 10^{-15}$ J mol⁻¹ K⁻⁶.

2.3. Cp of cobalt

A number of publications provide data for the molar heat capacity of Co, $C_{p,{\rm Co}}$, and the Curie temperature of cobalt, $T_{\rm C}^{\rm Co}$ [18–25]. The data for C_{p,C_0} adopted in this work correspond to those taken up in the SGTE database [18] and to those given by Fernández Guillermet [19] who made a critical evaluation of data for the thermodynamic properties of cobalt (cf. Section 4).

measurement to avoid diffusion bonding with the Fig. 1). This lift up and the following putting down reproducibility of the measurements, since the (between the sample stage and the Pt pans is chaing the Pt pans cannot be placed exactly at the same $\frac{1}{2}$ (see Fig. 2).

Therefore the Pt pans were diffusion bonded or so that position and contact area do not change in a utive measurements. Thus, only a transfer of the in necessary for the exchange of samples in a series (see Fig. 1).

The fusing of the Pt pans with the sample stag after placing the Pt pans exactly in the middle of Afterwards consecutive calibration DTA runs wer heating up to 1720 K; the calibration runs were r subsequent runs showed no deviations from the

The improvement of the reproducibility of the by diffusion bonding of the Pt pans is obvious shown in Fig. 2. Without this modification of the measurement of the m setup (i.e. [the fusi](#page-1-0)ng of the Pt pans) the required the measurements for the calibration and desmea the high-temperature region would not have bee

3.2. DTA runs

For the DTA measurements disc shaped Co (purity 9). Mo (purity 99.95%) samples with a diameter of a a thickness of about 1.4 mm were cut from rods pure metals. Subsequently the samples were gro to clean the surface of the samples. For the last $3 \,\rm \mu m$ diamond paste was used.

Three subsequent runs were performed for eac rate applied (here: 10, 15 and 20 K/min):

- I. empty measurement;
- II. cobalt sample;
- III. molybdenum sample.

For every heating/cooling rate a new cobalt sample was used. During the measurement the unavoidably slightly oxidised at the surface. To en dation does not affect the DTA measurement sig were carried out for the cobalt and molybdenum and the results were identical to the results of the

If the sample cell and the reference cell would same setup, the empty run should cause a zero should be no temperature difference between surement cell and the reference cell. However, difference in the setups for sample measurement cell occurs, and therefore the measurement signal

(cf. Section 2.2): $C_{p,Co}^{\text{app.}} = C_{p,M_0}(\Delta T_{t,Co}/\Delta T_{t,M_0})$. Results are shown in Fig. 3.

The true heat capacity is independent of heating and cooling rate. However, the apparent molar heat capacity of Co, determined as described above, strongly depends on the heating/cooling rate; also the ferro- to paramagnetic transition temperature shows a heating/cooling-rate dependence (see Fig. 3). These heating-rate and cooling-rate dependencies are caused by smearing due to thermal lag. [The oft](#page-1-0)en used, simple calibration procedure, that provides the basis for the results shown in Fig. 3, is inadequate.

Application of the present calibration and desmearing method based on the heat-flux model (Section 2.1) led to results for the molar heat capacity as function of temperature shown in Fig. 4. Evidently, the desmearing procedure leads to coincidence of the curves pertaining to the different heating and cooling rates and thus an apparent thermal hysteresis of the ferro- to paramagnetic transition does not occur, as it should be (see also Fig. 5). The small remaining differences between the various molar heat capacity curves are within the experimental accuracy of the DTA measurements.

The average of the molar heat capacity curves of Co, C_{p,C_0} , (calculated from the plots in Fig. 4) can be compared with corresponding literature data (cf. Section 2.3) in Fig. 5. It follows that the molar heat capacity curve determined in this work agrees very well with the literature data.

The values obtained for the instrumental DTA (fit) parameters $C_{p,t}$, $C_{p,r}$, R_s and ΔT_{tc} (as listed in Section 2.1 and determined as described immediately above) have been gathered in Table 1. The values determined for these physical parameters as determined by Kempen et al. [3], for the same DTA apparatus but using differ-

Fig. 3. Apparent molar heat capacity of Co, $C_{p,Co}^{app}$, for three different heating and cooling rates; calculated as described at the beginning of Section 4.

Fig. 4. Molar heat capacity of Co, C_{p,C_0} , for different heating rection for thermal smearing according to the heat flux m

ent calibration materials and pertaining to a di range, have also been given in Table 1.

The values determined here for $C_{p,t}$ and $C_{p,r}$ and of magnitude as those determined in Ref. [3 heat resistance R_s (between sample and thermo smaller than the value determined in Ref. [3]. stood as a consequence of (i) the fusing of the P stage in the current work (so the thermal contact gets better) and and (ii) the increasing contribution of radiation to increasing temperature.

The increasing contribution of radiation to increasing temperature also explains the decre

Fig. 5. Molar heat capacity of Co, $C_{p,Co}$, (average calculated comparison with literature data [20,21,23,24]. The literatur the temperature axis such that the Curie temperatures [18,19].

Table 1

Values for the instrumental DTA parameters as determined in the instrumental DTA parameters as determined parison with the values for these parameters determined apparatus, but at a lower temperature range

Fig. 6. The heat resistance R_t between the furnace wall and the thermocouples as a function of temperature.

tance *R*^t (between the furnace wall and the thermocouples) with increasing temperature (see Fig. 6). In particular, the dependence of R_t on temperature, for the temperature range investigated in Ref. [3] is, by extrapolation, very well compatible with the results obtained here at considerably higher temperatures.

5. Conclusions

- Calibration and desmearing of differential thermal analysis scans (temperature difference of sample and reference pans as function of temperature) – upon heating and cooling – is possible in the high-temperature region (up to, at least, 1570 K).
- By fusing of the (Pt) sample and reference pans on the sample stage the reproducibility of the measurements is improved considerably. Without this modification of the measurement setup the required reproducibility for the calibration and desmearing procedure in the high-temperature region cannot be achieved.
- try, Springer-Verlag, Berlin, Heidelberg, 1996.
[2] F. Liu, F. Sommer, C. Bos, E.J. Mittemeijer, Int. Mater. Rev.
- [3] A.T.W. Kempen, F. Sommer, E.J. Mittemeijer, Thermoch 21.
- [4] E. Gmelin, S.M. Sarge, Thermochim. Acta 347 (2000) 9.
- [5] G.W.H. Höhne, H.K. Cammenga, W. Eysel, E. Gmelin, V mochim. Acta 160 (1990) 1.
- [6] H.K. Cammenga, W. Eysel, E. Gmelin, W. Hemminger, Thermochim. Acta 219 (1993) 333.
- [7] J.D. Menczel, J. Therm. Anal. Cal. 49 (1997) 193.
- [8] H.-J. Flammersheim, N. Eckardt, W. Kunze, Thermochim.
- [9] S. Wiesner, E. Woldt, Thermochim. Acta 187 (1991) 357.
- [10] G.P. Krielaart, S. van der Zwaag, Mater. Sci. Technol. 14 (1
- [11] W. Poessnecker, Thermochim. Acta 187 (1991) 309. [12] Netzsch, Instrument Manual Netzsch DSC 404C Pegasus,
- [13] E. Kneller, Ferromagnetism, 1st edition, Springer, Berlin,
- [14] R.M. Bozorth, Ferromagnetism, 2nd edition, D. van N 1951.
- [15] Y.H. Jeong, D.J. Bae, I.K. Kwon, I.K. Moon, J. Appl. Phys. 70 [16] W.H. Press, S.A. Teukolsky, W.T. Vetterling, B.P. Flannery,
- C, Cambridge University Press, NY, 1997.
- [17] J.P. Cali, (NIST Database 1977) Standard Reference Mater
- [18] A.T. Dinsdale, Calphad 15 (1991) 317.
- [19] A. Fernández Guillermet, Int. J. Thermophys. 8 (1987) 48
- [20] V.E. Peletskii, E.B. Zaretskii, High Temp.-High Press. 13 (1 [21] M. Braun, R. Kohlhaas, Z. Naturforsch. A 19a (1964) 663.
- [22] M. Braun, R. Kohlhaas, Phys. Status Solidi 12 (1965) 429.
- [23] A.S. Normanton, Met. Sci. 9 (1975) 455.
- [24] Y.A. Kraftmakher, T.Y. Romashina, Sov. Phys.-Sol. State 8
- [25] E.A. Owen, D. Madoc Jones, Proc. Phys. Soc. Lond. B 67 (1
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