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# Thermodynamic description of [the](http://www.elsevier.com/locate/tca) [Au–Ag–Ge](http://www.elsevier.com/locate/tca) [ternar](http://www.elsevier.com/locate/tca)y system

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### **1. Introduction**

## High-Pb containing solders (e.g. Pb–5 wt.% Sn) as hightemperature solders have been widely used in electronic packaging industries. However, Pb is harmful to both the environment and human health. The development of high-temperature Pb-free solders to replace the conventional high-Pb containing solders has become an important issue now [1–3]. Despite the high price, Aubased alloys such as Au–Sn, Au–Sb, Au–Si and Au–Ge eutectic alloys are useful for bonding applications [4–11]. Especially, Au–20 wt.% Sn eutectic alloy has been used widely in high power electronic and optoelectronic devices because it has superior resistance to corrosion and high el[ectrical](#page-6-0) and thermal conductivity as well as high mechanical strength [3–9]. Recently, Au–Ge-based alloys are attractive as a great pot[ential](#page-6-0) [can](#page-6-0)didate for high temperature Pbfree solders in the electronic and optoelectronic packaging [10,11]. However, to reduce the costs of Au-based solders, the alloying elements including Ag, Al, Bi, Cu, Ga, Ge, In, Sb, Zn, etc. may be added to repla[ce](#page-6-0) [a](#page-6-0) [pa](#page-6-0)rt of the Au. In order to understand better the role of alloying elements and to develop new Au-based solders, knowledge of the precise phase dia[grams](#page-6-0) [an](#page-6-0)d reliable thermodynamic properties of the Au-based alloys is indispens[-](#page-6-0)

#### **ABSTRACT**

The Ag–Ge binary system has been assessed thermodynamically using the CALPHAD method through the Thermo-calc® software based on the available experimental information from the published literature. The solution phases including liquid, fcc A1(Au,Ag), and diamond A4(Ge), were modeled as substitutional solutions and their excess Gibbs energies were expressed by the Redlich–Kister polynomial. On the basis of the previous assessments of the Au–Ag and Au–Ge binary systems, the thermodynamic description of the Au–Ag–Ge ternary system has been performed. The liquidus projection and several vertical sections of this ternary system have been calculated, which are in good agreement with the reported experimental data.

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able. Recently, thermodynamic descriptions of many binary and ternary systems such as Au–Pb, Au–Al, Au–In, Au–Zn binary systems and Au–Ag–Si, Au–Ag–Sn, Au–Bi–Sb, Au–Ge–Sn, Au–Ge–Sb, Au–Ge–Si, Au–Ag–Pb, Au–Sb–Si, Au–In–Sn, Au–In–Sb, Au–Si–Sn and Au–Co–Sn ternary systems have been developed by Wang, Liu and Jin [12–27] using the CALPHAD method [28,29]. As an essential contribution to establish a consistent and available thermodynamic database of the multicomponent Au-based alloys, the purpose of the present work was to obtain a thermodynamic description of the Au–Ag–Ge ternary system.

[Am](#page-6-0)ong the three binary su[b-systems](#page-6-0), the Au–Ag and Au–Ge binary systems have been well assessed thermodynamically by Hassam et al. [30] and Wang et al. [16], respectively. The calculated phase diagrams of the Au–Ag and Au–Ge binary systems are shown in Figs. 1 and 2, respectively. Thermodynamic parameters for the Gibbs energies of various phases in the Au–Ag and Au–Ge binary systems obtained by Hassam et al. [30] and Wang et al. [\[16\]](#page-6-0) were employed [direc](#page-6-0)tly in the present optimization and calculation. The Ag–Ge binary system was reviewed previously by [Olesinski](#page-1-0) [and](#page-1-0) Abbaschian [31] and was optimized by Chevalier [32], which can reproduce most experimental information on thermodynamic properties and phase [bound](#page-6-0)aries. However, the lattice stabilities of the elements Ag and Ge used in Ref. [32] are different from those proposed recently by Dinsdale [33]. In order to achieve the co[mpatib](#page-6-0)ility of thermodynamic databases in the multi-component systems, thermodynamic parameters of various phases in the Ag–Ge binary system were reassessed firstly in the present work. Then, based on the a[lready](#page-6-0) [optim](#page-6-0)ized Au–Ag

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<span id="page-1-0"></span>

**Fig. 1.** Calculated phase diagram of the Ag–Au binary system by Hassam et al. [30].

and Au–Ge binary systems, the Au–Ag–Ge ternary system w[as](#page-6-0) optimized further using the CALPHAD method [28,29] through Thermo-calc® software [34]. Finally, thermodyna[mic pa](#page-6-0)rameters describing various phases in this ternary system were obtained.

## **2. Experimental information**

## 2.1. The Ag–Ge binary system

In the Ag–Ge binary system, there are three condensed phases including liquid, fcc A1(Ag) and diamond A4(Ge), which form a eutectic reaction. Using thermal analysis, Briggs et al.[35], Maucher [36], Hume-Rothery et al. [37], Predel and Bamlstahl [38] and Hassam et al. [39] determined the temperature and composition of this eutectic reaction as given in Table 1. The experimental data [35–39] on this eutectic reaction are in good agree[ment w](#page-6-0)ith each other and were accepted in the present work.

Phase boun[daries](#page-6-0) of the liquid phase [were](#page-6-0) [m](#page-6-0)easured by Briggs [et](#page-6-0) [al](#page-6-0). [35] and Maucher [36] by means of ther[mal analy](#page-6-0)sis in the whole composition range. Predel and Bamlstahl [38] determined



**Fig. 2.** Calculated phase diagram of the Au–Ge binary system by Wang et al. [16].

**Table 1** Eutectic reaction in the Ag–Ge binary system.

Reaction	T(K)	Composition $(x_{Co}^L)$	Reference
$L \leftrightarrow fcc \cdot A1(Ag) + diamond \cdot A4(Ge)$	923	0.260	[35]
	922	0241	$[36]$
	924		$[37]$
	923	0.240	$[38]$
	923.5	0.240	$[39]$
	923.4	0.249	$[32]$
	921	0.249	This work

the liquidus in the composition range from 6[4 at.%](#page-6-0) Ag to 82 at.% Ag using thermal analysis. The experimental resu[lts in](#page-6-0) Refs. [35,36,38] are generally consistent with each other and were used in the present optimization.

The solubility of Ge in the fcc A1(Ag) phase below the eutectic temperature was determined by Owen and Rowlands [40] through lattice parameter measurements using X-ray [powder](#page-6-0) [me](#page-6-0)thod. Pollock [41] reported the composition of the fcc\_A1(Ag) phase at room temperature (about 300 K) from thermoelectric measurements. The experimental information on the solubility of Ag in diamond A4(Ge) could not be found in t[he](#page-6-0) [lite](#page-6-0)rature. Therefore, the solubility of Ge in fcc A1(Ag) was taken into account, while the solubility of Ag in diamond A4(Ge) was neglected in the present optimization.

The enthalpies of mixing of liquid Ag–Ge alloys referred to liquid Ag and liquid Ge were measured by Catanet et al. [42,43] at 1280 K using calorimetry method. Batalin et al. [44] determined the enthalpies of mixing of liquid Ag–Ge alloys at 1430 K by means of the electromotive force (EMF) method. The experimental results obtained by Castanet et al. [42,43] show good agreement and are also compatible with the experimental data [of](#page-6-0) [Batalin](#page-6-0) et al. [44], although their experimental values ar[e](#page-6-0) [sligh](#page-6-0)tly discrepant due to the different measured temperatures. It should be noticed that the enthalpies of mixing determined by Batalin et al. [44] are deduced from the EMF [measurem](#page-6-0)ents. The enthalpies of mixing measured directly by Catanet et al. [42,43] through the calo[rimetr](#page-6-0)ic experiments are much more reliable and were thus given larger weights than the data of Batalin et al. [44] in the present optimization.

Activities of Ag in the liquid Ag–G[e](#page-6-0) [alloy](#page-6-0)s were determined by Batalin et al. [44] at 1430 K using the EMF method, by Eremenko et al. [45] at [1378](#page-6-0) [K](#page-6-0) [th](#page-6-0)rough the vapour measurements and by Martin-Garin et al.[46] at 1250 K and Oktay [47] at 1416 K using the Knudsen mass sp[ectrom](#page-6-0)etry technique. The activities of Ag determined by Batalin et al. [44], and Martin-Garin et al. [46] are in good a[greeme](#page-6-0)nt and are also consistent with the experimental values of [E](#page-6-0)remenko et al. [45] in the Ag-rich part, although their experimental tem[peratu](#page-6-0)res are different. [Howev](#page-6-0)er, the experimental data of Batalin et al. [44], Eremenko et al. [45] and Martin-Garin et al. [46] differ consi[derab](#page-6-0)ly from the scattered [experim](#page-6-0)ental data reported by Oktay [47], especially in the Ag-rich part. On the other hand, Ere[menko](#page-6-0) et al. [45] and Martin-Garin et al. [46] determined the activities of Ge in the liquid Ag–Ge alloys at 1250 K and 1378 K, r[espect](#page-6-0)ively. The activ[ities](#page-6-0) [o](#page-6-0)f Ge determined by [Ereme](#page-6-0)nko et al. [45] and Martin-Garin et al. [46] show good agreement. Consider[ing](#page-6-0) [th](#page-6-0)e accordance of most experimental data, the measured values in Refs. [\[44](#page-6-0)–46] were taken into a[ccoun](#page-6-0)t, while the reported data by Oktay [47] at 1416 K are scattered and thus were given up in the present optimiza[tion.](#page-6-0)

#### [2.2. Th](#page-6-0)e Au–Ag–Ge ternary system

[T](#page-6-0)he thermodynamic properties and phase relations of the Au–Ag–Ge ternary system were investigated experimentally by several authors [39,48–51]. Prince et al. [52] and Borzone et al. [53] reviewed this ternary system when compiled phase diagrams of

<span id="page-2-0"></span>Au-based alloys. According to the experimental results in Ref. [39], no stable ternary compound was found in the Au–Ag–Ge ternary system.

The thermodynamic properties of liquid alloys in the Au–Ag–Ge ternary system were investigated by the different researchers [48–51]. Hassam and Gaune-Escard [48] as [well](#page-6-0) [a](#page-6-0)s Hassam et al. [49] measured the enthalpies of mixing of the liquid Au–Ag–Ge ternary alloys at 1373 K along the different sections –  $x_{Ag}:x_{Ge} = 1:3$ ,  $x_{Ag}:x_{Ge} = 1:1$ ,  $x_{Ag}:x_{Ge} = 3:1$  and  $x_{Au}:x_{Ge} = 1:3$ ,  $x_{\text{Au}}$ : $x_{\text{Ge}}$  = 1:1,  $x_{\text{Au}}$ : $x_{\text{Ge}}$  = 3:1 by the direct reaction calorimetry. At the same time, Castanet [50] [repor](#page-6-0)ted the enthalpies of formation [of](#page-6-0) the liquid Au–Ag–Ge ternary alloys at 1348 K. The experimental values measured by Hassam and Gaune-Escard [48], Hassam et al. [49] and Castanet [50] are in reasonable agreement with each other, although there is a small temperature difference (25 K) in their experi[ments.](#page-6-0) In addition, the activities of Ag in the ternary liquid Au–Ag–Ge alloys at 1416 K were investigated by Yu and Howard [51] using the Knudsen cell-mas[s](#page-6-0) [spec](#page-6-0)trometer method. However, t[he](#page-6-0) [exp](#page-6-0)erimental values for the activities of components were not given in the original publication. Therefore, the experimentally measured enthalpies of mixing of the liquid Au–Ag–Ge ternary alloys in Refs. [48,49] were employed only in the present [opt](#page-6-0)imization.

As for the phase relations of the Au–Ag–Ge ternary system, Hassam et al. [39] determined the three vertical sections: Ag<sub>0.25</sub>Au<sub>0.75</sub>–Ge, Ag<sub>0.50</sub>Au<sub>0.50</sub>–Ge and Ag<sub>0.75</sub>Au<sub>0.25</sub>–Ge using differential thermal analysis. Based on these experimental results, the liquidus projection of this ternary system was established. The experimental information [39] was taken into account in the present o[ptimi](#page-6-0)zation.

#### **3. Thermodynamic models**

#### 3.1. Pure elements

The stable forms of the pure elements at 298.15 K and 1 bar are chosen as the reference states. The Gibbs energy for the pure element  $i$  in  $\phi$  status is given as:

$$
{}^{0}G_{i}^{\phi}(T) = G_{i}^{\phi}(T) - H_{i}^{SER} = a + b \cdot T + c \cdot T \ln T + d \cdot T^{2} + e \cdot T^{3}
$$

$$
+ f \cdot T^{-1} + g \cdot T^{7} + h \cdot T^{-9}
$$
(1)

where  $H_i^{\rm SER}$  is the enthalpy of the element  $i$  in its standard reference state (SER) at 298.15 K and 1 bar; T is the absolute temperature in K;  $G_i^\phi(T)$  is the Gibbs energy of the element  $i$  with structure  $\phi;{}^0G_i^\phi(T)$ is the molar Gibbs energy of the element  $i$  with the structure of  $\phi$ referred to the enthalpy of its stable state at 298.15 K and 1 bar. In the present work, the Gibbs energies of the elements Au, Ag and Ge,  $^{0}G^{\phi}_{\rm Au}(T)$ ,  $^{0}G^{\phi}_{\rm Ag}(T)$  and  $^{0}G^{\phi}_{\rm Ge}(T)$  are taken from the SGTE (Scientific Group Thermodata Europe) database [33].

## 3.2. Solution phases

The substitutional sol[ution](#page-6-0) model is employed to describe the solution phases including liquid, fcc A1(Au,Ag), and diamond A4(Ge), respectively. The molar Gibbs energy of the solution phase  $\phi$  ( $\phi$  = liquid, fcc\_A1, and diamond\_A4) can be expressed as:

$$
G_m^{\phi} = \sum x_i^0 G_i^{\phi} + RT \sum x_i \ln(x_i) + {}^E G_m^{\phi}
$$
 (2)

where  ${}^{0}G_{i}^{\phi}$  is the molar Gibbs energy of the element *i* (*i* = Ag, Au, Ge) with the structure  $\phi$ ,  $x_i$  the mole fraction of component  $i$ ,  $R$  gas constant,  $T$  temperature in K,  $^{E}G_{m}^{\phi}$  the excess Gibbs energy. The excess Gibbs energy of phase  $\phi$  can be expressed with

**Table 2** Thermodynamic parameters for the Au–Ag–Ge ternary system.

Phase	Thermodynamic parameter <sup>®</sup>	Reference
Liquid (Ag, Au, Ge)	$^{(0)}L_{A\alpha A u} = -16042 + 1.14T$	[30]
	${}^{(0)}L_{\text{Ag,Ge}} = +7636.87 - 6.822T$	
	$^{(1)}L_{\text{Ag-Ge}} = -14500.14 + 5.761T$	This work
	$^{(2)}L_{Ag,Ge} = -7029.56$	
	${}^{(0)}L_{A11}{}_{Ge} = -18294.684 - 13.671T$	
	$^{(1)}L_{A11}$ <sub>Ce</sub> = -8894.639 - 6.339T	[16]
	$^{(2)}L_{A11\text{Ge}} = -2174.476 - 4.925T$	
	$^{(0)}L_{A\alpha A u,Ge} = -40000 + 5T$	
	$^{(1)}L_{Ag,Au,Ge} = -110000 + 35T$	This work
	$^{(2)}L_{A\alpha A u.Ge}$ = +35000 + 5T	
$fcc_A1(Ag,Au,Ge)$	${}^{(0)}L_{A\alpha A u} = -15599$	[30]
	${}^{(0)}L_{\text{Ag},\text{Ge}} = +5696.47 + 9.917T$	This work
	$^{(1)}L_{\text{Ag-Ge}} = -20237.27$	
	${}^{(0)}L_{\text{Aut},Ge} = +10198.859 - 23.114T$	[16]
diamond_A4 (Ge)	${}^{0}G_{\text{Ge}}^{\text{dia.}}$ cited from SGTE database	[33]

\* Note: Gibbs energies are expressed in J/mol. The lattice [stabil](#page-6-0)ities of the elements Au, Ag and Ge in liquid, fcc A1 and diamond A4 were given by Dinsdale [33].

Redlich–Kister–Muggianu expression [54,55]:

$$
{}^{E}G_{m}^{\phi} = x_{Ag}x_{Au} \sum_{j=0}^{n} {}^{(j)}L_{Ag,Au}^{\phi}(x_{Ag} - x_{Au})^{j} + x_{Ag}x_{Ge} \sum_{j=0}^{n} {}^{(j)}L_{Ag,Ge}^{\phi}(x_{Ag} - x_{Ge})^{j}
$$

$$
+ x_{Au}x_{Ge} \sum_{j=0}^{n} {}^{(j)}L_{Au,Ge}^{\phi}(x_{Au} - x_{Ge})^{j} + x_{Ag}x_{Au}x_{Ge}L_{Ag,Au,Ge}^{\phi}
$$
(3)

with

$$
^{(j)}L^{\phi}_{\text{Ag,Ge}} = A_j + B_j T \tag{4}
$$

$$
L_{Ag,Au,Ge}^{\phi} = x_{Ag}^{(0)} L_{Ag,Au,Ge} + x_{Au}^{(1)} L_{Ag,Au,Ge} + x_{Ge}^{(2)} L_{Ag,Au,Ge}
$$
 (5)

where  $A_j$  and  $B_j$  are parameters to be optimized in the present work.  ${}^{(j)}L^{\phi}_{\mathsf{Ag},\mathsf{Au}}$  and  ${}^{(j)}L^{\phi}_{\mathsf{Au},\mathsf{Ge}}$  are binary interaction parameters, which are taken directly from the Au–Ag and Au–Ge binary systems assessed by Hassam et al. [30] and Wang et al. [16], respectively. The ternary interactive parameters  $^{(j)}L_{\rm Ag, Au, Ge}$  are parameters to be optimized in the present work.



**Fig. 3.** Calculated phase diagram of the Ag–Ge binary system in the present work.

<span id="page-3-0"></span>

**Fig. 4.** Comparison of the calculated phase diagram of the Ag–Ge binary system with experimental data [35,36,38,40,41] in the present work.

## **4. Results and discussion**

Usin[g the lattice sta](#page-6-0)bilities of the elements Au, Ag and Ge compiled by Dinsdale [33], the model parameters for various phases in the Au–Ag–Ge ternary system was optimized using the PARROT module in the Thermo-calc® software package developed by Sundman et al. [34]. This module works by minimizing the square sum of the differences between experimental data and calculated values. In [the](#page-6-0) [op](#page-6-0)timization procedure, each set of experimental data is given a certain weight according to the reliability and compatibility of experimental data. It should be claimed that the weights of [much](#page-6-0) more reliable experimental data are larger than those of less ones during the optimization. For thermodynamic data, in general, the activity of a component determined by the EMF method are much more reliable and within a smaller experimental error t[han](#page-2-0) that determined by vapour pressure method, while the enthalpies of mixing of liquid alloys obtained directly by calorimetry are much more believable than that derived from indirect measurements (such as EMF). As for phase diagram data, it is better to use the mea-



 $1.0$ △ Martin et al. 1979, 1250 K 0.9 □ Batalin et al. 1971, 1430 K ♦ Oktay, 1993, 1416 K  $0.8$ Eremenko et al. 1963, 1378 K  $\star$  $0.7$ Activity, Ag  $0.6$  $0.5$  $0.4$  $0.3$  $0.2$  $0.1$ 0  $0.6$  $0.2$  $0.4$  $0.8$  $1.0$ Ω Mole fraction, Ag

Fig. 6. Calculated activity of Ag with the experimental data [44-47] at 1250 K (Ref. state: liquid Ag).

sured experimental data by thermal analysis method. The weights can be changed systematically during the optimization until most of experimental data is accounted f[or](#page-6-0) [withi](#page-6-0)n the claimed uncertainty limits. Thermodynamic parameters for all condensed phases in the Au–Ag–Ge ternary system used and obtained finally in the present work are summarized in Table 2.

## 4.1. The Ag–Ge binary system

Fig. 3 shows the calculated phase diagram of the Ag–Ge binary system. The compari[son](#page-2-0) [of](#page-2-0) [th](#page-2-0)e calculated phase diagram with the experimental data by Briggs et al. [35], Maucher [36], Hume-Rothery et al. [37], Predel and Bamlstahl [38], Hassam et al. [39], Owen and Rowlands [40] and Pollock [41] is presented in Fig. 4. The calculated liquidus is in agreement with the experimental data [35,36,38]. The calculated temperature and composition of the eutectic reaction agree we[ll](#page-6-0) [with](#page-6-0) the exp[erime](#page-6-0)ntal data [35–39] an[d](#page-6-0) [the](#page-6-0) [p](#page-6-0)reviously assessed va[lues](#page-6-0) [32] as given in [Table](#page-6-0) 1. Therefore, the r[easona](#page-6-0)ble agreem[ent](#page-6-0) [is](#page-6-0) obtained between the calculated



**Fig. 5.** Calculated enthalpies of mixing of liquid Ag–Ge alloys at 1250 K in comparison with the experimental data [42–44] (Ref. states: liquid Ag and Ge).

**Fig. 7.** Calculated activity of Ge with the experimental data [45,46] at 1250 K (Ref. state: liquid Ge).

<span id="page-4-0"></span>



**Fig. 8.** Comparison of the calculated enthalpies of mixing of liquid Au–Ag–Ge ternary alloys with the experimental data [48,49] referred to liquid Ag, Au and Ge at 1373 K. (a)  $Au_{0.25}Ge_{0.75}$ -Ag; (b)  $Au_{0.50}Ge_{0.50}$ -Ag and (c)  $Au_{0.75}Ge_{0.25}$ -Ag.

**Fig. 9.** Comparison of the calculated enthalpies of mixing of liquid Au–Ag–Ge ternary alloys with the experimental data [48,49] referred to liquid Ag, Au and Ge at 1373 K. (a)  $Ag_{0.75}Ge_{0.25}$ -Au; (b)  $Ag_{0.50}Ge_{0.50}$ -Au and (c)  $Ag_{0.25}Ge_{0.75}$ -Au.

<span id="page-5-0"></span>

**Fig. 10.** Calculated liquidus projection of the Au–Ag–Ge ternary system in the present work.

results and the experimental information [35–39] in the present work.

The comparison of the enthalpies of mixing of the liquid Ag–Ge alloys between the calculated and experimental values at 1280 K is shown in Fig. 5. It can be seen that the calculated mixing enthalpies agree with the experimental d[ata](#page-6-0) [by](#page-6-0) [Ca](#page-6-0)stanet et al. [42,43] [an](#page-6-0)d Batalin et al. [44] if considering the experimental error.

Fig. 6 compares the calculated activity of Ag in liquid Ag–Ge alloys at 1250 K with the experimental data determined by Batalin [et](#page-3-0) [al.](#page-3-0) [44], Eremenko et al. [45], Martin-Garin et al. [46] and Oktay [47]. The calculated activity of Ag is reasona[bly](#page-6-0) [consi](#page-6-0)stent with the e[xperim](#page-6-0)ental data [44–46], but shows an obvious deviation with the experimental data [47]. Fig. 7 shows the comparison of the calculated activity of Ge in liquid Ag–Ge alloys at 1250 K with the experimental d[ata](#page-6-0) [m](#page-6-0)easured by Ereme[nko](#page-6-0) [et](#page-6-0) al. [45] and Martin-Garin et al. [46]. The calculated activity of Ge is in good agreement with th[e](#page-6-0) [experime](#page-6-0)[ntal da](#page-3-0)ta [45,46].

#### 4.2. The Au–Ag–Ge ternary system

[Com](#page-6-0)bining t[he presen](#page-6-0)t optimization of the Ag–Ge binary system with the previous assessments of the Au–Ag and Au–Ge binary



Fig. 12. Calculated vertical section of  $Ag_{0.50}Au_{0.50}$ -Ge with the experimental data [39].

systems, the Au–Ag–Ge ternary system has been further optimized based on available experimental data. Thermodynamic properties of liquid alloys, liquidus projection and several vertical sections of this ternary system are also calculated and compared with the experimental data in Figs. 8–13. Reasonable agreements are achieved between the calculated results and the experimental data.

Enthalpies of mixing of the liquid Au–Ag–Ge ternary alloys at 1373 K along different across sections were calculated in comparisons with the experimental data measured by Hassam and Gaune-Escard [48] [and](#page-4-0) [Has](#page-4-0)sam et al. [49] as shown in Figs. 8 and 9. As can be seen, the calculated enthalpies of mixing of the liquid ternary alloys along two cross-sections with Ag to Ge ratio of 1:3 and 1:1 at 1373 K show slight deviation from the experimental data [48,49] in Fig. 8(a) and (b). However, the good agreements are [achie](#page-6-0)ved between th[e](#page-6-0) [calcu](#page-6-0)lated ent[halpies](#page-4-0) [of](#page-4-0) [mixi](#page-4-0)ng of the liquid Au–Ag–Ge ternary alloys along three cross sections with Ag to Ge ratio of 3:1, 1:1 and 1:3 and the experimental data at 1373 K in Fig. 9. The calculated results in the present work are still reason[abl](#page-6-0)e [and](#page-4-0) [acc](#page-4-0)eptable if one considers the experimental error (about

1400



C Hassam et al. 1988 1300 1200 Liquid 1100 Temperature, K 1000  $L+$ (Ge) 900 Ìй  $\Omega$ ത്ത Φ  $\alpha$ জা  $\overline{\omega}$ ৩ল  $L+$ fcc(Au,Ag)+(Ge) 800 fcc(Au,Ag) 700 fcc(Au,Ag)+(Ge) 600 500 400  $\mathbf 0$  $0.2$  $0.4$ 0.6  $0.8$  $1,0$ Mole fraction, Ge

Fig. 11. Calculated vertical section of  $Ag_{0.25}Au_{0.75}$ -Ge with the experimental data [39].

**Fig. 13.** Calculated vertical section of  $Ag_{0.75}Au_{0.25}$ -Ge with the experimental data [39].

<span id="page-6-0"></span>8%) of the data measured by Hassam and Gaune-Escard [48] and Hassam et al. [49].

In the Au–Ag–Ge ternary system, invariant reaction associated with liquid phase is a ternary monovariant eutectic reaction. Fig. 10 is the calculated liquidus projection of this ternary system. The monovariant curve  $e_1e_2$  runs smoothly from the Ag–Ge binary eutectic point  $e_1$  to the Au–Ge binary eutectic point  $e_2$ .

Figs. 11–13 are the calculated vertical sections of Ag<sub>0.25</sub>[Au](#page-5-0)<sub>0.75</sub>[–Ge](#page-5-0), Ag<sub>0.50</sub>Au<sub>0.50</sub>–Ge and Ag<sub>0.75</sub>Au<sub>0.25</sub>–Ge in the Au–Ag–Ge ternary system with the experimental data [39], respectively. As can be seen, the calculated phase relations and phase boundaries in Figs. 12 and 13 are in good agreement [with](#page-5-0) the experimental data [39]. In Fig. 11, the calculated phase relations of the  $Ag<sub>0.25</sub>Au<sub>0.75</sub> - Ge$  section are consistent with the experimental results, although the calculated phase boundary for the three-phase field,  $L + fcc(Au, Ag) + (Ge)$ , shows a slight deviation from the ex[perimental](#page-5-0) [data measu](#page-5-0)red by Hassam et al. [39].

### **5. Conclusions**

The Ag–Ge binary system has been reassessed using the CAL-PHAD method through Thermo-calc<sup>®</sup> software package. A set of self-consistent parameters for describing various phases in the Ag–Ge binary system was obtained, which can be used to reproduce well the reported experimental data including phase diagram and thermodynamic properties. Combined the previous assessments of the Au–Ag and Au–Ge binary systems with the available experimental information on the Au–Ag–Ge ternary system, the thermodynamic description of the Au–Ag–Ge ternary system has been developed. The liquidus projection and several vertical sections were calculated. The calculated results are in good agreement with the reported experimental data.

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