

Mechanism for bipolar resistive switching in transition-metal oxidesM. J. Rozenberg,^{1,2} M. J. Sánchez,³ R. Weht,^{4,5} C. Acha,² F. Gomez-Marlasca,⁴ and P. Levy⁴¹*Laboratoire de Physique des Solides, UMR 8502, Université Paris-Sud, Orsay 91405, France*²*Departamento de Física J. J. Giambiagi, FCEN, Universidad de Buenos Aires, Ciudad Universitaria Pab. I, 1428 Buenos Aires, Argentina*³*Centro Atómico Bariloche and Instituto Balseiro, CNEA, 8400 San Carlos de Bariloche, Argentina*⁴*Gerencia de Investigación y Aplicaciones, CNEA, 1650 San Martín, Argentina*⁵*Instituto Sabato, Universidad Nacional de San Martín–CNEA, 1650 San Martín, Argentina*

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We introduce a model that accounts for the bipolar resistive switching phenomenon observed in transition-metal oxides. It qualitatively describes the electric-field-enhanced migration of oxygen vacancies at the nanoscale. The numerical study of the model predicts that strong electric fields develop in the highly resistive dielectric-electrode interfaces leading to spatially inhomogeneous oxygen vacancies distribution and a concomitant resistive switching effect. The theoretical results qualitatively reproduce nontrivial resistance hysteresis experiments that we also report providing key validation to our model.

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I. INTRODUCTION

There is a great deal of experimental activity currently devoted to explore new technologies for the next generation of electronic memory devices.¹ Among various promising options, the resistive random access memory (RRAM), which is based on the resistive switching (RS) phenomenon, has emerged as a preeminent candidate.^{2,3} The RS effect is a large, reversible, and nonvolatile change in the resistance after the application of voltage or current pulses. The typical RRAM system has a capacitorlike structure composed of insulating or semiconducting materials sandwiched between two metal electrodes. RS has been observed in a wide variety of systems such as simple and complex oxides, organic compounds, etc.^{3,4} However, there are specific characteristics of the switching behavior observed in each type of material. In the case of binary oxides, which are highly insulating, it is believed that the RS effect may be due to the formation and rupture of conductive filaments within the insulating media.^{5–7} In contrast, in the more conducting or semiconducting complex oxides with perovskite structures, such as doped cuprates and manganites, the relevance of oxygen vacancies is often invoked. Despite a bursting body of experimental data that is rapidly becoming available^{8–12} the precise mechanism behind the physical effect of RS remains elusive. A few qualitative models have been proposed emphasizing different aspects: electric-field-induced defect migration,^{5,13,14} phase separation,¹⁵ tunneling across interfacial domains,¹⁶ control of the Schottky barrier's height,^{3,17} etc. A general consensus has emerged on the empirical relevance of three key features: (i) a highly spatially inhomogeneous conduction in the low resistive state, (ii) the existence of a significant number of oxygen vacancy defects, and (iii) a preeminent role played by the interfaces, namely, the regions of the oxide that are near each of the metallic electrodes which often form Schottky barriers. Here, we shall introduce and study the behavior of a simple model that incorporates, at a qualitative level, those three features. By means of a numerical simulation we shall show that the

model correctly reproduces key nontrivial hysteresis cycles observed in experiments on perovskite-type transition-metal oxides (TMO).

II. MODEL

Several experiments revealed that the conduction in the low resistive state is highly inhomogeneous and dominated by one-dimensional paths that are associated with enhanced conduction channels.^{5,7} These paths would be created upon an initial application of strong electric fields that bring the dielectric close to its breakdown point. Thus, we shall assume that the electric transport is dominated by a single conductive path embedded within a more insulating host.

The second important feature incorporated into our model is the relevance of defects within the dielectric. Several experiments point to a preeminent role played by oxygen vacancies.^{5,14,18,19} Moreover, it is a universal and salient feature of TMO that their resistivity is dramatically affected by the precise oxygen stoichiometry. One may thus expect that oxygen vacancy concentration may be the most significant parameter controlling the *local* resistivity, ρ , of a given material. This feature is included in our model by assuming that each nanodomain of the path is characterized by a certain concentration of oxygen vacancy defects, δ . We adopt the most simple linear relation $\rho \propto \delta$, which follows from the fact that in TMO perovskites the presence of oxygen vacancies severely disrupts the electronic conduction properties. Nevertheless, we emphasize that the specific form of $\rho(\delta)$ is not crucial for the results that we shall describe later on.

The third important feature that our model incorporates is the key role played by the interfaces,¹⁶ namely, the regions of the dielectric that are in physical proximity to the metallic electrodes. There is growing evidence that these are the regions where the RS takes place.^{13,17,20–23}

Our model is schematically shown in Fig. 1 and consists of a single conductive channel within a more insulating dielectric, which is represented by a one-dimensional resistive network on N links. The first and last N_l links correspond to

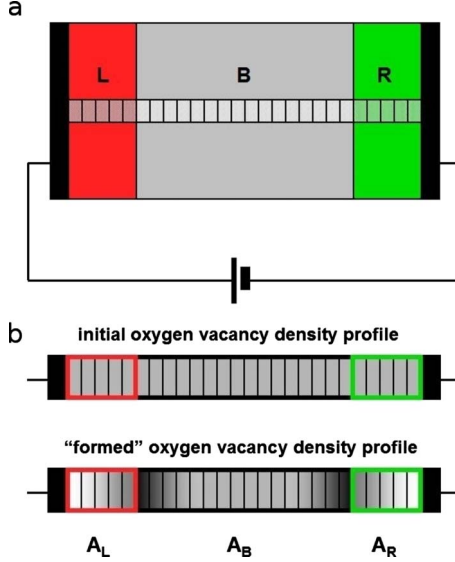


FIG. 1. (Color online) (a) Schematic model with a single conductive channel within the dielectric. The three regions L , R , and B correspond to the two high resistance interfaces and the more conductive central bulk, respectively. The small boxes indicate the domains. (b) Detailed scheme of the conductive path. The grayscale qualitatively depicts the variation in the oxygen vacancy concentration through the channel (darker corresponds to higher concentration). The top figure shows the initial state with uniformly distributed oxygen vacancies and the bottom one shows the inhomogeneous distribution after the first few “forming” voltage cycles (see text).

high resistance interfacial regions next to the external electrode, and the central $N-2N_I$ links describe the bulk section. Each link is characterized by a certain concentration of oxygen vacancies, which determines the resistivity of the link. They may be physically associated to small domains of nanoscopic dimensions which may actually correspond to grains of the polycrystalline oxide. We take $\rho_i = A_\alpha \delta_i$, with $\alpha = B$ if i is in the bulk ($N_I < i \leq N - N_I$), $\alpha = L$ if i is in the left interface ($i \leq N_I$), and $\alpha = R$ if i is in the right interface ($N - N_I < i \leq N$). In our study we set $N = 100$ and $N_I = 10$. The following equation specifies how the vacancies diffuse through the network domains under an external voltage:

$$p_{ab} = \delta_a (1 - \delta_b) \exp(-V_0 + \Delta V_a). \quad (1)$$

It gives the probability for transfer of vacancies from domain a to a nearest-neighbor domain b . The probability is proportional to the concentration of vacancies present in domain a and to the concentration of “available vacancy sites” at the target domain. The Arrhenius factor $\exp(-V_0)$ is controlled by a dimensionless constant, V_0 , related to the activation energy for vacancies diffusion. The important factor $\exp(\Delta V_a)$ models the enhancement (or suppression) of the diffusive process due to the local electric field at domain a .

From Eq. (1), a constant V_0 leads to an initially constant distribution $\delta_i = \delta_o$ for all i . The value of the initial constant concentration, δ_o , must be much smaller than 1, since it physically represents the concentration of defects (oxygen vacancies) within a domain. We adopt $\delta_o = 10^{-4}$.

Similarly to actual resistive switching experiments, we simulate the applied voltage protocol $V(t)$ by linear ramps that follow the sequence $0 \rightarrow +V_{\max} \rightarrow 0 \rightarrow -V_{\max} \rightarrow 0$ (our convention is that the right electrode is grounded). The duration is of s time steps. The sequence may be repeated a number of cycles n for a total duration $\tau_{\max} = ns$. In our simulations we choose $V_0/V_{\max} = 0.016$, which provides a non-negligible but slow diffusive contribution to the evolution of δ_i with respect to the total time duration of the simulations (i.e., the total number of time steps). We set $V_{\max} = 1000$ that provides for a sufficiently large electric stress. Our qualitative results are rather robust with respect to the choice of model parameters; a detailed systematic study of their dependence is left for future work.

The coefficients A_B , A_R , and A_L still remain to be specified. With no loss of generality, we fix the value of the bulk coefficient to unity $A_B = 1$ and leave the interfacial A_R and A_L free. In this initial study we shall concentrate in the symmetric case, $A_R = A_L$, that corresponds to most common experimental devices.

The numerical simulations are performed through the following steps: (i) at each simulation time step t ($1 \leq t \leq \tau_{\max}$) a given external voltage $V(t)$ is applied to the resistive network (the electrodes are assumed perfect conductors). The current through the system is computed as $I(t) = V(t)/R_T$, with R_T as the total (i.e., two terminal) resistance

$$R_T = c \sum_{i=1}^N \rho_i = \sum_{\alpha} \sum_{i \in \alpha} A_\alpha \delta_i, \quad (2)$$

where $\alpha = R, B, L$ denotes the three network regions and c denotes an unessential geometrical constant related to the dimensions of the domains (which we set to unity). (ii) We compute the local voltage profile $V_i(t) = I(t)\rho_i$ and the voltages drops $\Delta V_i(t) = V_{i+1}(t) - V_i(t)$. (iii) We use Eq. (1) to compute all the oxygen vacancy transfers between nearest neighboring domains and update the values $\delta_i(t)$ to a new set of concentrations $\delta_i(t+1)$. (iv) We use these new values to recompute the current at τ_{t+1} under the applied voltage $V(t+1)$ as indicated in the first step.

III. NUMERICAL RESULTS AND COMPARISON TO EXPERIMENTS

We now turn to the discussion of our results. We set $A_R = A_L = 1000 \gg A_B = 1$, which is consistent with our experimental data and with previous reports in bulk and thin films of conducting perovskites.^{14,21,25} In Fig. 2 we show the results for the hysteresis loop of the total resistance R_T . The different data curves in Fig. 2(a) display the results in subsequent voltage cycles 5, 6, and 7. The inset of Fig. 2(a) shows that the hysteresis as a function of current remains qualitatively similar. We note that during the first few initial cycles the resistance shows nonrepetitive memory effects that converge to a hysteresis loop with a stable shape. Interestingly, this is reminiscent of the initial “forming” that experimental samples seem to require in order to start displaying reproducible switching effects. The peculiar type of hysteresis loop that we obtain has been already reported by the Houston

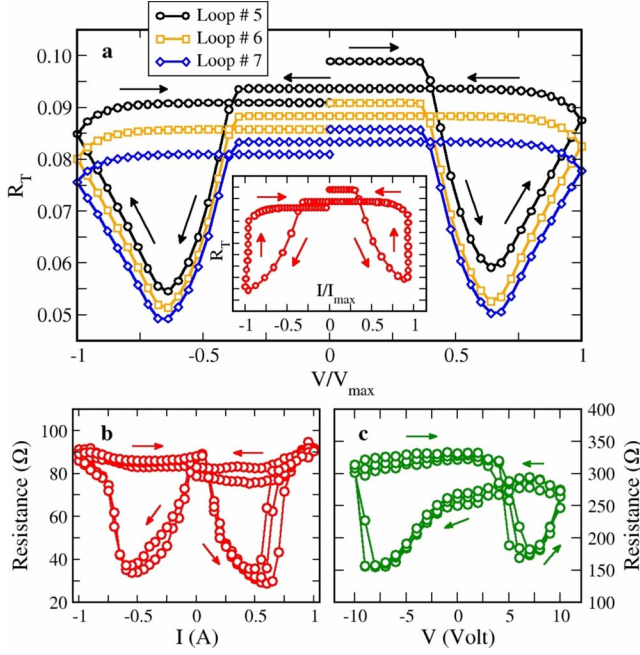


FIG. 2. (Color online) Top panel: resistive hysteresis loop (R_T vs V) for the subsequent voltage cycles number 5, 6, and 7. (a) Inset: the R_T vs I hysteresis (loop number 5) shows qualitatively similar results (the vertical axis scale is the same as in the main figure). Bottom panel: experimental hysteresis loops measured in (b) manganite and (c) cuprate devices. The first one was pulsed in current control mode while the second in voltage mode. The details of the experimental procedures are described in Refs. 21 and 25, respectively.

group²⁴ in experiments on (Pr,Ca)MnO₃ manganite systems, where it has been termed “table with legs.” It is evidently a nontrivial effect and we have experimentally reproduced it in both, a related manganite (Pr,La,Ca)MnO₃ and a cuprate (YBa₂Cu₃O_{7-x}) sample, as shown in the bottom panels of Fig. 2.

There are several features worth pointing out: during each voltage protocol loop, there is a clear variation of the resistance R_T between a rather broad maximum for a large range of V (i.e., the “table”) and two relatively narrow minima (i.e., the “legs”). These maximum and minima correspond to the high and low resistance states, R_T^{HI} and R_T^{LO} . The $R_T(V)$ loops are approximately symmetric in V which reflects the left-right symmetry of the system. Throughout the voltage loop, the system begins in the initial R_T^{HI} state and undergoes the sequence of resistance changes $\rightarrow R_T^{LO+} \rightarrow R_T^{HI+}$ under positive bias and then $\rightarrow R_T^{LO-} \rightarrow R_T^{HI-}$ under negative bias. The final state at zero bias is R_T^{HI} , very close but not identical to the previous initial state. Interestingly, a similar small drift is also observed in the experimental data.

The qualitative agreement between our prediction of the table with legs and the experimentally observed hysteresis loops provides a significant validation for our model. Therefore, to gain physical insight into the mechanism of the RS effect we shall discuss in detail the evolution of the vacancies distribution under the applied voltage protocol. In Fig. 3 we show successive snapshots of the oxygen vacancy concentration profile δ_i at the beginning of loops 5, 6, and 7.

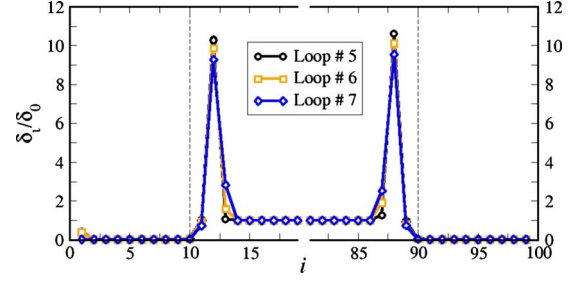


FIG. 3. (Color online) Density concentration profiles normalized to the initial uniform density value δ_i/δ_0 at the beginning of voltage cycles number 5, 6, and 7 in the symmetric system.

Recalling that the initial equilibrium distribution of oxygen vacancy concentration is uniform $\delta_i = \delta_0$, these curves reveal that, under the action of the repetitive voltage cycling, the δ_i evolve toward a new stable distribution. The salient features of the profile δ_i are a significant depletion in the interfacial regions and a strong accumulation peaks at both internal boundaries between the bulk and the interfacial regions. The reason can be understood as follows. The largest electric fields occur at the two interfacial regions since initially their resistance is much larger than the bulk one ($A_L, A_R \gg A_B$). Therefore, oxygen vacancy migration is enhanced in the interfacial regions, with the ions moving either toward the electrodes or the bulk, depending on the direction of the applied voltage. When the ions reach the metallic electrodes they start to pile up.¹⁴ On the other hand, the vacancies that migrate toward the bulk eventually leave the interfacial region and enter the bulk. There, their diffusion virtually stops, since the electric fields in the more conducting bulk are much smaller. Successive initial cycles yield a cumulative effect, with a depletion of the interfacial regions (and some pileup at the edges) and a concomitant accumulation at the bulk side of the interfacial/bulk boundary. Significantly this accumulation, as seen in Fig. 3, is quite large and narrow leading to a substantial increase in the local resistance. This feature will be a key to understand the origin of the legs of the hysteresis loop, which we shall consider next.

In Fig. 4 we show snapshots, during the first half of the voltage cycle, of the vacancy concentration and local resistance profiles in the interfacial regions and their boundaries with the bulk. These are the active regions of the system where the electric-field-enhanced migration takes place. Notice that since the current $I(t)$ is uniform along the conductive path, the local electric fields are directly proportional to the local resistance. Let us start at $V=0$, from the state at the beginning of a cycle. Interestingly, the ρ_i profile indicates significant electric fields in both interfacial regions which extends into the neighboring bulk. Thus, the depletion of vacancies in the interfaces and the accumulation at the boundaries are such that compensate for the difference between the respective A coefficients to yield similar electric fields across the boundaries of the regions. Yet, at the very left end of the system there is a small pileup of vacancies which, as soon as the voltage is ramped up, will translate into the largest local fields and initiate the ionic migration. At $V/V_{\max}=0.25$, we observe a snapshot of the migration of the vacancies across the left interfacial region toward the bulk.

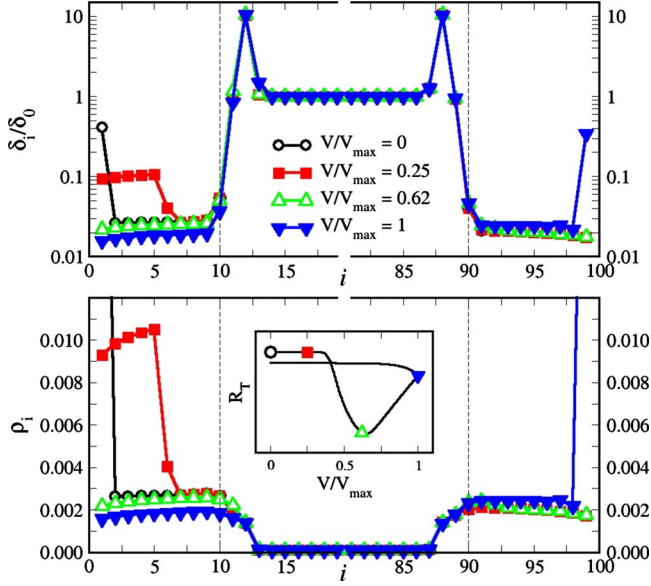


FIG. 4. (Color online) Top (semi-log scale): snapshots of the density concentration profiles for the symmetric configuration normalized to the initial uniform density value δ_i/δ_0 during the hysteresis cycle (first half). Bottom: the corresponding profiles of local resistance ρ_i for the same snapshots. Inset: position of the snapshots in the (first half) hysteresis loop.

From the resistance expression Eq. (2), so long as the vacancies remain within the interfacial region, the system remains in R_T^{HI} state. At $V/V_{\max}=0.62$, the vacancies have moved out of the left interfacial region and entered the bulk, where their migration suddenly stops. Once in the bulk, the contribution

to the total resistance of these migrating vacancies is reduced ($A_B \ll A_L$); thus, the system reaches the R_T^{LO} state (leg of the table). Notice that in this state, the largest fields occur at the boundaries of the bulk and the interfacial regions. Thus, as V is further increased, the left interfacial region depletes further and therefore the voltage drop gets lower there. In contrast, on the right side the electric fields are further enhanced and there is now a migration of vacancies from the accumulation peak of the bulk toward the right interfacial region. This leads to an increase in the total resistance and, at the maximal voltage $V/V_{\max}=1$, we find that the vacancies have entered the interfacial region and already piled up at the right end. Thus, the system is back to R_T^{HI} . The voltage protocol continues with the decrease of V back to zero but keeping the same (positive) polarity. Therefore, no significant change in the δ_i and ρ_i profiles occurs and half of the table with legs is already formed. When the negative polarity part of the cycle begins a similar analysis follows, since the distribution of vacancy concentrations is a mirror image of the initial one. This forms the other half of the table.

To complete our study we consider the effect of introducing an asymmetry in the model parameters A_R and A_L . In Fig. 5 we display the results for the hysteresis loops upon increasing the asymmetry. The results of the simulations show the gradual evolution of the table with legs toward a conventional rectangular hysteresis cycle.²⁴ Asymmetry in experimental samples can either be due to the fabrication process, as for instance, in the obvious case of using a different type of metal for the electrodes. Though our samples were fabricated in a symmetric configuration, we induced a significant asymmetry by vigorous pulsing with a given polarity (i.e., poling) before measuring the resistance hysteresis character-

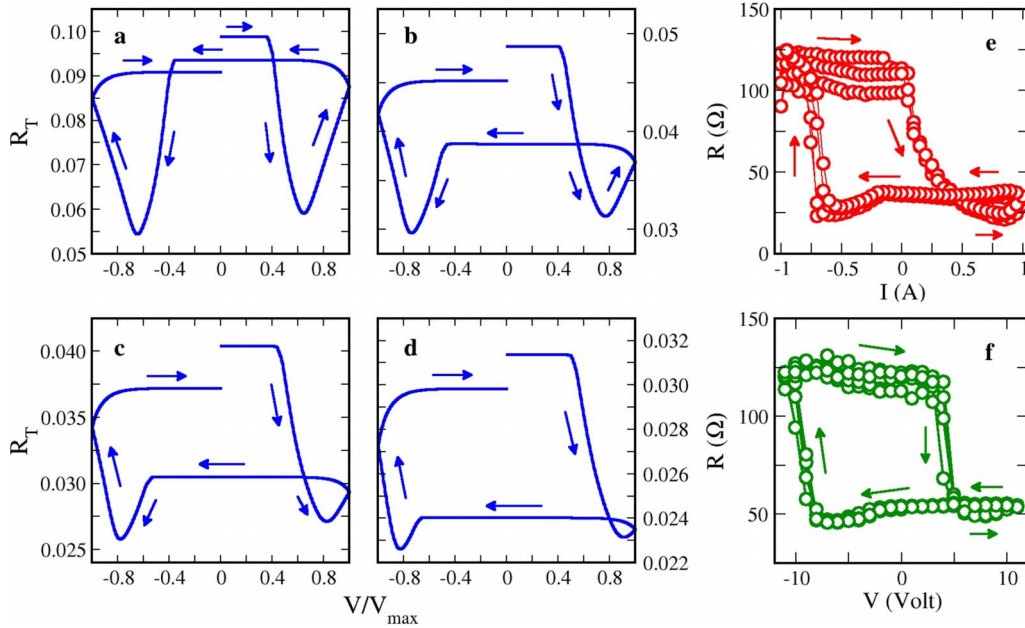


FIG. 5. (Color online) Resistive hysteresis loops obtained for an increasing degree of asymmetry. $A_L=1000$ and $A_R=1000, 100, 50$, and 25 in panels (a), (b), (c), and (d), respectively. The right panels show experimental data for a manganite (e) and a cuprate sample (f) that were rendered asymmetric by means of intense and fixed polarity pulsing. The former was pulsed in current control mode and the latter in voltage control similarly as in Refs. 21 and 25, respectively. Notice the qualitative similarity of data of panels (e) and (f) with panel (d) and of data in Fig. 2(b) with panel (a). The data of Fig. 2(c) seem to be in between the results of panels (a) and (b).

istic. Significantly, as shown in Fig. 5, we find that the experimental data obtained in an asymmetric manganite sample and the cuprate, induced by intensive same polarity pulsing, are in good qualitative agreement with our simulations. These results provide additional validation to our model.

IV. CONCLUSIONS

To conclude, our results put on solid theoretical grounds the key role played by oxygen vacancies in the mechanism of resistive switching in TMO. They also provide valuable insights, predicting a nontrivial spatial profile of the oxygen

vacancy distribution which may be of help for device design. An exciting idea for future work is to explore the possibility of using atomistic first-principles calculations to study properties of electrode–transition-metal oxide interfaces to estimate the parameters of the model and provide guidance in the material choice for actual memory devices.

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- ¹G. I. Meijer, *Science* **319**, 1625 (2008).
 - ²R. Waser and M. Aono, *Nature Mater.* **6**, 833 (2007).
 - ³A. Sawa, *Mater. Today* **11**, 28 (2008).
 - ⁴M. Janousch, G. I. Meijer, U. Staub, B. Delley, S. F. Karg, and B. P. Andreasson, *Adv. Mater.* **19**, 2232 (2007).
 - ⁵K. Szot, W. Speier, G. Bihlmayer, and R. Waser, *Nature Mater.* **5**, 312 (2006).
 - ⁶I. H. Inoue, S. Yasuda, H. Akinaga, and H. Takagi, *Phys. Rev. B* **77**, 035105 (2008).
 - ⁷K. Fujiwara, T. Nemoto, M. J. Rozenberg, Y. Nakamura, and H. Takagi, *Jpn. J. Appl. Phys.* **47**, 6266 (2008).
 - ⁸I. G. Baek, M. S. Lee, S. Seo, M. J. Lee, D. H. Seo, D.-S. Suh, J. C. Park, S. O. Park, H. S. Kim, I. K. Yoo, U.-I. Chung, and J. T. Moon, *Tech. Dig.-Int. Electron Devices Meet.* (2004) 587.
 - ⁹S. Q. Liu, N. J. Wu, and A. Ignatiev, *Appl. Phys. Lett.* **76**, 2749 (2000).
 - ¹⁰A. Beck, J. G. Bednorz, Ch. Gerber, C. Rossel, and D. Widmer, *Appl. Phys. Lett.* **77**, 139 (2000).
 - ¹¹Y. Watanabe, J. G. Bednorz, A. Bietsch, Ch. Gerber, D. Widmer, A. Beck, and S. J. Wind, *Appl. Phys. Lett.* **78**, 3738 (2001).
 - ¹²B. J. Choi, D. S. Jeong, S. K. Kim, C. Rohde, S. Choi, J. H. Oh, H. J. Kim, C. S. Hwang, K. Szot, R. Waser, B. Reichenberg, and S. Tiedke, *J. Appl. Phys.* **98**, 033715 (2005).
 - ¹³A. Baikalov, Y. Q. Wang, B. Shen, B. Lorenz, S. Tsui, Y. Y. Sun, Y. Y. Xue, and C. W. Chu, *Appl. Phys. Lett.* **83**, 957 (2003).
 - ¹⁴Y. B. Nian, J. Strozier, N. J. Wu, X. Chen, and A. Ignatiev, *Phys. Rev. Lett.* **98**, 146403 (2007).
 - ¹⁵N. A. Tulina, S. A. Zver'kov, Y. M. Mukovskii, and D. A. Shulyatev, *Europhys. Lett.* **56**, 836 (2001); N. A. Tulina, *Phys. Usp.* **50**, 1171 (2007).
 - ¹⁶M. J. Rozenberg, I. H. Inoue, and M. J. Sánchez, *Phys. Rev. Lett.* **92**, 178302 (2004).
 - ¹⁷D. S. Jeong, H. Schroeder, and R. Waser, *Phys. Rev. B* **79**, 195317 (2009).
 - ¹⁸D.-J. Seong, M. Jo, D. Lee, and H. Hwang, *Electrochem. Solid-State Lett.* **10**, H168 (2007).
 - ¹⁹S. Tsui, A. Baikalov, J. Cmaidalka, Y. Y. Sun, Y. Q. Wang, Y. Y. Xue, C. W. Chu, L. Chen, and A. J. Jacobson, *Appl. Phys. Lett.* **85**, 317 (2004).
 - ²⁰X. Chen, N. J. Wu, J. Strozier, and A. Ignatiev, *Appl. Phys. Lett.* **87**, 233506 (2005).
 - ²¹M. Quintero, P. Levy, A. G. Leyva, and M. J. Rozenberg, *Phys. Rev. Lett.* **98**, 116601 (2007); F. Gomez-Marlasca and P. Levy, *J. Phys.: Conf. Ser.* **167**, 012036 (2009).
 - ²²A. Sawa, T. Fujii, M. Kawasaki, and Y. Tokura, *Appl. Phys. Lett.* **85**, 4073 (2004).
 - ²³T. Fujii, M. Kawasaki, A. Sawa, H. Akoh, Y. Kawazoe, and Y. Tokura, *Appl. Phys. Lett.* **86**, 012107 (2005).
 - ²⁴A. Ignatiev, N. J. Wu, X. Chen, Y. B. Nian, C. Papagianni, S. Q. Liu, and J. Strozier, *Phase Transitions* **81**, 791 (2008).
 - ²⁵C. Acha and M. J. Rozenberg, *J. Phys.: Condens. Matter* **21**, 045702 (2009); C. Acha, *Physica B: Condens. Matter* **404**, 2746 (2009).