



# Terrestrial laser scanning of the main reflector of the Effelsberg 100 m radio telescope

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Manufacterer's model at 70° elev., Courtesy N. Junkes

- Geodesists are interested in gravitationally induced path length variations at different elevation angles
- Astronomers are interested in surface quality

# Principles of terrestrial laser scanners





N.B.: Size of footprint depends on angle of incidence  $1/\cos \gamma \rightarrow$  for  $\gamma = 70^{\circ} \rightarrow$  factor of 3



# Scanning of radio telescopes







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Leica HDS 6100 Terrestrial Laser Scanner

- Scanning in 7 elevations: 90°, 75°, 60°, 45°, 30°, 15°, 7.5°
- Duration: 30 Min per elevation angle
- Spacial resolution: 8 mm x 8 mm (at distance of 50 m)
- Ca. 370 Mio. points per Elevation =  $1.11 \times 10^9$  observations
- Point precision (s = 30 50m): 5 8 mm
- Size of laser spot (foortprint)
  - 9.6 mm/30 m
  - 14 mm/50 m





# Scanning 2010







### **Data decimation**





Constant angular increments lead to inhomogeneous point densities → overweighting of central area lead to wrong estimates if deformations present in this area

#### Original point density



#### Homogeneous point density





### Least squares adjustment



#### Parameters of rotation paraboloid

$$g(\mathbf{x}_i^p, \boldsymbol{x}) = \frac{\mathbf{x}_i^2 + \mathbf{y}_i^2}{4f} - \mathbf{z}_i = 0$$

#### With transformations

$$\mathbf{x}_i^p = \mathbf{R}_x(\varphi_x) \cdot \mathbf{R}_y(\varphi_y) \cdot \mathbf{x}_i^l - \mathbf{x}_v$$

Parameters of rotational paraboloid

$$\boldsymbol{x} = [\mathbf{x}_v \ \mathbf{y}_v \ \mathbf{z}_v \ \varphi_x \ \varphi_y \ f]^T$$

- Outer 10m ring not used for parameter estimation (unreliable)
- Outlier elimination (distance threshold)
- Adjustment with Gauß-Helmert-Model
- Cluster,130 GB memory, 4 h per elevation







### **Focal length results**







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### Micro surfaces

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## Spline approximations









### Comparisons









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#### Leica Scan Station P20

- Scanning in 7 elevations: 90°, 75°, 60°, 45°, 30°, 15°, 7.5°
- Duration: 15 Min per elevation angle
- Spacial resolution: 6 mm x 6 mm (at distance of 50 m)
- Ca. 500 Mio. points per Elevation =  $1.5 \times 10^9$  observations
- Point precision (s = 30 50m): 2 4 mm
- Size of laser spot (foortprint)
  - 8,8 mm/30 m
  - 12.8 mm/50 m





## Scanning after sunset













### 7.5° Elevation



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### **Raw results**

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Scanner has instrumental errors

 b) Estimation of form paramaters depends on data density



### **Results after calibrations**

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- Data density
- Horizontal collimation error
- Trunnion axis error
- Vertical index error
- Eccentricities of graduated circles
- Eccentricities of axes



## Focal lengths of 2010 and 2013







# Reflectivity







### **Radial residuals I**







### **Radial residuals II**







### Elev. 60°, Panel 800

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Residuals at elevation 60°













## Panels at 7.5° elevation









## Panels at 7.5° elevation







## Panels at 90° elevation



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- Terrestrial laser scanners (TLS) have dominant systematic errors, which need to be calibrated/corrected for
- Position of TLS is important (near primary focus)
- Data analysis for radio telescopes requires sophisticated pre-processing steps



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